



# Introduction to Cipher Systems

**Saad Al-Momen**



**CIPHER SYSTEMS**

**Fourth Class**

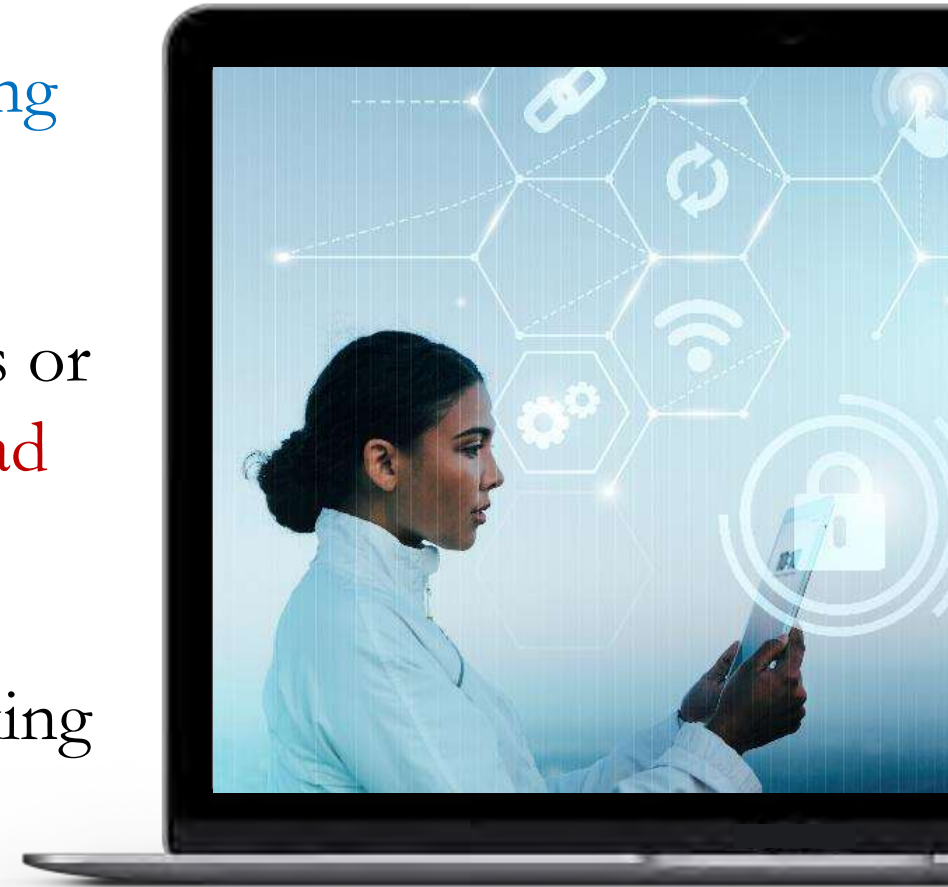
**Department of Mathematics**

**College of Science - University of Baghdad**

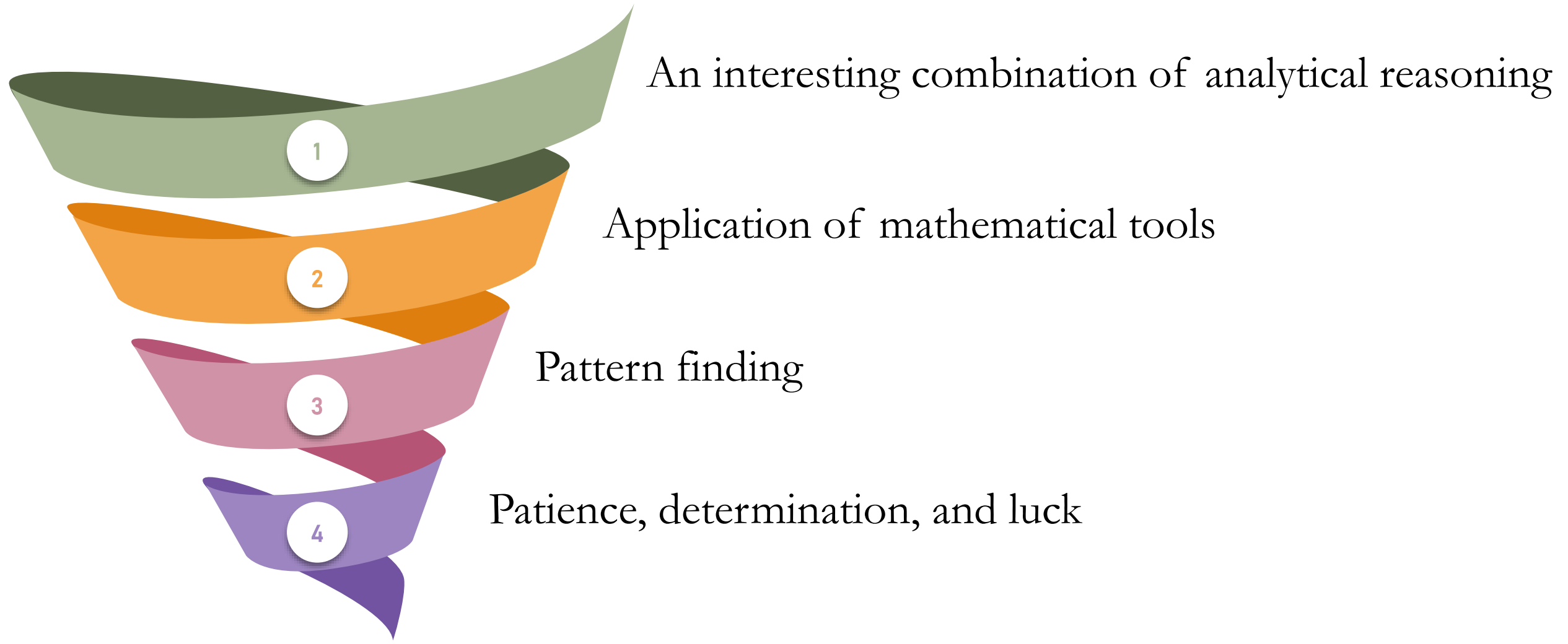


# What is Cryptography?

- Cryptography is the science of using mathematics to encrypt and decrypt data.
- Cryptography is the study of **secret (crypto-) writing (-graphy)**.
- Cryptography enables you to store sensitive information or transmit it across insecure channels or networks (like the Internet) so that it **cannot be read** by anyone except the intended recipient.
- **Cryptography** is the science of securing data.
- **Cryptanalysis** is the science of analyzing and breaking secure communication.

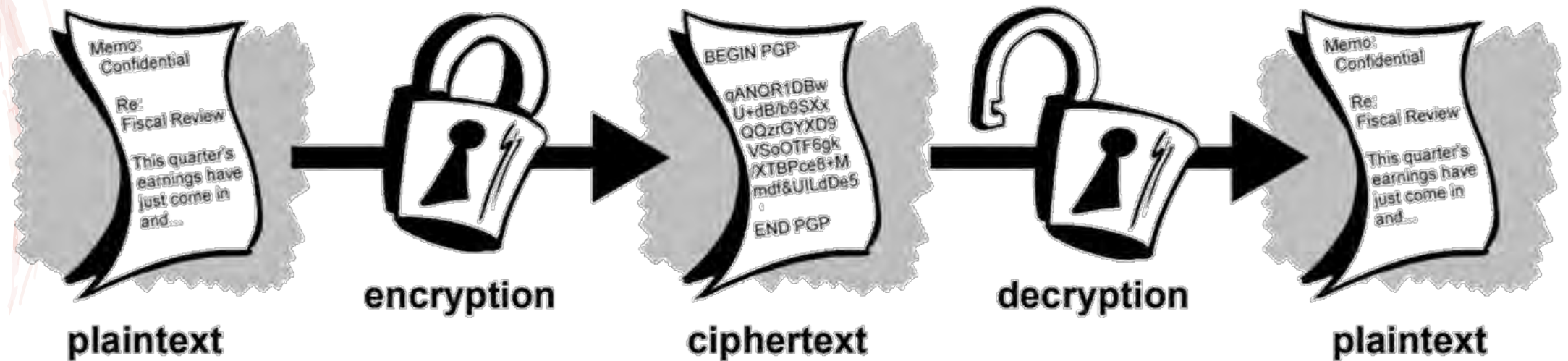


# Classical Cryptanalysis Involves





# How does Cryptography Work?



The security of encrypted data is entirely dependent on two things:

- The strength of the cryptographic algorithm.
- The secrecy of the key.



# **Basic Concepts**

# Encryption domains and codomains

**A** denotes a finite set called the *alphabet of definition*. For example,  $A = \{0;1\}$ , or the English alphabet  $A = \{a, b, \dots, z\}$ .

**M** denotes a set called the *message space*. **M** consists of strings of symbols from an alphabet of definition. An element of **M** is called a *plaintext*.

**C** denotes a set called the *ciphertext space*. **C** consists of strings of symbols from an alphabet of definition, which may differ from the alphabet of definition for **M**. An element of **C** is called a *ciphertext*.

# Encryption and decryption transformations

$\mathbf{K}$  denotes a set called the *key space*. An element of  $\mathbf{K}$  is called a *key*.

Each element  $e \in \mathbf{K}$  uniquely determines a *bijection* from  $\mathbf{M}$  to  $\mathbf{C}$ , denoted by  $E_e$ .  $E_e$  is called an *encryption function* or an *encryption transformation*. Note that  $E_e$  must be a bijection if the process is to be reversed and a unique plaintext message recovered for each distinct ciphertext.

For each  $d \in \mathbf{K}$ ,  $D_d$  denotes a *bijection* from  $\mathbf{C}$  to  $\mathbf{M}$  (i.e.,  $D_d: \mathbf{C} \rightarrow \mathbf{M}$ ).  $D_d$  is called a *decryption function* or *decryption transformation*.

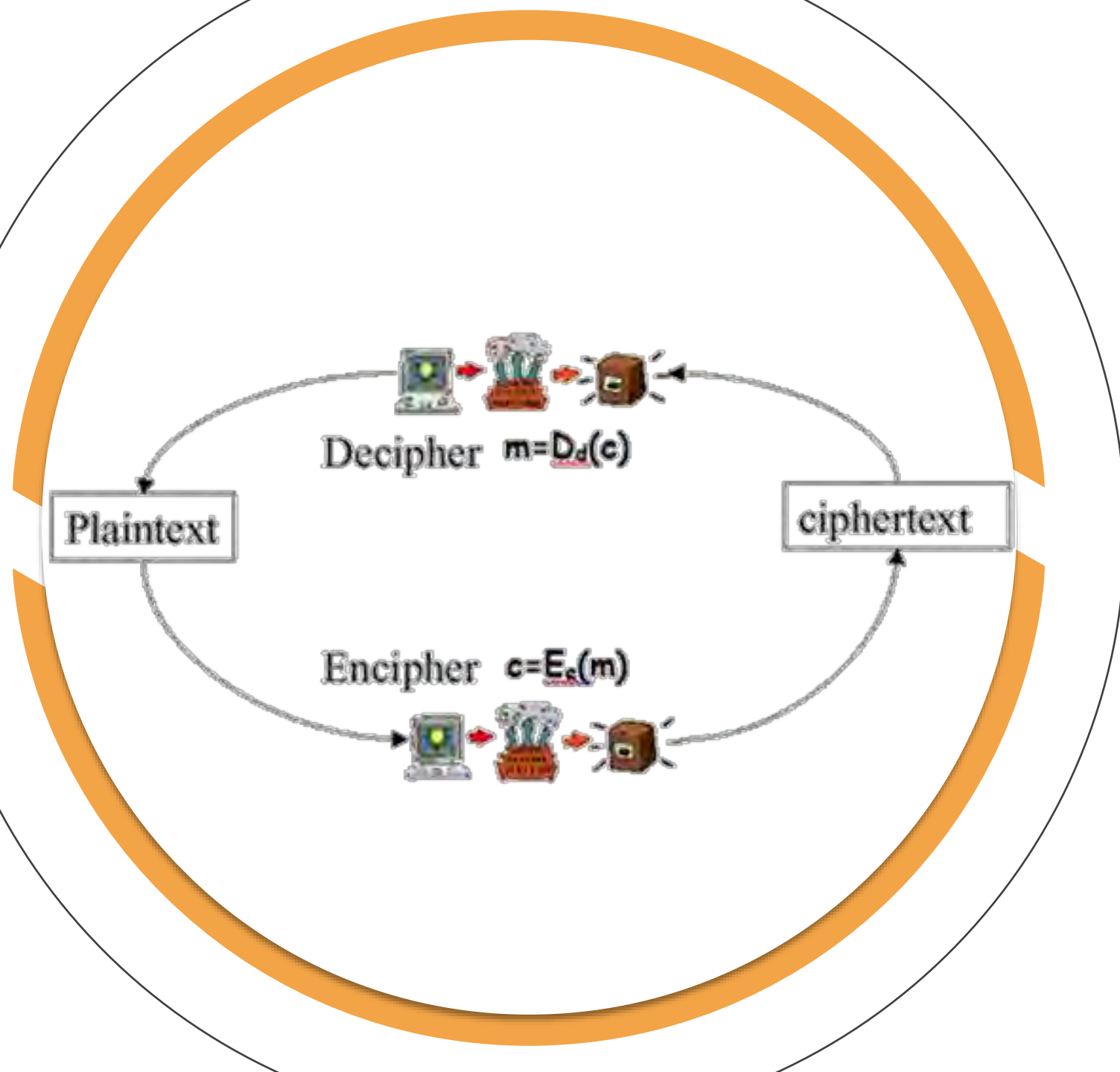
# Encryption and decryption transformations

The process of applying the transformation  $E_e$  to a message  $m \in \mathbf{M}$  is usually referred to as *encrypting*  $m$  or the *encryption* of  $m$ .

The process of applying the transformation  $D_d$  to a ciphertext  $c$  is usually referred to as *decrypting*  $c$  or the *decryption* of  $c$ .

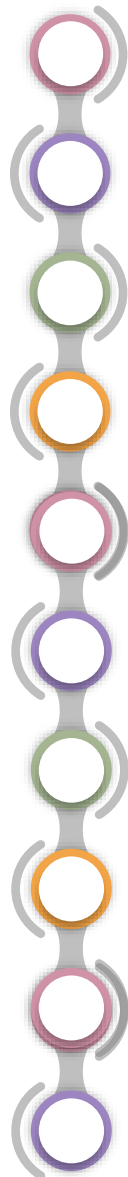
An *encryption scheme* consists of a set  $\{E_e: e \in \mathbf{K}\}$  of encryption transformations and a corresponding set  $\{D_d: d \in \mathbf{K}\}$  of decryption transformations with the property that for each  $e \in \mathbf{K}$  there is a unique key  $d \in \mathbf{K}$  such that  $D_d = E_e^{-1}$ ; that is,  $D_d(E_e(m)) = m$  for all  $m \in \mathbf{M}$ . An encryption scheme is sometimes referred to as a *cipher*.

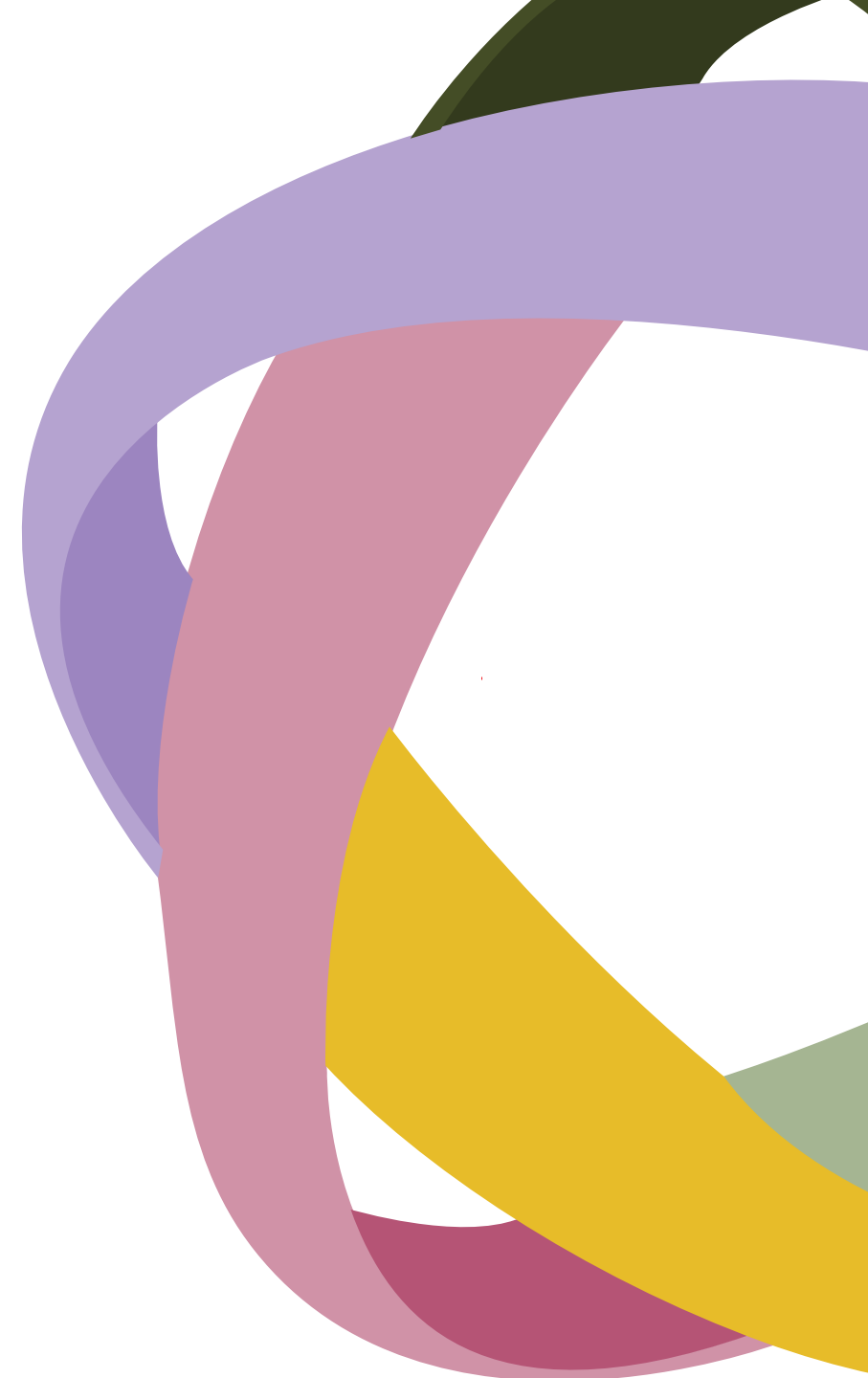
# Secret Writing

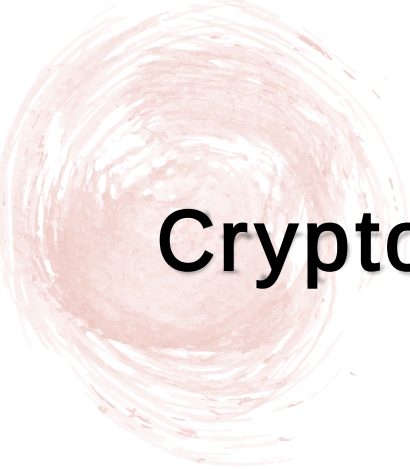




# **Terminology**

- 
-  *Cryptography*
  -  *Plaintext*
  -  *Ciphertext*
  -  *Cipher*
  -  *Key*
  -  *Encipher (Encode)*
  -  *Decipher (Decode)*
  -  *Cryptanalysis*
  -  *Cryptology*
  -  *Cryptanalyst*





# Cryptography

The art or science encompassing the principles and methods of transforming an **intelligible message** into one that is **unintelligible**, and then retransforming that message back to its original form.

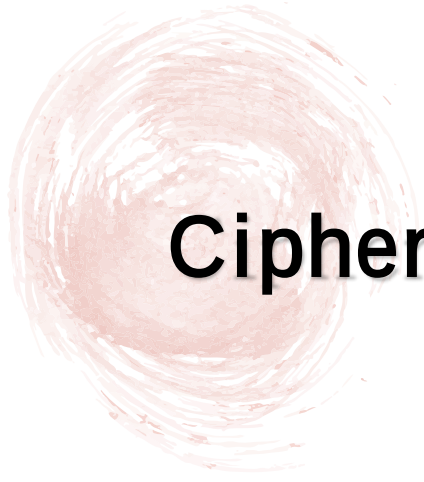




# Plaintext

The original **intelligible** message.





# Ciphertext

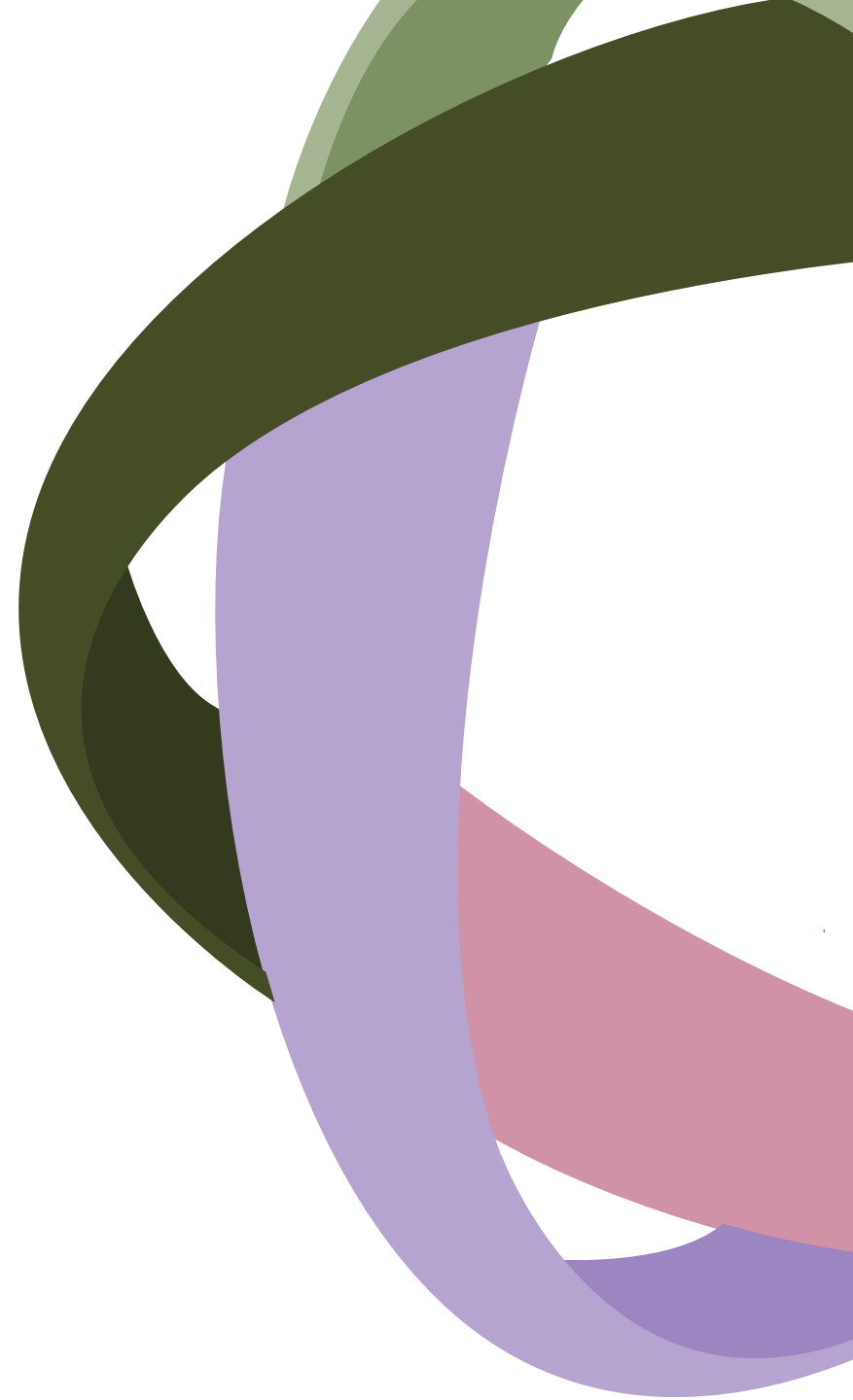
The transformed message, i.e.  
**unintelligible** message.





# Cipher

An **algorithm** for transforming an intelligible message into one that is unintelligible by transposition and/or substitution methods.

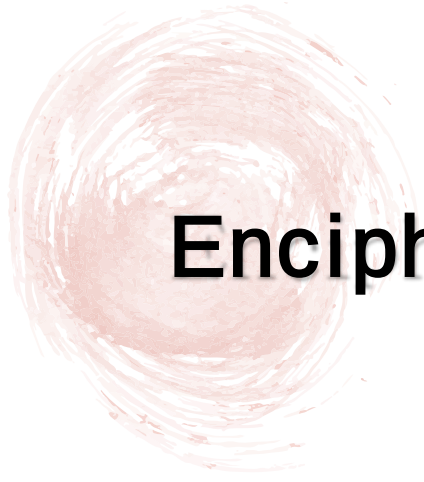




# Key

Some **critical information** used by the cipher, known only to the sender & receiver.





## Encipher (Encode)

The process of converting **plaintext** to **ciphertext** using a cipher and a key.





## Decipher (Decode)

The process of converting **ciphertext** back into **plaintext** using a cipher and a key.

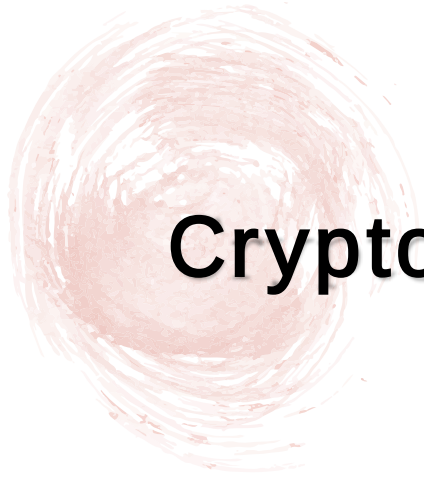




# Cryptanalysis

The study of principles and methods of transforming an unintelligible message back into an intelligible message **without** knowledge of the key. Also called codebreaking.





# Cryptology

**Both** cryptography and cryptanalysis.



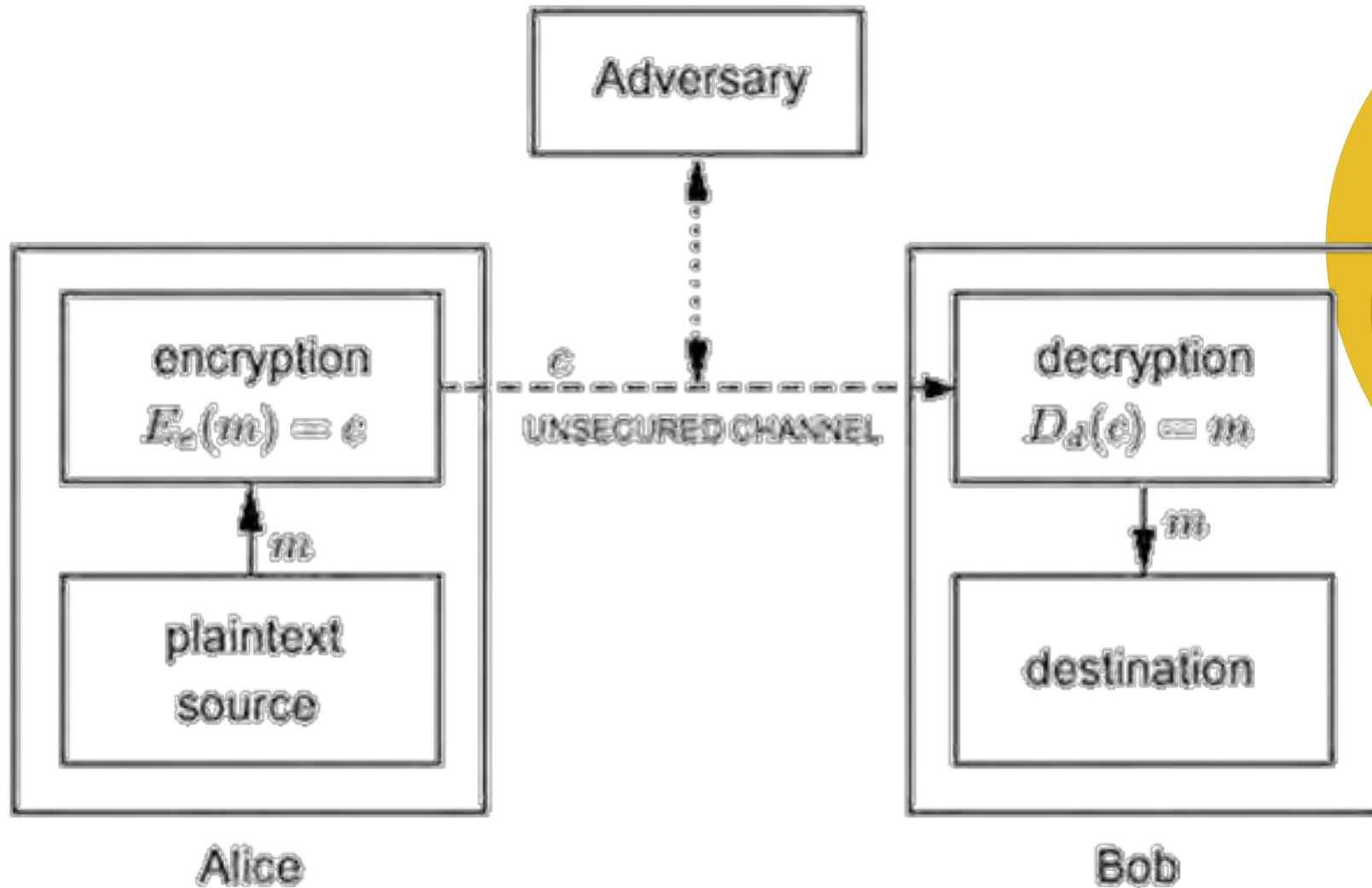


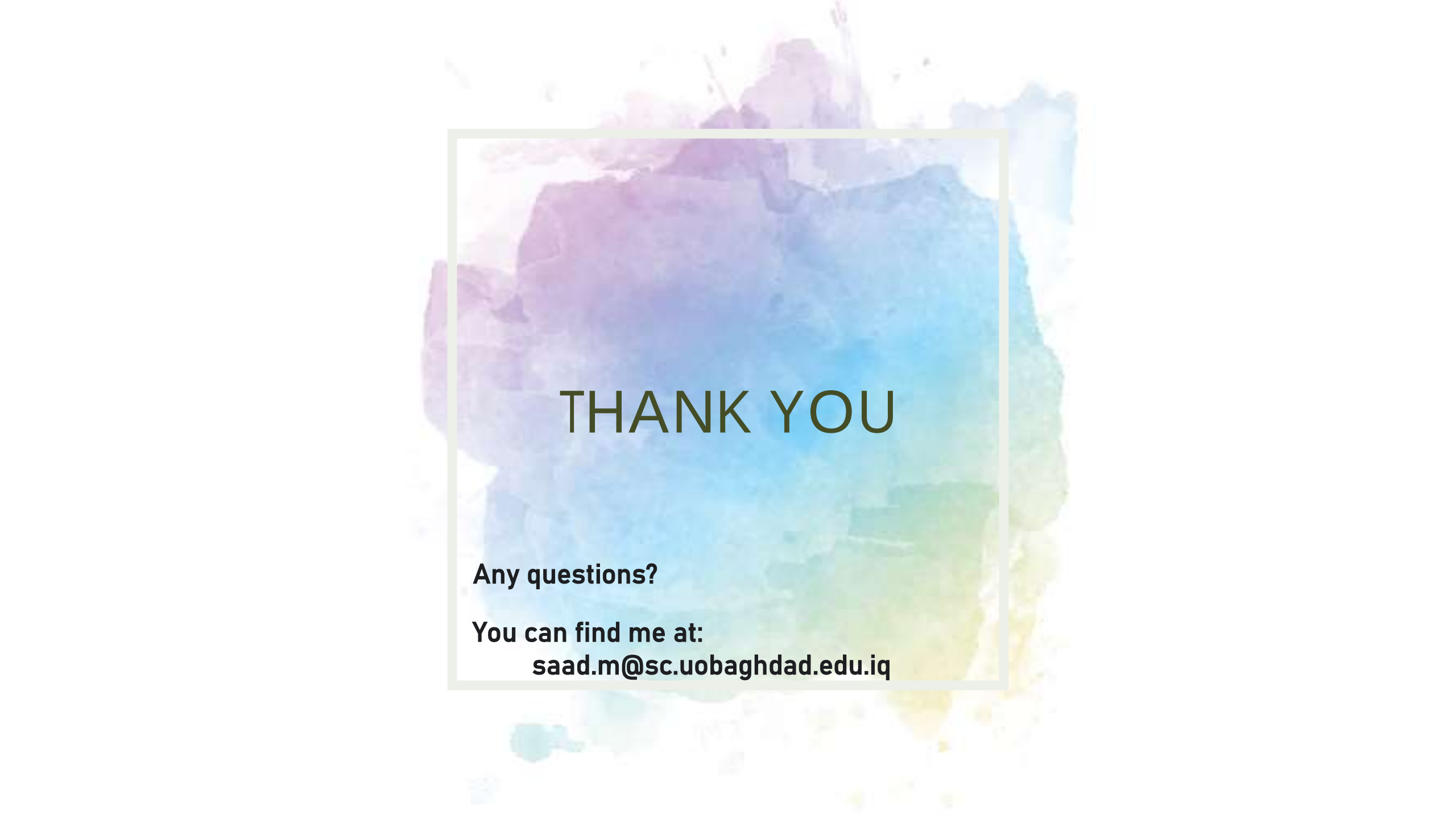
# Cryptanalyst

**Someone** who engages in cryptanalysis.



# The Block Diagram to Cipher System





# THANK YOU

**Any questions?**

**You can find me at:**

**[saad.m@sc.uobaghdad.edu.iq](mailto:saad.m@sc.uobaghdad.edu.iq)**

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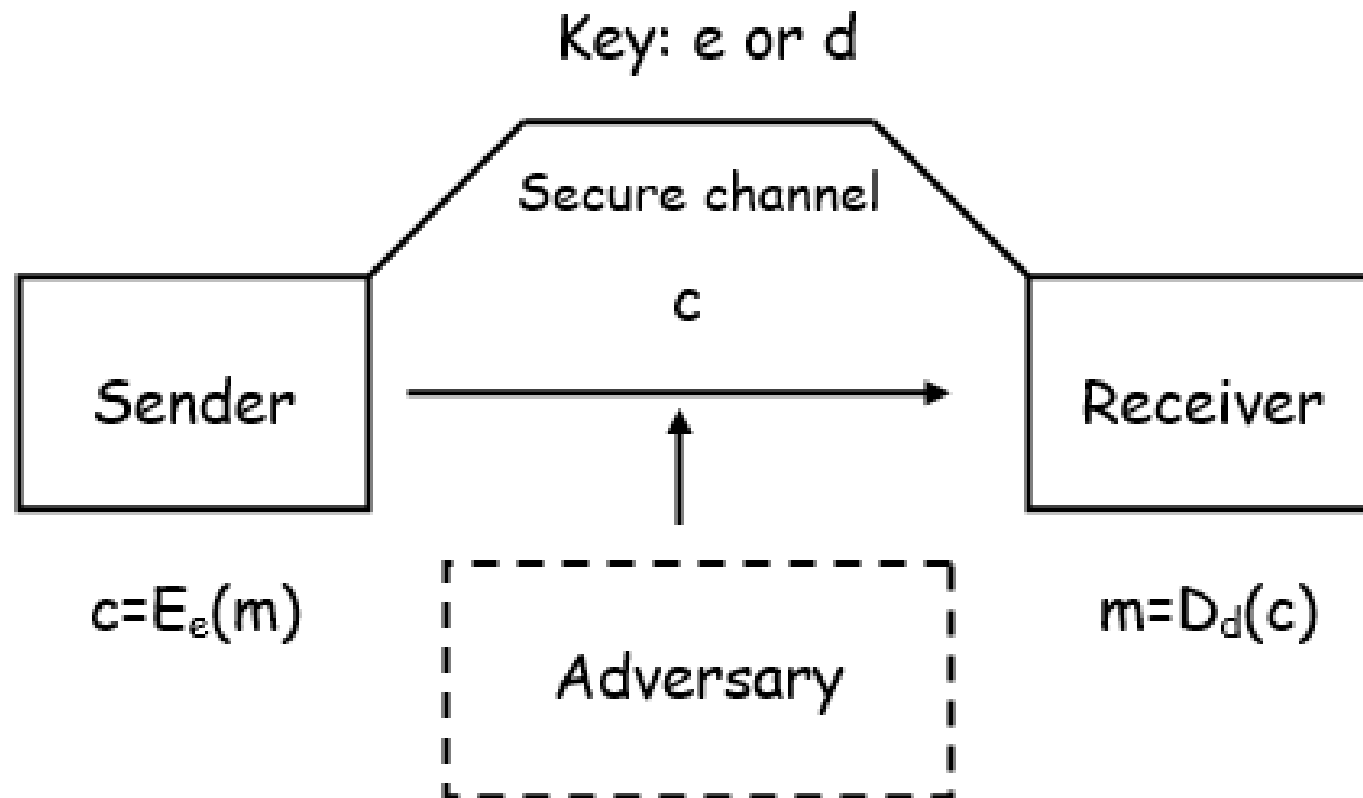


# **Secret Key Systems**



# Secret Key Systems

In such type of systems the encipher key and the decipher key must be known **only** by the sender and the receiver, so **they must exchange the key over a secure channel.**

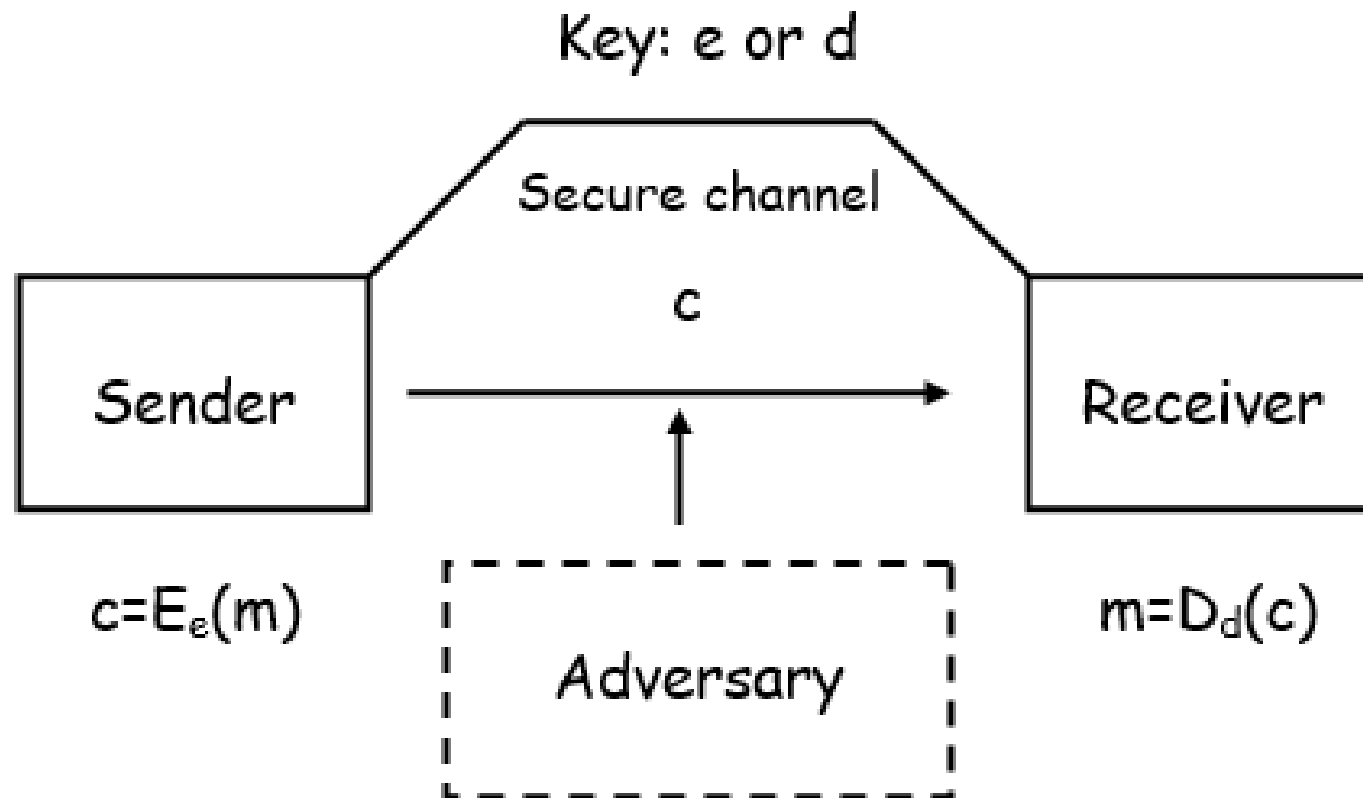




# Secret Key Systems

The problems with secret key cryptography are:

1. Requires establishment of a secure channel for key exchange.
2. Two parties cannot start communication if they never met.





# Transposition Cipher



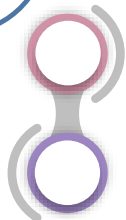
# Transposition Cipher

In transposition ciphers the letters of the original message (plaintext) are **arranged in a different order** to get the ciphertext.

Plaintext → Rearrange characters → Ciphertext

1

## Simple Transposition



Message reversal cipher

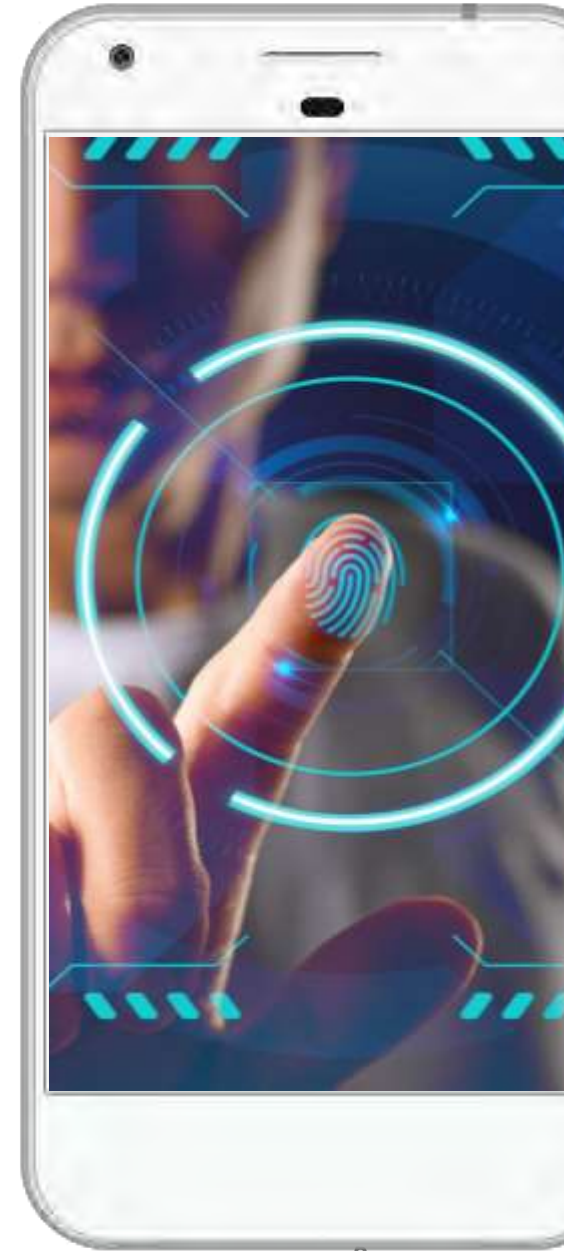
Columnar transposition

2

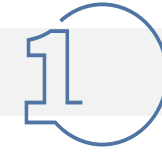
## Double Transposition



Double columnar transposition



# Message Reversal Cipher



Simple Transposition

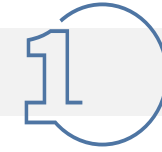
Plaintext = UNIVERSITY OF BAGHDAD



Ciphertext = DADHGAB FO YTISREVINU

Mathematically if  $L$  is the length of the message then  $c=E(k)=L+1-k$ , where  $k$  is the position of the letter in the plaintext.

# Columnar Transposition



## Simple Transposition

- We arrange the message as array of 2-dimension.
- The number of rows and columns depends on the length of the message.
- If the length of the message equal to **30** then the probability of the numbers of rows and columns are: **15X2, 2X15, 10X3, 3X10, 5X6, or 6X5.**
- Note that if the length of the message is 29, we must add a dummy letter in the end of the message.

# Columnar Transposition

## 1 Simple Transposition

Plaintext = UNIVERSITY OF BAGHDAD

the length of the message is 19, we will add a dummy letter X to the end of the message and the length will be 20.

Plaintext = UNIVERSITY OF BAGHDADX

We can say that  $20 = 4 \times 5$

# Columnar Transposition

1

Simple Transposition

Plaintext = UNIVERSITY OF BAGHDAD~~X~~

| 1 | 2 | 3 | 4 | 5 |
|---|---|---|---|---|
| U | N | I | V | E |
| R | S | I | T | Y |
| O | F | B | A | G |
| H | D | A | D | X |

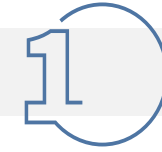
If the key is (4,3,2,1,5)



| 4 | 3 | 2 | 1 | 5 |
|---|---|---|---|---|
| V | I | N | U | E |
| T | I | S | R | Y |
| A | B | F | O | G |
| D | A | D | H | X |

Ciphertext = VTADIIBANSFDUROHEYGX

# Columnar Transposition



## Simple Transposition

To make the key easy to remember we take a keyword like **TODAY** and rearrange its letters alphabetically

|   |   |   |   |   |
|---|---|---|---|---|
| T | O | D | A | Y |
| 4 | 3 | 2 | 1 | 5 |

So (4,3,2,1,5) is the key that will use to rearrange the array columns.



Decipher the above ciphertext.



# Double Columnar Transposition



## Double Transposition

- Double Transposition consists of **two** applications of columnar transposition to a message.
- The two applications may use the same key for each of the two steps, or they may use different keys.

# Double Columnar Transposition

2

Double Transposition

|   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|
| 2 | 4 | 3 | 5 | 7 | 1 | 6 |
| D | I | G | I | T | A | L |
| U | N | I | V | E | R | S |
| I | T | Y | O | F | B | A |
| G | H | D | A | D | X | X |

Number the letters in the keyword in alphabetical order.

First pick a keyword, such as **DIGITAL**, and then write the message under it in

|   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|
| D | I | G | I | T | A | L |
| U | N | I | V | E | R | S |
| I | T | Y | O | F | B | A |
| G | H | D | A | D | X | X |

Read the cipher off by columns, starting with the lowest-numbered column

$CT_1 = \text{RBXUIGIYDNTHVOASAXEFD}$

|   |   |   |   |
|---|---|---|---|
| 2 | 1 | 3 | 4 |
| B | A | C | K |
| R | B | X | U |
| I | G | I | Y |
| D | N | T | H |
| V | O | A | S |
| A | X | F | E |
| D | X | X | X |

Select and number a second keyword (example **BACK**), and write  $CT_1$  under it in rows

Take it off by columns again

$CT_2 = \text{BGNOXXRIDVADXITAFXUYHSEX}$

# Double Columnar Transposition



## Double Transposition

To **decrypt** a double transposition:

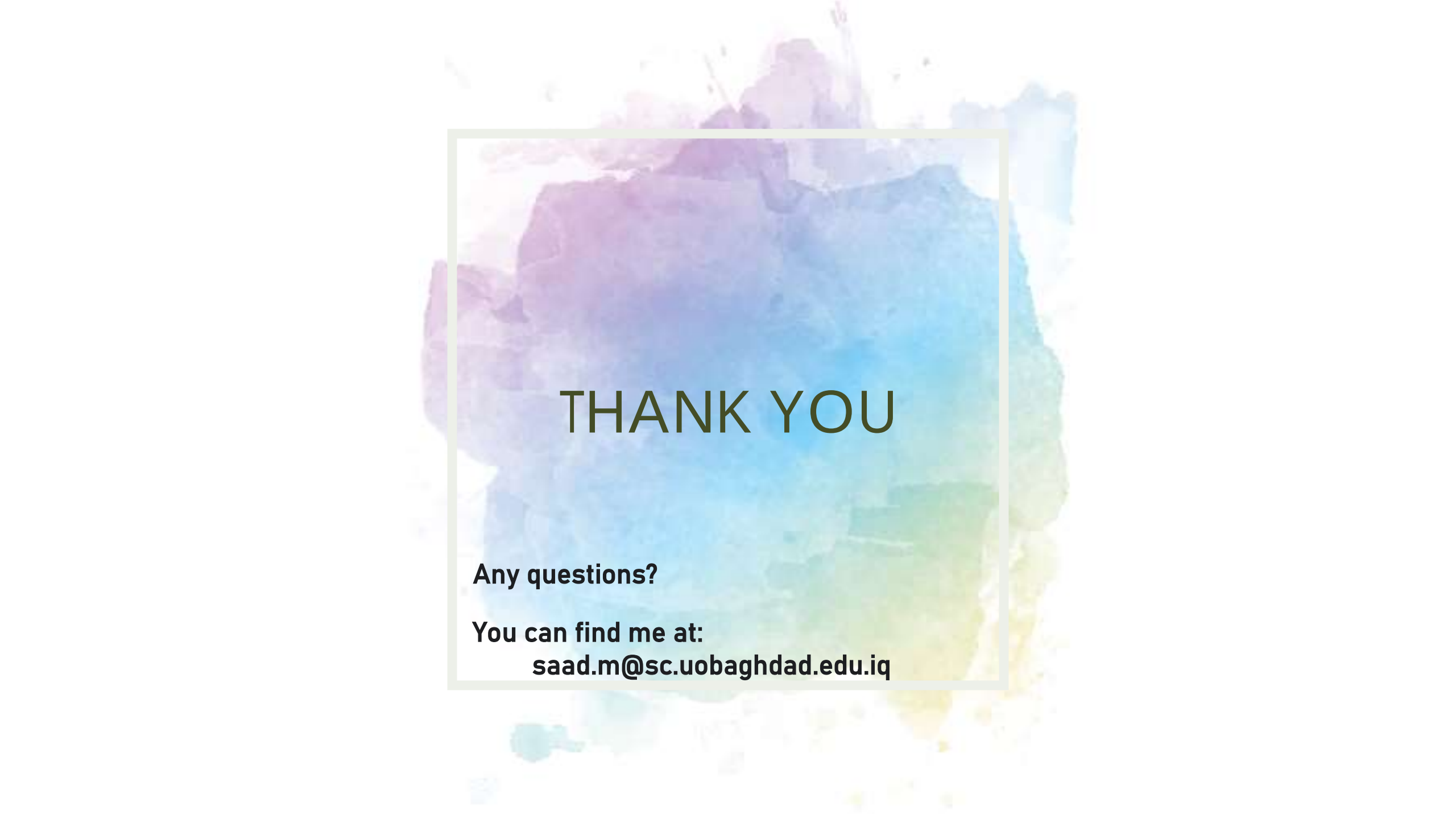
- Construct a block with the right number of rows under the keyword.
- Blocking off the short columns.
- Write the cipher in by columns, and read it out by rows.



Decipher the above ciphertext.



Try to solve the above example (encipher and decipher) without adding the X's.

A large, abstract watercolor splash in shades of purple, blue, and green serves as the background for the slide. A thin, light green rectangular border frames the central text area.

# THANK YOU

**Any questions?**

**You can find me at:**

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# **Substitution Cipher**



# Substitution Cipher

A system of encryption in which **each letter of a message is replaced with another character**, but retains its position within the message.



## Monoalphabetic

A substitution cipher system is the system that uses **one alphabet** throughout encryption.

### A. Simple substitution cipher

Simple substitution ciphers replaced each character of plaintext with the corresponding character of the ciphertext.



## 1.

# Direct Standard

- The Caesar cipher is the one most famous and simplest of all ciphers.
- In the Caesar cipher, each letter is **replaced with the third letter following it** in the alphabet.

Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

Ciphertext alpha.:

|   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |   |   |   |
|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|---|---|
| D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  | A | B | C |
| 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 0 | 1 | 2 |

# 1. Direct Standard

Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

Ciphertext alpha.:

|   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |   |   |   |
|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|---|---|
| D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  | A | B | C |
| 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 0 | 1 | 2 |

As an example, if the message is: UNIVERSITY OF BAGHDAD, then

|   |   |   |   |   |   |   |   |   |   |  |   |   |  |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|--|---|---|--|---|---|---|---|---|---|---|
| U | N | I | V | E | R | S | I | T | Y |  | O | F |  | B | A | G | H | D | A | D |
| X | Q | L | Y | H | U | V | L | W | B |  | R | I |  | E | D | J | K | G | D | G |

As we see, in Caesar cipher the key is **k=3**

We can choose a different value to the key in the range **between 0 and 25**.

$$c = E_k(m) = (m + k) \bmod 26$$

## 1.

## Direct Standard

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

**Encipher:**  $c = E_k(m) = (m + k) \bmod 26$

**Decipher:**  $m = D_k(c) = (c - k) \bmod 26$

For example in the above example  $E_3(A) = E_3(0) = (0 + 3) \bmod 26 = 3 = D$  and  $E_3(Y) = E_3(24) = (24 + 3) \bmod 26 = 1 = B$  and so on.

If the adversary received the ciphertext and he know that the sender used the shift method, the only thing he need to do, is to try all the possibilities that equal to 25 trials.



Decipher the above ciphertext.



What is the cardinality of the key space of the direct standard method?

## 2.

# Standard Reverse

- This method is similar to the Direct standard, except that the ciphertext alphabet are written in **reversed order from Z to A**.

$$\text{Encipher: } c = E_k(m) = (25 - m + k) \bmod 26$$

For example if  $k=0$  then,

**Plaintext alpha.:**

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

**Ciphertext alpha.:**

|    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |   |   |   |   |   |   |   |   |   |   |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|---|---|---|---|---|---|---|---|---|
| 25 | 24 | 23 | 22 | 21 | 20 | 19 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
| Z  | Y  | X  | W  | V  | U  | T  | S  | R  | Q  | P  | O  | N  | M  | L  | K  | J | I | H | G | F | E | D | C | B | A |

## 2.

## Standard Reverse

Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

Ciphertext alpha.:

|    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |   |   |   |   |   |   |   |   |   |   |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|---|---|---|---|---|---|---|---|---|
| 25 | 24 | 23 | 22 | 21 | 20 | 19 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
| Z  | Y  | X  | W  | V  | U  | T  | S  | R  | Q  | P  | O  | N  | M  | L  | K  | J | I | H | G | F | E | D | C | B | A |

As an example, if the message is: UNIVERSITY OF BAGHDAD, then

|   |   |   |   |   |   |   |   |   |   |  |   |   |  |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|--|---|---|--|---|---|---|---|---|---|---|
| U | N | I | V | E | R | S | I | T | Y |  | O | F |  | B | A | G | H | D | A | D |
| F | M | R | E | V | I | H | R | G | B |  | L | U |  | Y | Z | T | S | W | Z | W |



Decipher the above ciphertext.



What is the cardinality of the key space of the standard reverse method?

## 3.

# Multiplicative Cipher

- Ciphers based on **multiply** each character by a key  $k$ ; that  
**Encipher:  $c = E_k(m) = (m * k) \bmod 26$**
- Where  $k$  and 26 are relatively prime ( **$\text{GCD}(k, 26) = 1$** ), so that the letters of the alphabet produce a complete set of residues, so that in this case the key must be an **odd number and not equal to 13**.

For example if  $k=9$  then,

**Plaintext alpha.:**

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

**Ciphertext alpha.:**

|   |   |    |   |    |    |   |    |    |   |    |    |   |    |    |   |    |    |   |    |    |   |    |    |   |    |
|---|---|----|---|----|----|---|----|----|---|----|----|---|----|----|---|----|----|---|----|----|---|----|----|---|----|
| 0 | 9 | 18 | 1 | 10 | 19 | 2 | 11 | 20 | 3 | 12 | 21 | 4 | 13 | 22 | 5 | 14 | 23 | 6 | 15 | 24 | 7 | 16 | 25 | 8 | 17 |
| A | J | S  | B | K  | T  | C | L  | U  | D | M  | V  | E | N  | W  | F | O  | X  | G | P  | Y  | H | Q  | Z  | I | R  |

## 3.

# Multiplicative Cipher

**Plaintext alpha.:**

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

**Ciphertext alpha.:**

|   |   |    |   |    |    |   |    |    |   |    |    |   |    |    |   |    |    |   |    |    |   |    |    |   |    |
|---|---|----|---|----|----|---|----|----|---|----|----|---|----|----|---|----|----|---|----|----|---|----|----|---|----|
| 0 | 9 | 18 | 1 | 10 | 19 | 2 | 11 | 20 | 3 | 12 | 21 | 4 | 13 | 22 | 5 | 14 | 23 | 6 | 15 | 24 | 7 | 16 | 25 | 8 | 17 |
| A | J | S  | B | K  | T  | C | L  | U  | D | M  | V  | E | N  | W  | F | O  | X  | G | P  | Y  | H | Q  | Z  | I | R  |

As an example, if the message is: UNIVERSITY OF BAGHDAD, then

|   |   |   |   |   |   |   |   |   |   |  |   |   |  |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|--|---|---|--|---|---|---|---|---|---|---|
| U | N | I | V | E | R | S | I | T | Y |  | O | F |  | B | A | G | H | D | A | D |
| Y | N | U | H | K | X | G | U | P | I |  | W | T |  | J | A | C | L | B | A | B |



Decipher the above ciphertext.



What is the cardinality of the key space of the multiplicative cipher method?

## 3.

# Multiplicative Cipher

Encipher:  $c = E_k(m) = (m * k) \bmod 26$

Decipher:  $m = D_k(c) = (c * k^{-1}) \bmod 26$

[Proof:  $c * k^{-1} = m * k * k^{-1} = m$ ]

$$9^{-1} \bmod 26 = 3$$

$$[9 * 3 = 27 \bmod 26 = 1]$$

$$7^{-1} \bmod 26 = 15$$

$$[7 * 15 = 105 \bmod 26 = 1]$$

.

.

.

Note #1

Decryption

## 3.

# Multiplicative Cipher

Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

$$k=2$$

Note #2

$$(\text{GCD}(k, 26)=1)$$

Ciphertext alpha.:

|   |   |   |   |   |    |    |    |    |    |    |    |    |   |   |   |   |   |    |    |    |    |    |    |    |    |
|---|---|---|---|---|----|----|----|----|----|----|----|----|---|---|---|---|---|----|----|----|----|----|----|----|----|
| 0 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 | 20 | 22 | 24 | 0 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 | 20 | 22 | 24 |
| A | C | E | G | I | K  | M  | O  | Q  | S  | U  | W  | Y  | A | C | E | G | I | K  | M  | O  | Q  | S  | U  | W  | Y  |

3.

# Multiplicative Cipher

Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

$$k=4$$

Note #2

$$(\text{GCD}(k, 26)=1)$$

Ciphertext alpha.:

|   |   |   |    |    |    |    |   |   |    |    |    |    |   |   |   |    |    |    |    |   |   |    |    |    |    |
|---|---|---|----|----|----|----|---|---|----|----|----|----|---|---|---|----|----|----|----|---|---|----|----|----|----|
| 0 | 4 | 8 | 12 | 16 | 20 | 24 | 2 | 6 | 10 | 14 | 18 | 22 | 0 | 4 | 8 | 12 | 16 | 20 | 24 | 2 | 6 | 10 | 14 | 18 | 22 |
| A | E | I | M  | Q  | U  | Y  | C | G | K  | O  | S  | W  | A | E | I | M  | Q  | U  | Y  | C | G | K  | O  | S  | W  |

### 3. Multiplicative Cipher

# Plaintext alpha.:

| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

## Note #2

**k=13**

$$(\text{GCD}(k, 26) = 1)$$

## Ciphertext alpha.:

[illegible]

## 4.

## Affine Cipher

- Addition (shifting) and multiplication can be **combined** to give an Affine transformation

$$\text{Encipher: } c = E_{k_1, k_2}(m) = (m * k_1 + k_2) \bmod 26$$

- The conditions on  $k_1$  are the same conditions on the key of the multiplicative cipher, and the conditions on  $k_2$  are the same conditions on the key of the additive cipher.

Now, if  $k_1 = 7$  and  $k_2 = 4$  then,

**Plaintext alpha.:**

| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

**Ciphertext alpha.:**

|   |    |    |    |   |    |    |   |   |    |    |   |    |    |    |   |    |    |   |   |    |    |   |   |    |    |
|---|----|----|----|---|----|----|---|---|----|----|---|----|----|----|---|----|----|---|---|----|----|---|---|----|----|
| 4 | 11 | 18 | 25 | 6 | 13 | 20 | 1 | 8 | 15 | 22 | 3 | 10 | 17 | 24 | 5 | 12 | 19 | 0 | 7 | 14 | 21 | 2 | 9 | 16 | 23 |
| E | L  | S  | Z  | G | N  | U  | B | I | P  | W  | D | K  | R  | Y  | F | M  | T  | A | H | O  | V  | C | J | Q  | X  |

## 4.

## Affine Cipher

Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

Ciphertext alpha.:

|   |    |    |    |   |    |    |   |   |    |    |   |    |    |    |   |    |    |   |   |    |    |   |   |    |    |
|---|----|----|----|---|----|----|---|---|----|----|---|----|----|----|---|----|----|---|---|----|----|---|---|----|----|
| 4 | 11 | 18 | 25 | 6 | 13 | 20 | 1 | 8 | 15 | 22 | 3 | 10 | 17 | 24 | 5 | 12 | 19 | 0 | 7 | 14 | 21 | 2 | 9 | 16 | 23 |
| E | L  | S  | Z  | G | N  | U  | B | I | P  | W  | D | K  | R  | Y  | F | M  | T  | A | H | O  | V  | C | J | Q  | X  |

As an example, if the message is: UNIVERSITY OF BAGHDAD, then

|   |   |   |   |   |   |   |   |   |   |  |   |   |  |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|--|---|---|--|---|---|---|---|---|---|---|
| U | N | I | V | E | R | S | I | T | Y |  | O | F |  | B | A | G | H | D | A | D |
| O | R | I | V | G | T | A | I | H | Q |  | Y | N |  | L | E | U | B | Z | E | Z |



Decipher the above ciphertext.



What is the cardinality of the key space of the Affine cipher method?

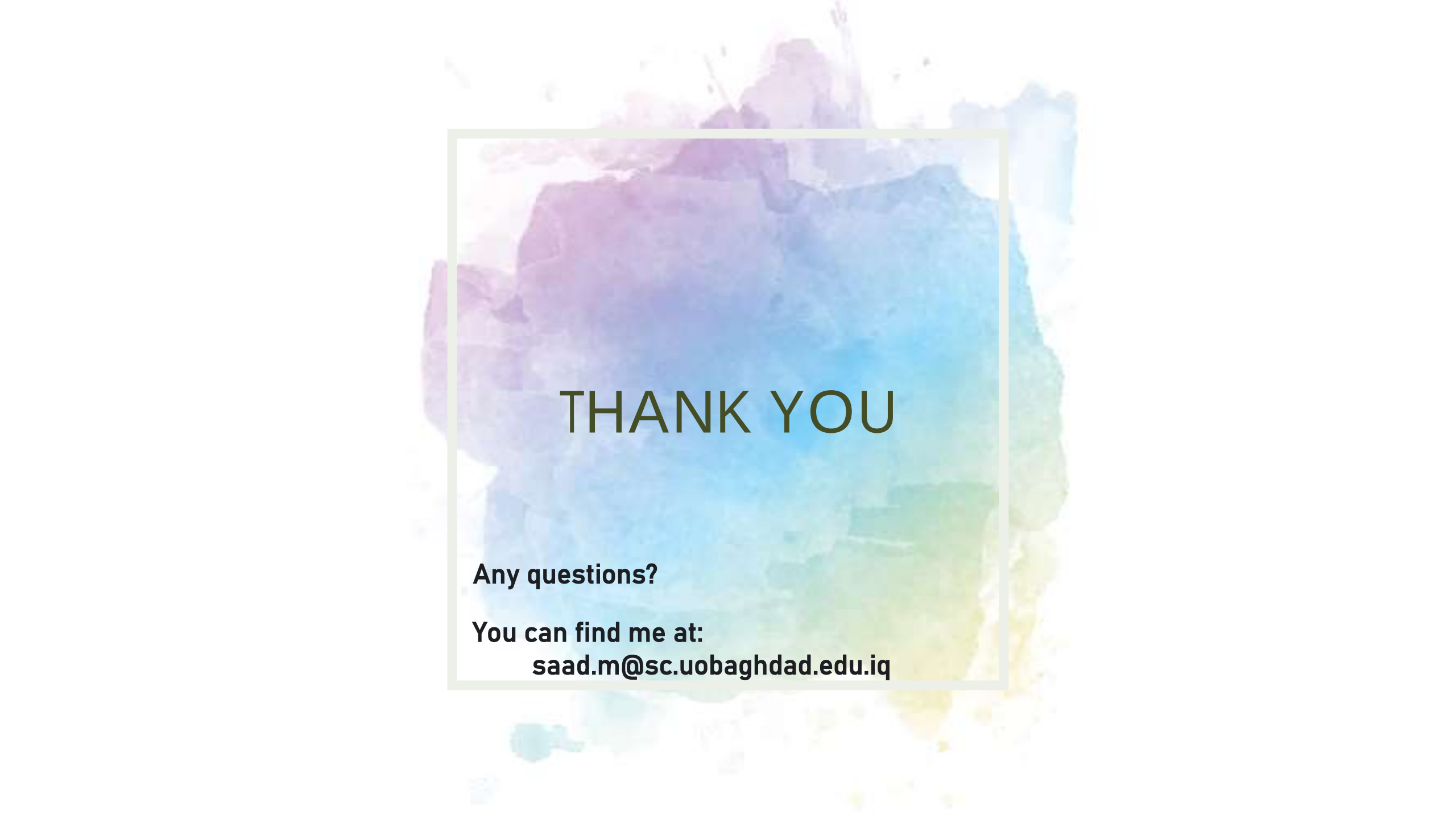
Encipher:  $c = E_{k_1, k_2}(m) = (m * k_1 + k_2) \bmod 26$

Decipher:  $m = D_{k_1, k_2}(c) = ((c - k_2) * (k_1)^{-1}) \bmod 26$

$$\begin{aligned} \text{[Proof: } (c - k_2) * (k_1)^{-1} &= ((m * k_1 + k_2) - k_2) * (k_1)^{-1} \\ &= ((m * k_1) + k_2 - k_2) * (k_1)^{-1} \\ &= (m * k_1) * (k_1)^{-1} \\ &= m * (k_1 * (k_1)^{-1}) = m \text{ ]} \end{aligned}$$

Note

Decryption

A large, abstract watercolor splash in shades of purple, blue, and green serves as the background for the slide. A thin, light green rectangular border frames the central text area.

# THANK YOU

**Any questions?**

**You can find me at:**

**[saad.m@sc.uobaghdad.edu.iq](mailto:saad.m@sc.uobaghdad.edu.iq)**

# Introduction to Cipher Systems

**Saad Al-Momen**

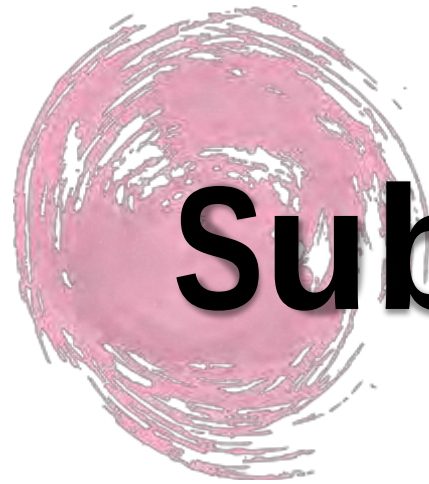


**CIPHER SYSTEMS**

**Fourth Class**

**Department of Mathematics**

**College of Science - University of Baghdad**



# **Substitution Cipher**



# Substitution Cipher

1

## Monoalphabetic

### A. Simple substitution cipher

1.

Direct Standard

2.

Standard Reverse

3.

Multiplicative Cipher

4.

Affine Cipher



## 5. Mixed Alphabet

If we permit the cipher alphabet to be any rearrangement of the plain alphabet, then we can generate an enormous number of distinct modes of encryption.

[illegible]

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[illegible]

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[illegible]

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[illegible]

## 5.

# Mixed Alphabet

If we permit the cipher alphabet to be any rearrangement of the plain alphabet, then we can generate an enormous number of distinct modes of encryption.

|    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |   |   |   |   |   |   |   |   |   |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|---|---|---|---|---|---|---|---|
| A  | B  | C  | D  | E  | F  | G  | H  | I  | J  | K  | L  | M  | N  | O  | P  | Q  | R | S | T | U | V | W | X | Y | Z |
| 26 | 25 | 24 | 23 | 22 | 21 | 20 | 19 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 |

## 5.

# Mixed Alphabet

If we permit the cipher alphabet to be any rearrangement of the plain alphabet, then we can generate an enormous number of distinct modes of encryption.

|    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |   |   |   |   |   |   |   |   |   |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|---|---|---|---|---|---|---|---|
| A  | B  | C  | D  | E  | F  | G  | H  | I  | J  | K  | L  | M  | N  | O  | P  | Q  | R | S | T | U | V | W | X | Y | Z |
| 26 | 25 | 24 | 23 | 22 | 21 | 20 | 19 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 |

There are **26!** such rearrangements, which is over **400,000,000,000,000,000,000,000,000**, i.e.  **$4 \times 10^{26}$**  which gives rise to an equivalent number of distinct cipher alphabets.

If an enemy agent could check **one** of these possible keys **every second**, it would take roughly one **billion times the lifetime of the universe** to check all of them and find the correct one.

## 5.

# Mixed Alphabet

For example, one of the  $26!$  is the following  
Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

Ciphertext alpha.:

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| X | J | Z | S | M | L | H | U | B | V | D | C | Y | Q | P | I | R | W | T | F | K | E | G | N | A | O |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

if the message is: UNIVERSITY OF BAGHDAD,

|   |   |   |   |   |   |   |   |   |   |  |   |   |  |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|--|---|---|--|---|---|---|---|---|---|---|
| U | N | I | V | E | R | S | I | T | Y |  | O | F |  | B | A | G | H | D | A | D |
| K | Q | B | E | M | W | T | B | F | A |  | P | L |  | J | X | H | U | S | X | S |

The **disadvantage** of this method is that the arrangement is **difficult to be remembered**.



Decipher the above ciphertext.

## 6.

## Keyword Mixed

In this method we need a keyword like **MATHEMATICS**, and a keyletter like **S**, then:

1. Remove the repeated letters from the keyword, and you will get **MATHEICS**.
2. Put the first letter of the modified keyword **under the keyletter** flowed by the remaining letters of the keyword.

Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

Ciphertext alpha.:

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |   |   |   |   |   |   |   |   |
|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|---|---|---|---|---|---|---|---|
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | M | A | T | H | E | I | C | S |
|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|---|---|---|---|---|---|---|---|

## 6.

## Keyword Mixed

In this method we need a keyword like **MATHEMATICS**, and a keyletter like **S**, then:

1. Remove the repeated letters from the keyword, and you will get **MATHEICS**.
2. Put the first letter of the modified keyword **under the keyletter** flowed by the remaining letters of the keyword.
3. Complete the ciphertext alphabet by the **remaining letters without repetitions**.

Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

Ciphertext alpha.:

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| B | D | F | G | J | K | L | N | O | P | Q | R | U | V | W | X | Y | Z | M | A | T | H | E | I | C | S |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

6.

## Keyword Mixed

Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

Ciphertext alpha.:

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| B | D | F | G | J | K | L | N | O | P | Q | R | U | V | W | X | Y | Z | M | A | T | H | E | I | C | S |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

if the message is: UNIVERSITY OF BAGHDAD,

|   |   |   |   |   |   |   |   |   |   |  |   |   |  |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|--|---|---|--|---|---|---|---|---|---|---|
| U | N | I | V | E | R | S | I | T | Y |  | O | F |  | B | A | G | H | D | A | D |
| T | V | O | H | J | Z | M | O | A | C |  | W | K |  | D | B | L | N | G | B | G |



Decipher the above ciphertext.

## 7.

# Transposed Keyword Mixed

---

In this method

1. We need a **keyword** like **MATHEMATICS**.
2. **Removing** the repeated letters.
3. **Put it in a matrix** with number of columns equal to the number of the letters in the modified keyword.

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| M | A | T | H | E | I | C | S |
|---|---|---|---|---|---|---|---|

## 7.

# Transposed Keyword Mixed

In this method

1. We need a **keyword** like **MATHEMATICS**.
2. **Removing** the repeated letters.
3. **Put it in a matrix** with number of columns equal to the number of the letters in the modified keyword.

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| M | A | T | H | E | I | C | S |
| B | D | F | G | J | K | L | N |
| O | P | Q | R | U | V | W | X |
| Y | Z |   |   |   |   |   |   |

4. Then we take the matrix letters **column by column** and we will get

Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

Ciphertext alpha.:

## 7. Transposed Keyword Mixed

In this method

1. We need a **keyword** like **MATHEMATICS**.
2. **Removing** the repeated letters.
3. **Put it in a matrix** with number of columns equal to the number of the letters in the modified keyword.

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| M | A | T | H | E | I | C | S |
| B | D | F | G | J | K | L | N |
| O | P | Q | R | U | V | W | X |
| Y | Z |   |   |   |   |   |   |

4. Then we take the matrix letters **column by column** and we will get

Plaintext alpha.:

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z

Ciphertext alpha.:

[illegible]

## 7. Transposed Keyword Mixed

In this method

1. We need a **keyword** like **MATHEMATICS**.
2. **Removing** the repeated letters.
3. **Put it in a matrix** with number of columns equal to the number of the letters in the modified keyword.

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| M | A | T | H | E | I | C | S |
| B | D | F | G | J | K | L | N |
| O | P | Q | R | U | V | W | X |
| Y | Z |   |   |   |   |   |   |

4. Then we take the matrix letters **column by column** and we will get

Plaintext alpha.:

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z

Ciphertext alpha.:

M B O Y A D P Z



## 7. Transposed Keyword Mixed

In this method

1. We need a **keyword** like **MATHEMATICS**.
2. **Removing** the repeated letters.
3. **Put it in a matrix** with number of columns equal to the number of the letters in the modified keyword.

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| M | A | T | H | E | I | C | S |
| B | D | F | G | J | K | L | N |
| O | P | Q | R | U | V | W | X |
| Y | Z |   |   |   |   |   |   |

4. Then we take the matrix letters **column by column** and we will get Plaintext alpha.:

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z

Ciphertext alpha.:

[illegible]

## 7. Transposed Keyword Mixed

In this method

1. We need a **keyword** like **MATHEMATICS**.
2. **Removing** the repeated letters.
3. **Put it in a matrix** with number of columns equal to the number of the letters in the modified keyword.

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| M | A | T | H | E | I | C | S |
| B | D | F | G | J | K | L | N |
| O | P | Q | R | U | V | W | X |
| Y | Z |   |   |   |   |   |   |

4. Then we take the matrix letters **column by column** and we will get Plaintext alpha.:

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z

Ciphertext alpha.:

[illegible]

## 7.

# Transposed Keyword Mixed

In this method

1. We need a **keyword** like **MATHEMATICS**.
2. **Removing** the repeated letters.
3. **Put it in a matrix** with number of columns equal to the number of the letters in the modified keyword.

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| M | A | T | H | E | I | C | S |
| B | D | F | G | J | K | L | N |
| O | P | Q | R | U | V | W | X |
| Y | Z |   |   |   |   |   |   |

4. Then we take the matrix letters **column by column** and we will get Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

Ciphertext alpha.:

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |  |  |  |  |  |  |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|--|--|--|--|--|--|
| M | B | O | Y | A | D | P | Z | T | F | Q | H | G | R | E | J | U | I | K | V |  |  |  |  |  |  |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|--|--|--|--|--|--|

## 7.

# Transposed Keyword Mixed

In this method

1. We need a **keyword** like **MATHEMATICS**.
2. **Removing** the repeated letters.
3. **Put it in a matrix** with number of columns equal to the number of the letters in the modified keyword.

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| M | A | T | H | E | I | C | S |
| B | D | F | G | J | K | L | N |
| O | P | Q | R | U | V | W | X |
| Y | Z |   |   |   |   |   |   |

4. Then we take the matrix letters **column by column** and we will get Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

Ciphertext alpha.:

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |  |  |  |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|--|--|--|
| M | B | O | Y | A | D | P | Z | T | F | Q | H | G | R | E | J | U | I | K | V | C | L | W |  |  |  |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|--|--|--|

## 7.

# Transposed Keyword Mixed

In this method

1. We need a **keyword** like **MATHEMATICS**.
2. **Removing** the repeated letters.
3. **Put it in a matrix** with number of columns equal to the number of the letters in the modified keyword.

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| M | A | T | H | E | I | C | S |
| B | D | F | G | J | K | L | N |
| O | P | Q | R | U | V | W | X |
| Y | Z |   |   |   |   |   |   |

4. Then we take the matrix letters **column by column** and we will get Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

Ciphertext alpha.:

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| M | B | O | Y | A | D | P | Z | T | F | Q | H | G | R | E | J | U | I | K | V | C | L | W | S | N | X |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

7.

# Transposed Keyword Mixed

Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

Ciphertext alpha.:

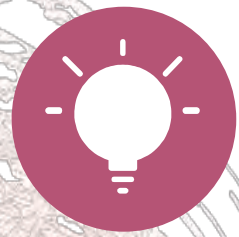
|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| M | B | O | Y | A | D | P | Z | T | F | Q | H | G | R | E | J | U | I | K | V | C | L | W | S | N | X |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

if the message is: UNIVERSITY OF BAGHDAD,

|   |   |   |   |   |   |   |   |   |   |  |   |   |  |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|--|---|---|--|---|---|---|---|---|---|---|
| U | N | I | V | E | R | S | I | T | Y |  | O | F |  | B | A | G | H | D | A | D |
| C | R | T | L | A | I | K | T | V | N |  | E | D |  | B | M | P | Z | Y | M | Y |



Decipher the above ciphertext.



# Substitution Cipher

1

## Monoalphabetic

### A. Simple Substitution Cipher

1. Direct Standard
2. Standard Reverse
3. Multiplicative Cipher
4. Affine Cipher
5. Mixed Alphabet
6. Keyword Mixed
7. Transposed Keyword Mixed

### B. Homophonic Substitution Cipher

1. Beale Cipher
2. Higher order homophonic





# Substitution Cipher

1

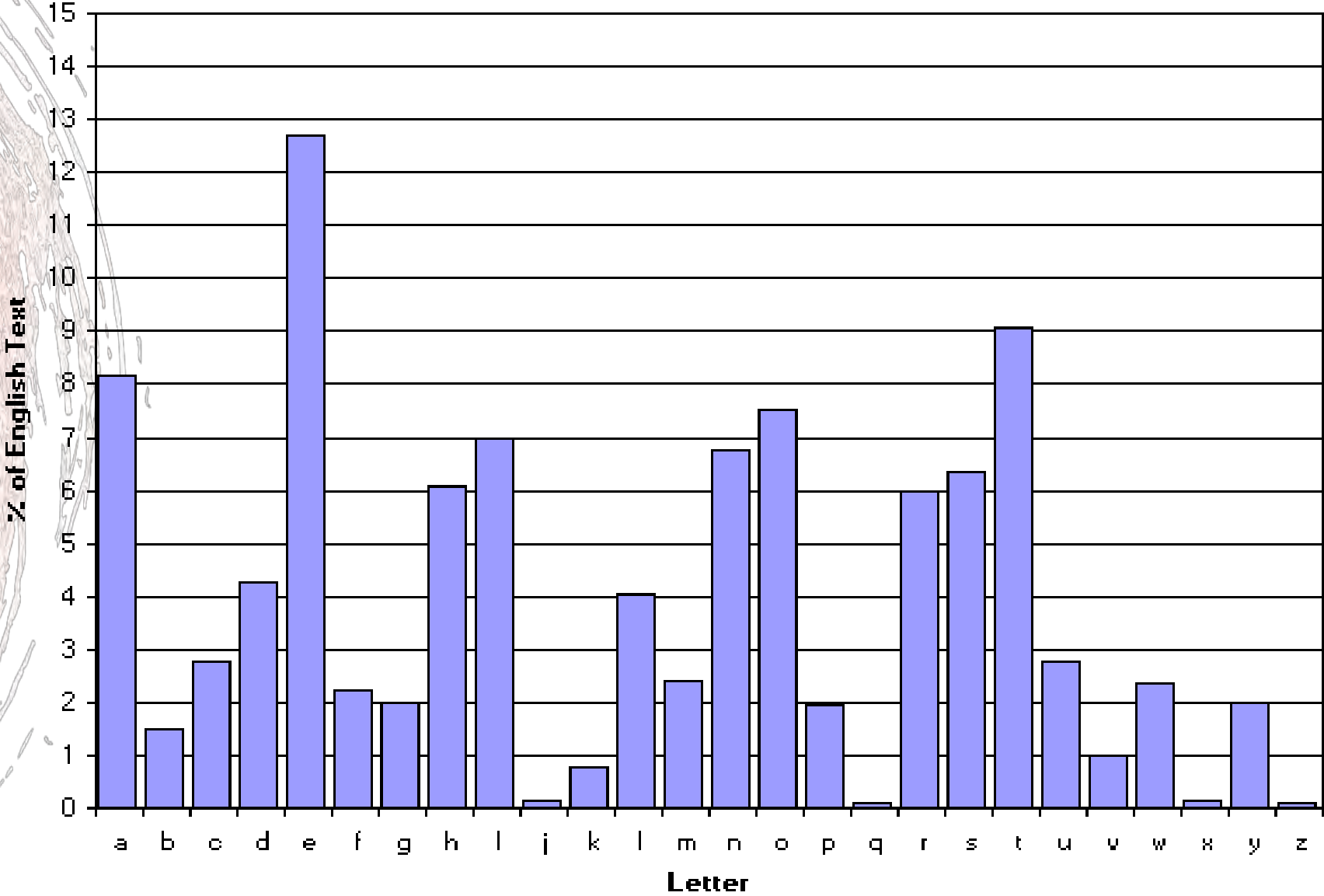
## Monoalphabetic

### B. Homophonic Substitution Cipher

- Homophonic substitution cipher are similar to simple substitution, except the mapping is **one-to many**.
- The Homophonic Substitution Cipher involves replacing each letter with a **variety of substitutes**.
- The number of potential substitutes being **proportional to the frequency** of the letter.



English Letter Frequency



| Letter | %      | Letter | %     |
|--------|--------|--------|-------|
| a      | 8.167  | n      | 6.749 |
| b      | 1.492  | o      | 7.507 |
| c      | 2.782  | p      | 1.929 |
| d      | 4.253  | q      | 0.095 |
| e      | 12.702 | r      | 5.987 |
| f      | 2.228  | s      | 6.327 |
| g      | 2.015  | t      | 9.056 |
| h      | 6.094  | u      | 2.758 |
| i      | 6.966  | v      | 0.978 |
| j      | 0.153  | w      | 2.360 |
| k      | 0.772  | x      | 0.150 |
| l      | 4.025  | y      | 1.974 |
| m      | 2.406  | z      | 0.074 |

The point of offering several substitution options for popular letters is to **balance out the frequencies** of symbols in the ciphertext.

Every symbol will constitute roughly **1%** of the ciphertext.

|   |    |    |    |    |    |    |    |    |    |    |    |    |
|---|----|----|----|----|----|----|----|----|----|----|----|----|
| A | 09 | 12 | 33 | 47 | 53 | 67 | 78 | 92 |    |    |    |    |
| B | 48 | 81 |    |    |    |    |    |    |    |    |    |    |
| C | 13 | 41 | 62 |    |    |    |    |    |    |    |    |    |
| D | 01 | 03 | 45 | 79 |    |    |    |    |    |    |    |    |
| E | 14 | 16 | 24 | 44 | 46 | 55 | 57 | 64 | 74 | 82 | 87 | 98 |
| F | 10 | 31 |    |    |    |    |    |    |    |    |    |    |
| G | 06 | 25 |    |    |    |    |    |    |    |    |    |    |
| H | 23 | 39 | 50 | 56 | 65 | 68 |    |    |    |    |    |    |
| I | 32 | 70 | 73 | 83 | 88 | 93 |    |    |    |    |    |    |
| J | 15 |    |    |    |    |    |    |    |    |    |    |    |
| K | 04 |    |    |    |    |    |    |    |    |    |    |    |
| L | 26 | 37 | 51 | 84 |    |    |    |    |    |    |    |    |
| M | 22 | 27 |    |    |    |    |    |    |    |    |    |    |
| N | 18 | 58 | 59 | 66 | 71 | 91 |    |    |    |    |    |    |
| O | 00 | 05 | 07 | 54 | 72 | 90 | 99 |    |    |    |    |    |
| P | 38 | 95 |    |    |    |    |    |    |    |    |    |    |
| Q | 94 |    |    |    |    |    |    |    |    |    |    |    |
| R | 29 | 35 | 40 | 52 | 77 | 80 |    |    |    |    |    |    |
| S | 11 | 19 | 36 | 76 | 86 | 96 |    |    |    |    |    |    |
| T | 17 | 20 | 30 | 43 | 49 | 69 | 75 | 85 | 97 |    |    |    |
| U | 08 | 61 | 63 |    |    |    |    |    |    |    |    |    |
| V | 34 |    |    |    |    |    |    |    |    |    |    |    |
| W | 60 | 89 |    |    |    |    |    |    |    |    |    |    |
| X | 28 |    |    |    |    |    |    |    |    |    |    |    |
| Y | 21 | 52 |    |    |    |    |    |    |    |    |    |    |
| Z | 02 |    |    |    |    |    |    |    |    |    |    |    |

| Letter | %      | Letter | %     |
|--------|--------|--------|-------|
| a      | 8.167  | n      | 6.749 |
| b      | 1.492  | o      | 7.507 |
| c      | 2.782  | p      | 1.929 |
| d      | 4.253  | q      | 0.095 |
| e      | 12.702 | r      | 5.987 |
| f      | 2.228  | s      | 6.327 |
| g      | 2.015  | t      | 9.056 |
| h      | 6.094  | u      | 2.758 |
| i      | 6.966  | v      | 0.978 |
| j      | 0.153  | w      | 2.360 |
| k      | 0.772  | x      | 0.150 |
| l      | 4.025  | y      | 1.974 |
| m      | 2.406  | z      | 0.074 |

|   |    |    |    |    |    |    |    |    |    |    |    |    |
|---|----|----|----|----|----|----|----|----|----|----|----|----|
| A | 09 | 12 | 33 | 47 | 53 | 67 | 78 | 92 |    |    |    |    |
| B | 48 | 81 |    |    |    |    |    |    |    |    |    |    |
| C | 13 | 41 | 62 |    |    |    |    |    |    |    |    |    |
| D | 01 | 03 | 45 | 79 |    |    |    |    |    |    |    |    |
| E | 14 | 16 | 24 | 44 | 46 | 55 | 57 | 64 | 74 | 82 | 87 | 98 |
| F | 10 | 31 |    |    |    |    |    |    |    |    |    |    |
| G | 06 | 25 |    |    |    |    |    |    |    |    |    |    |
| H | 23 | 39 | 50 | 56 | 65 | 68 |    |    |    |    |    |    |
| I | 32 | 70 | 73 | 83 | 88 | 93 |    |    |    |    |    |    |
| J | 15 |    |    |    |    |    |    |    |    |    |    |    |
| K | 04 |    |    |    |    |    |    |    |    |    |    |    |
| L | 26 | 37 | 51 | 84 |    |    |    |    |    |    |    |    |
| M | 22 | 27 |    |    |    |    |    |    |    |    |    |    |
| N | 18 | 58 | 59 | 66 | 71 | 91 |    |    |    |    |    |    |
| O | 00 | 05 | 07 | 54 | 72 | 90 | 99 |    |    |    |    |    |
| P | 38 | 95 |    |    |    |    |    |    |    |    |    |    |
| Q | 94 |    |    |    |    |    |    |    |    |    |    |    |
| R | 29 | 35 | 40 | 52 | 77 | 80 |    |    |    |    |    |    |
| S | 11 | 19 | 36 | 76 | 86 | 96 |    |    |    |    |    |    |
| T | 17 | 20 | 30 | 43 | 49 | 69 | 75 | 85 | 97 |    |    |    |
| U | 08 | 61 | 63 |    |    |    |    |    |    |    |    |    |
| V | 34 |    |    |    |    |    |    |    |    |    |    |    |
| W | 60 | 89 |    |    |    |    |    |    |    |    |    |    |
| X | 28 |    |    |    |    |    |    |    |    |    |    |    |
| Y | 21 | 52 |    |    |    |    |    |    |    |    |    |    |
| Z | 02 |    |    |    |    |    |    |    |    |    |    |    |

U N I V E R S I T Y O F B A G H D A D 7  
08 18 32 34 14 29 11 70 17 21 00 10 48 09 06 23 01 12 03 5

| Letter | %      | Letter | %     |
|--------|--------|--------|-------|
| a      | 8.167  | n      | 6.749 |
| b      | 1.492  | o      | 7.507 |
| c      | 2.782  | p      | 1.929 |
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| e      | 12.702 | r      | 5.987 |
| g      | 2.015  | t      | 7.056 |
| h      | 6.094  | u      | 2.758 |
| i      | 6.966  | v      | 0.978 |
| j      | 0.153  | w      | 2.360 |
| k      | 0.772  | x      | 0.150 |
| l      | 4.025  | y      | 1.974 |
| m      | 2.406  | z      | 0.074 |



Decipher the above ciphertext.

1.

# Beale Cipher

|                                                                                                           |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|-----------------------------------------------------------------------------------------------------------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 1                                                                                                         | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 | 16 |    |    |    |
| "Christmas, the annual festival of Christ's birth. Christmas Day falls on December 25 and celebrates the  |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
| 17                                                                                                        | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 |
| birth of Jesus Christ in Bethlehem as recounted in the Gospels of Matthew and Luke. It is, after Easter,  |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
| 36                                                                                                        | 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 |
| the most important feast in the Church's year. Since the Gospels make no mention of dates, it is not      |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
| 55                                                                                                        | 56 | 57 | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 71 | 72 | 73 |
| certain that Christ was born on this day. In fact, Christmas Day did not officially come into being until |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
| 74                                                                                                        | 75 | 76 | 77 | 78 | 79 | 80 | 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 | 91 | 91 |
| 354 when Pope Gregory proclaimed December 25 as the date of the Nativity. In doing so, he was             |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
| 91                                                                                                        | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 |    |    |    |    |    |    |    |    |    |    |
| following the early Church's policy of absorbing rather than repressing existing pagan rites which, since |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
| early times, had celebrated the winter solstice and the coming of spring."                                |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |

|    |    |    |    |    |    |    |
|----|----|----|----|----|----|----|
| B  | A  | G  | H  | D  | A  | D  |
| 07 | 03 | 27 | 90 | 09 | 14 | 51 |

## 2. Higher Order Homophonic

Recall that, given enough ciphertext, most ciphers are **theoretically breakable** because there is a **single key that deciphers the ciphertext into meaningful plaintext**; all other keys produce meaningless sequence of letters.

It is possible to construct higher-order homophonic ciphers where each ciphertext **deciphers into more than one meaningful plaintext** using different keys.

To construct a **second-order homophonic** cipher (meaning that for each plaintext there are **two possible meaningful** plaintexts).

## 2. Higher Order Homophonic

For example; Let  $n=5$ . The following is 5X5 matrix for the plaintext alphabet {E, I, L, M, S}.

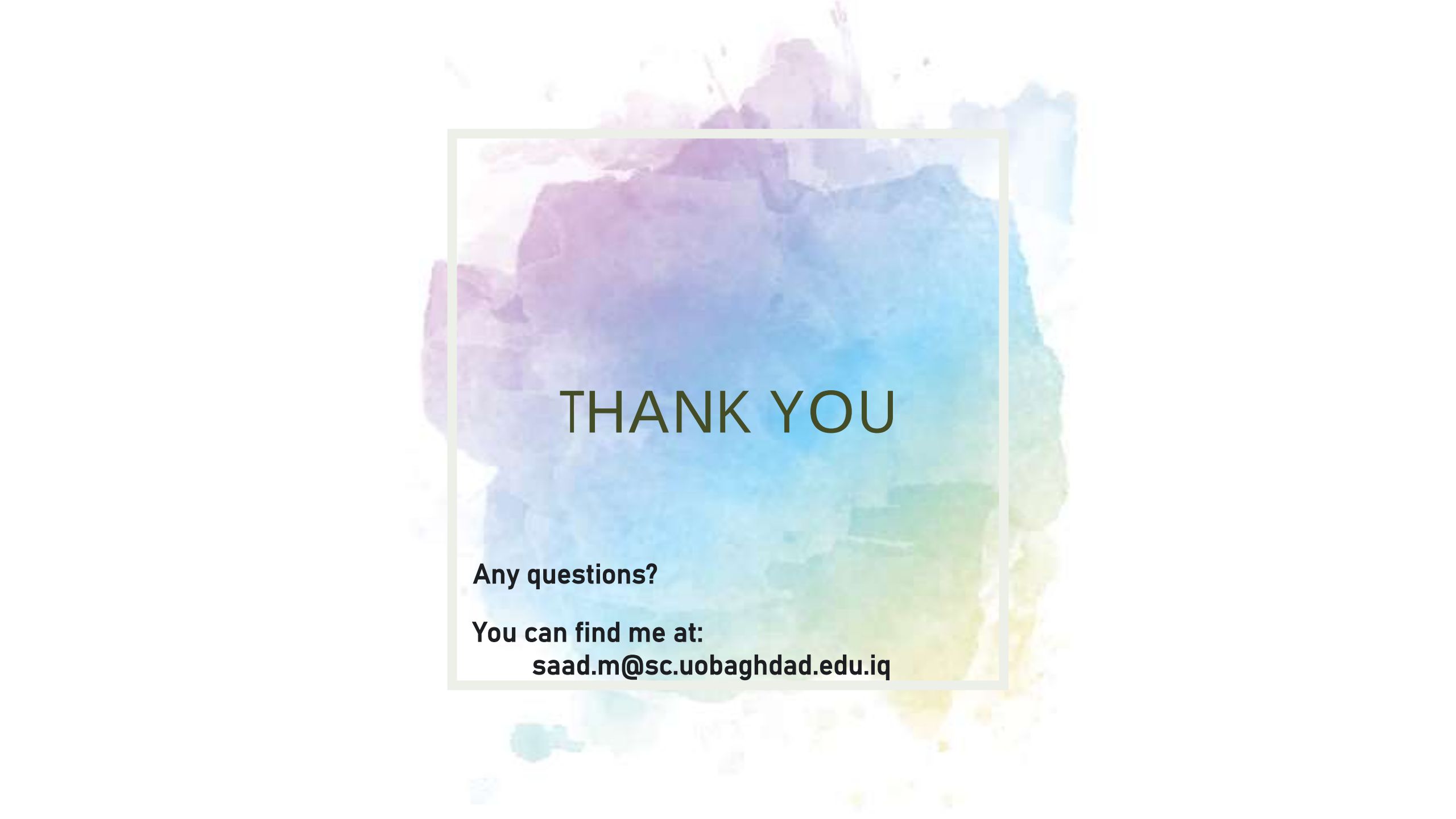
|   | E  | I  | L  | M  | S  |
|---|----|----|----|----|----|
| E | 10 | 22 | 18 | 02 | 11 |
| I | 12 | 01 | 25 | 05 | 20 |
| L | 19 | 06 | 23 | 13 | 07 |
| M | 03 | 16 | 08 | 24 | 15 |
| S | 17 | 09 | 21 | 14 | 04 |

And the message that we want to encipher is SMILE which is replace by LIMES, then

|   |   |    |    |    |    |    |
|---|---|----|----|----|----|----|
| M | = | S  | M  | I  | L  | E  |
| X | = | L  | I  | M  | E  | S  |
| C | = | 21 | 16 | 05 | 19 | 11 |



Decipher the above ciphertext.

A large, abstract watercolor splash in shades of purple, blue, and green serves as the background for the slide. A thin, light green rectangular border frames the central text area.

# THANK YOU

**Any questions?**

**You can find me at:**

**[saad.m@sc.uobaghdad.edu.iq](mailto:saad.m@sc.uobaghdad.edu.iq)**



# Introduction to Cipher Systems

**Saad Al-Momen**



**CIPHER SYSTEMS**

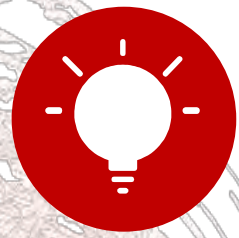
**Fourth Class**

**Department of Mathematics**

**College of Science - University of Baghdad**



# Substitution Cipher



# Substitution Cipher

A system of encryption in which **each letter of a message is replaced with another character**, but retains its position within the message.

2

## Polyalphabetic

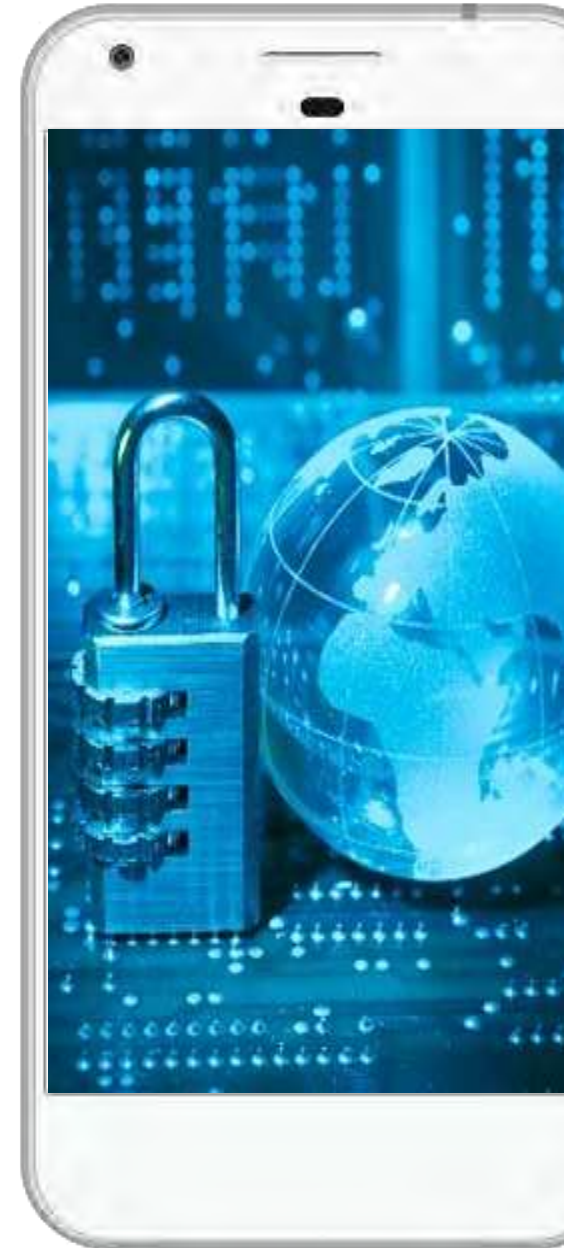
Polyalphabetic substitution cipher is a substitution cipher in which **the cipher alphabet changes during the encryption**. The change is defined by a key

1.

Vigenere Cipher

2.

Beaufort Cipher



1.

# Vignere Cipher

The Vignere Cipher, proposed by Blaise de Vignere from the court of Henry III of France in the sixteenth century, is a polyalphabetic substitution based on the following tableau:

|   | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| B | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| I | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I |
| K | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J |
| L | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
| M | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L |
| N | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| O | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| P | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| Q | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| R | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R |
| T | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| U | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T |
| V | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

1.

# Vignere Cipher

The **first** row is a shift of 0

The **second** is a shift of 1

•

•

•

The **last** is a shift of 25.

Mathematically,

$$E_{k_i}(m) = (m + k_i) \bmod 26$$

|   | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| B | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| I | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I |
| K | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J |
| L | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
| M | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L |
| N | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| O | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| P | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| Q | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| R | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R |
| T | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| U | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T |
| V | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

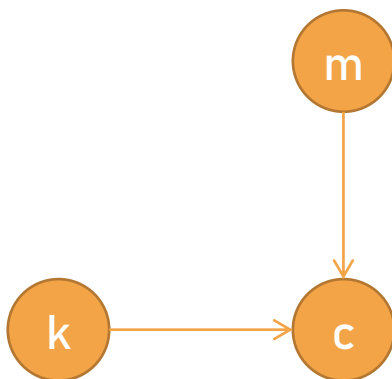
1.

# Vignere Cipher

TO BE OR NOT TO BE THAT IS THE QUESTION

Keyword: RELATIONS

Keyword: RELATIONSRELATIONSRELATIONSREL  
 Plaintext: TOBEORNOTTOBETHATISTHEQUESTION  
 Ciphertext:



Encryption

|   | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| B | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| I | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I |
| K | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J |
| L | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
| M | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L |
| N | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| O | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| P | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| Q | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| R | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R |
| T | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| U | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T |
| V | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

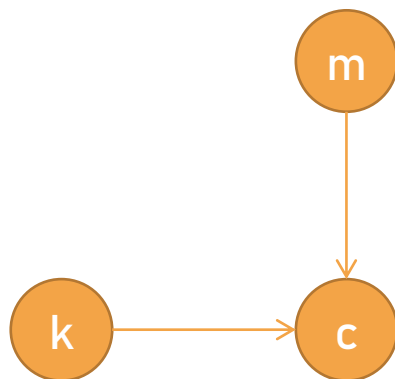
1.

# Vigenere Cipher

TO BE OR NOT TO BE THAT IS THE QUESTION

Keyword: RELATIONS

Keyword: RELATIONSRELATIONSRELATIONSREL  
 Plaintext: TOBEORNOTTOBETHATISTHEQUESTION  
 Ciphertext: K



Encryption

|   | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| B | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| I | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I |
| K | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J |
| L | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
| M | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L |
| N | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| O | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| P | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| Q | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| R | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R |
| T | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| U | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T |
| V | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

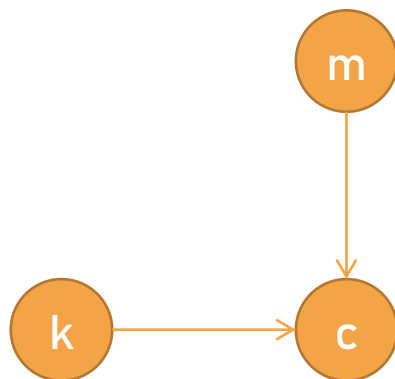
1.

# Vignere Cipher

TO BE OR NOT TO BE THAT IS THE QUESTION

Keyword: RELATIONS

Keyword: RELATIONSRELATIONSRELATIONSREL  
 Plaintext: TOBEORNOTTOBETHATISTHEQUESTION  
 Ciphertext: K S



Encryption

|   | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| B | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| I | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I |
| K | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J |
| L | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
| M | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L |
| N | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| O | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| P | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| Q | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| R | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R |
| T | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| U | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T |
| V | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

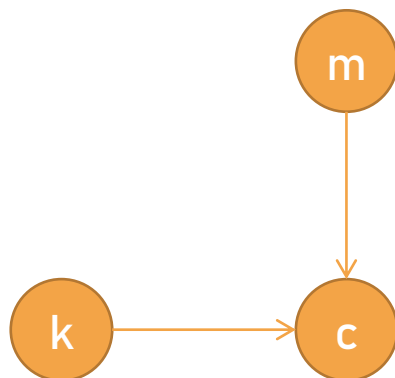
1.

# Vignere Cipher

To be or not to be that is the question

**Keyword:** Relations

**Keyword:** RELATIONSRELATIONSRELATIONSREL  
**Plaintext:** TOBEORNOTTOBETHATISTHEQUESTION  
**Ciphertext:** K SM



Encryption

|   | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| B | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| I | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I |
| K | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J |
| L | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
| M | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L |
| N | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| O | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| P | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| Q | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| R | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R |
| T | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| U | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T |
| V | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

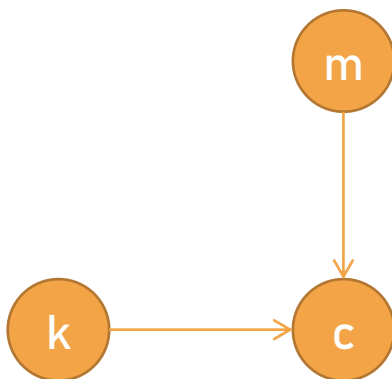
1.

# Vignere Cipher

TO BE OR NOT TO BE THAT IS THE QUESTION

Keyword: RELATIONS

Keyword: RELATIONSRELATIONSRELATIONSREL  
 Plaintext: TOBEORNOTTOBETHATISTHEQUESTION  
 Ciphertext: K S M E



Encryption

|   | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| B | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| I | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I |
| K | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J |
| L | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
| M | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L |
| N | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| O | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| P | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| Q | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| R | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R |
| T | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| U | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T |
| V | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

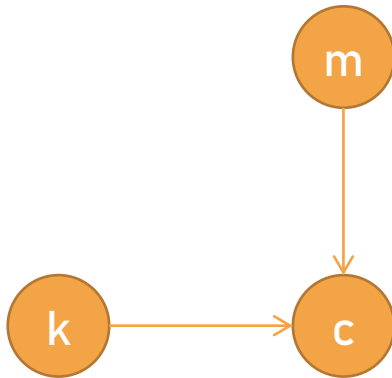
1.

# Vigenere Cipher

TO BE OR NOT TO BE THAT IS THE QUESTION

Keyword: RELATIONS

Keyword: RELATIONSRELATIONSRELATIONSREL  
Plaintext: TOBEORNOTTOBETHATISTHEQUESTION  
Ciphertext:KSMHZBBLKSMEMPOGAJXS EJC SFLZSY



Encryption

- The **strength** of the Vigenere cipher against frequency analysis can be seen by examining the above ciphertext.

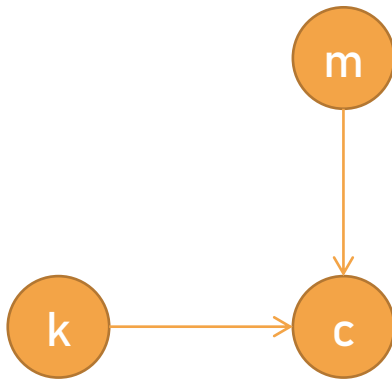
## 1.

## Vignere Cipher

TO BE OR NOT TO BE THAT IS THE QUESTION

Keyword: RELATIONS

Keyword: RELATIONSRELATIONSRELATIONSREL  
 Plaintext: T O B E O R N O T T O B E T H A T I S T H E Q U E S T I O N  
 Ciphertext: K S M E H Z B B L K S M E M P O G A J X S E J C S F L Z S Y



Encryption

- The **strength** of the Vignere cipher against frequency analysis can be seen by examining the above ciphertext.
- Note that there are 7 'T's in the plaintext message and that they have been encrypted by 'K,' 'L,' 'K,' 'M,' 'G,' 'X,' and 'L' respectively.
- This successfully masks the frequency characteristics of the English 'T'.

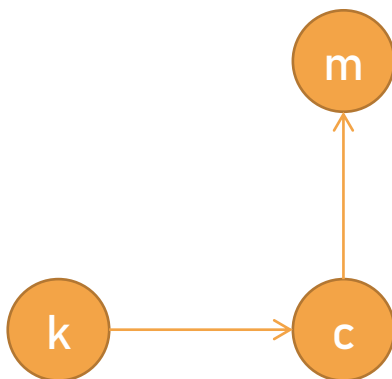
1.

# Vignere Cipher

TO BE OR NOT TO BE THAT IS THE QUESTION

Keyword: RELATIONS

Keyword: RELATIONSRELATIONSRELATIONSREL  
 Plaintext:  
 Ciphertext: K S M E H Z B B L K S M E M P O G A J X S E J C S F L Z S Y



Decryption

|   | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| B | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| I | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I |
| K | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J |
| L | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
| M | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L |
| N | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| O | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| P | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| Q | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| R | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R |
| T | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| U | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T |
| V | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

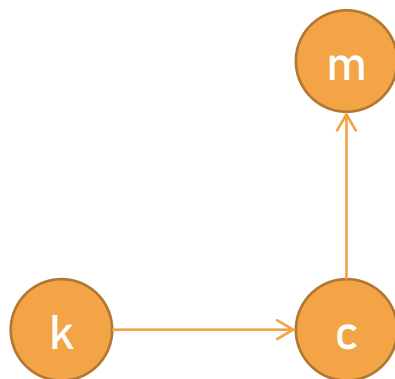
1.

# Vignere Cipher

TO BE OR NOT TO BE THAT IS THE QUESTION

Keyword: RELATIONS

Keyword: RELATIONSRELATIONSRELATIONSREL  
 Plaintext: T  
 Ciphertext: K S M E H Z B B L K S M E M P O G A J X S E J C S F L Z S Y



Decryption

|   | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| B | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| I | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I |
| K | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J |
| L | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
| M | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L |
| N | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| O | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| P | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| Q | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| R | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R |
| T | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| U | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T |
| V | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

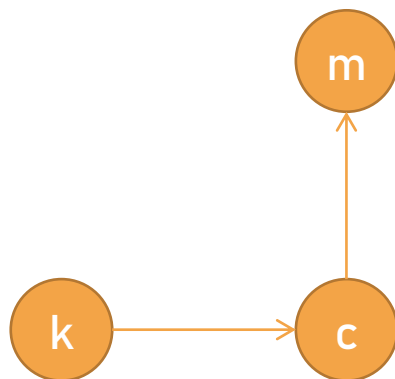
1.

# Vignere Cipher

TO BE OR NOT TO BE THAT IS THE QUESTION

Keyword: RELATIONS

Keyword: RELATIONSRELATIONSRELATIONSREL  
 Plaintext: TO  
 Ciphertext: KSM EH Z B B L K S M E M P O G A J X S E J C S F L Z S Y



Decryption

|   | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| B | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| I | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I |
| K | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J |
| L | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
| M | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L |
| N | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| O | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| P | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| Q | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| R | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R |
| T | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| U | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T |
| V | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

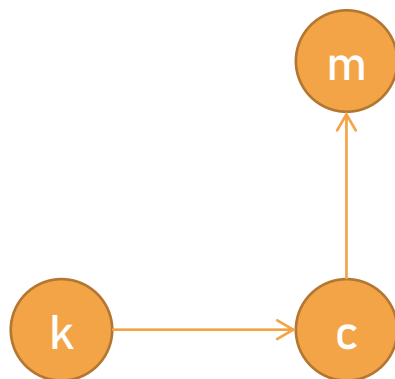
1.

# Vignere Cipher

TO BE OR NOT TO BE THAT IS THE QUESTION

Keyword: RELATIONS

Keyword: RELATIONSRELATIONSRELATIONSREL  
 Plaintext: TOB  
 Ciphertext: KSM EH Z B B L K S M E M P O G A J X S E J C S F L Z S Y



Decryption

|   | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| B | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| I | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I |
| K | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J |
| L | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
| M | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L |
| N | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| O | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| P | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| Q | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| R | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R |
| T | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| U | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T |
| V | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

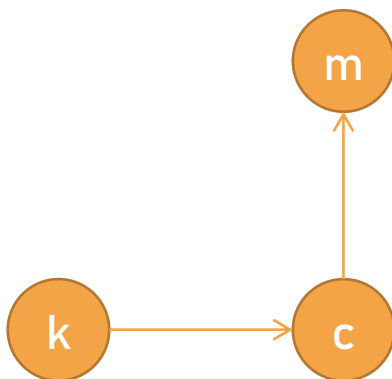
1.

# Vignere Cipher

TO BE OR NOT TO BE THAT IS THE QUESTION

Keyword: RELATIONS

Keyword: RELATIONSRELATIONSRELATIONSREL  
 Plaintext: TOBEORNOTTOBETHATISTHEQUESTION  
 Ciphertext: KSMHZZBBLKSMEMPOGAJXS EJC SFLZSY

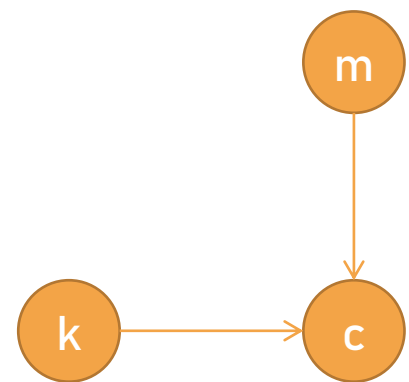


Decryption

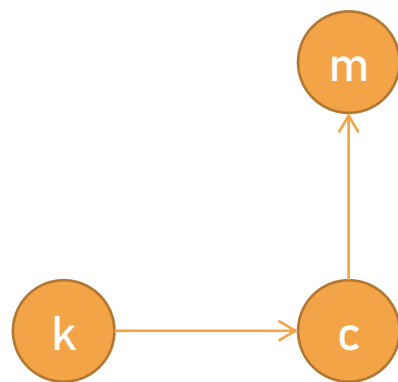
|   | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| B | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| I | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I |
| K | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J |
| L | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
| M | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L |
| N | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| O | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| P | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| Q | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| R | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R |
| T | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| U | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T |
| V | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

1.

# Vignere Cipher



Encryption



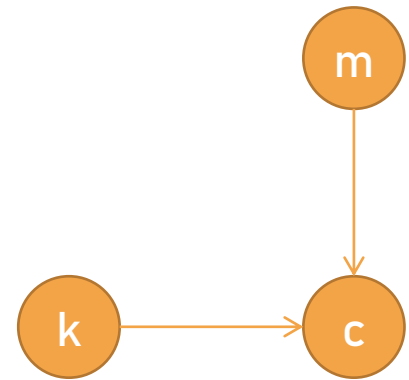
Decryption

Keyword: RELATIONS

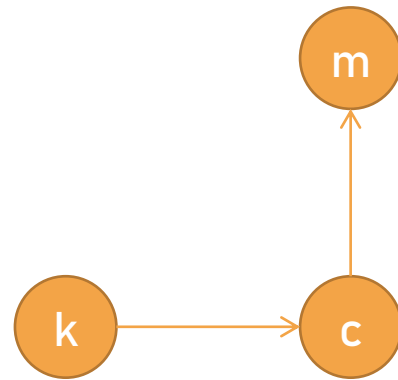
|   | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| B | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| I | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I |
| K | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J |
| L | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
| M | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L |
| N | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| O | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| P | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| Q | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| R | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R |
| T | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| U | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T |
| V | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |

1.

# Vigenere Cipher



Encryption



Decryption

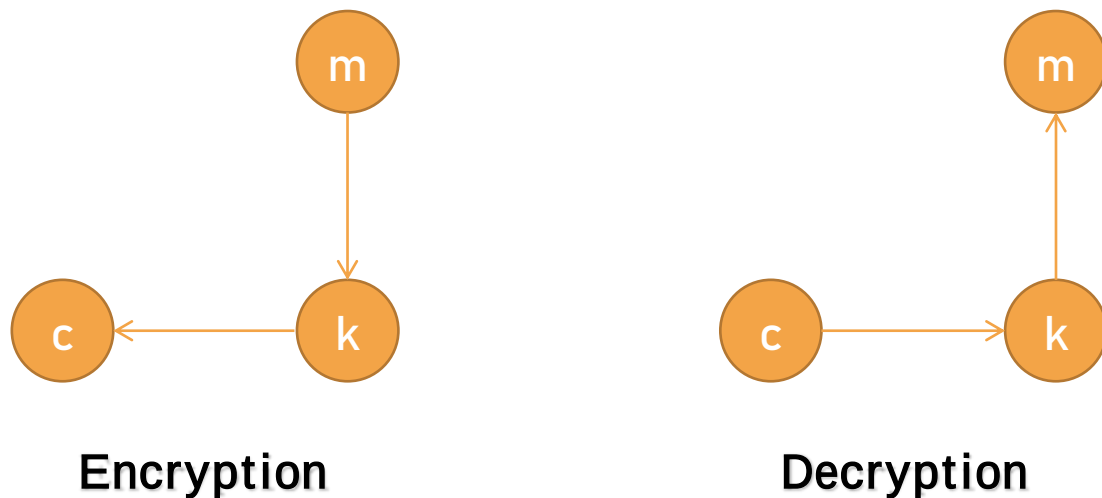
Keyword: RELATIONS

|   | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| E | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| I | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| L | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
| N | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| O | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| R | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R |
| T | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |

| Cipher   | Enciphering   | Deciphering   |
|----------|---------------|---------------|
| Vigenere | $c = m + k_i$ | $m = c - k_i$ |

2.

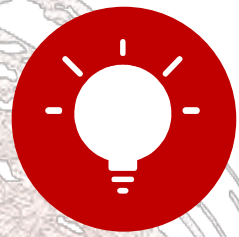
# Beaufort Cipher



**Keyword:** RELATIONSRELATIONSRELATIONSREL  
**Plaintext:** TOBEORNOTTOBETHATISTHEQUESTION  
**Ciphertext:** YQKWFRBZZYQKWABOUKZLEWDOKVZJQY

| Cipher   | Enciphering   | Deciphering   |
|----------|---------------|---------------|
| Beaufort | $c = k_i - m$ | $m = k_i - c$ |

|   | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z |
| B | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A |
| C | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B |
| D | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C |
| E | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D |
| F | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E |
| G | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F |
| H | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G |
| I | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H |
| J | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I |
| K | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J |
| L | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K |
| M | M | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L |
| N | N | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M |
| O | O | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N |
| P | P | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O |
| Q | Q | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P |
| R | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R |
| T | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S |
| U | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T |
| V | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U |
| W | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V |
| X | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W |
| Y | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X |
| Z | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | O | P | Q | R | S | T | U | V | W | X | Y |



# Substitution Cipher

A system of encryption in which **each letter of a message is replaced with another character**, but retains its position within the message.



## Polygraphic

Polygram substitution ciphers encipher **block of letters** at the time, rather than a single letter.

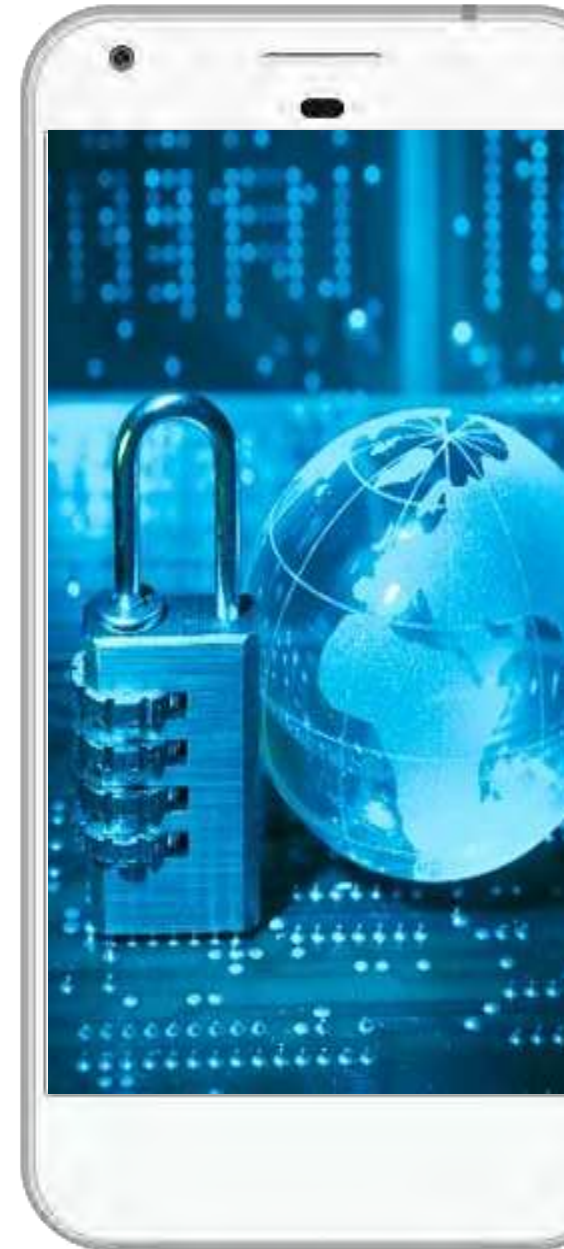
This makes cryptanalysis **harder**, as it destroys the single letter frequency distribution.

1.

**Playfair Cipher**

2.

**Hill Cipher**



1.

# Playfair Cipher

To encipher a message in Playfair,

- **Pick** a keyword.
- **Omit** the repeated letters.
- **Follow** the keyword with the rest of the alphabet.
- **Write** it into a 5X5 Square.
- **Combine** I and J in one cell.



1.

# Playfair Cipher

Example

If we **pick** the keyword

**MANCHESTER**



1.

# Playfair Cipher

Example

If we **pick** the keyword

**MANCHESTER**



1.

# Playfair Cipher

Example

**MANCHEST R**  
**Omit**



1.

# Playfair Cipher

Example

**MANCHESTR**

**Omit**



1.

# Playfair Cipher

Example

**MANCHESTR**BDFGIJKLOPQUVWXYZ

**Follow**



1.

# Playfair Cipher

## Example

|   |   |   |   |   |
|---|---|---|---|---|
| M | A | N | C | H |
| E | S | T | R | B |
| D | F | G | I | K |
| L | O | P | Q | U |
| V | W | X | Y | Z |

**Write**



1.

# Playfair Cipher

## Example

|   |   |   |     |   |
|---|---|---|-----|---|
| M | A | N | C   | H |
| E | S | T | R   | B |
| D | F | G | I/J | K |
| L | O | P | Q   | U |
| V | W | X | Y   | Z |

**Combine**



# 1.

# Playfair Cipher

## Example

|   |   |   |     |   |
|---|---|---|-----|---|
| M | A | N | C   | H |
| E | S | T | R   | B |
| D | F | G | I/J | K |
| L | O | P | Q   | U |
| V | W | X | Y   | Z |

This is the **key** that we will use to encipher and decipher our message.



## 1. Playfair Cipher

To encrypt

**“THIS SECRET MESSAGE IS ENCRYPTED”**

We need to **prepare** the plaintext message by **break it up** into two-letter groups.



## 1. Playfair Cipher

If both letters in a **pair** are the same, insert an X between them.

If there is only one letter in the last group, add an X to it.

THIS SECRET MESSAGE IS ENCRYPTED

TH IS SE CR ET ME **SX** SA GE IS EN CR YP TE D



## 1. Playfair Cipher

If both letters in a **pair** are the same, insert an X between them.

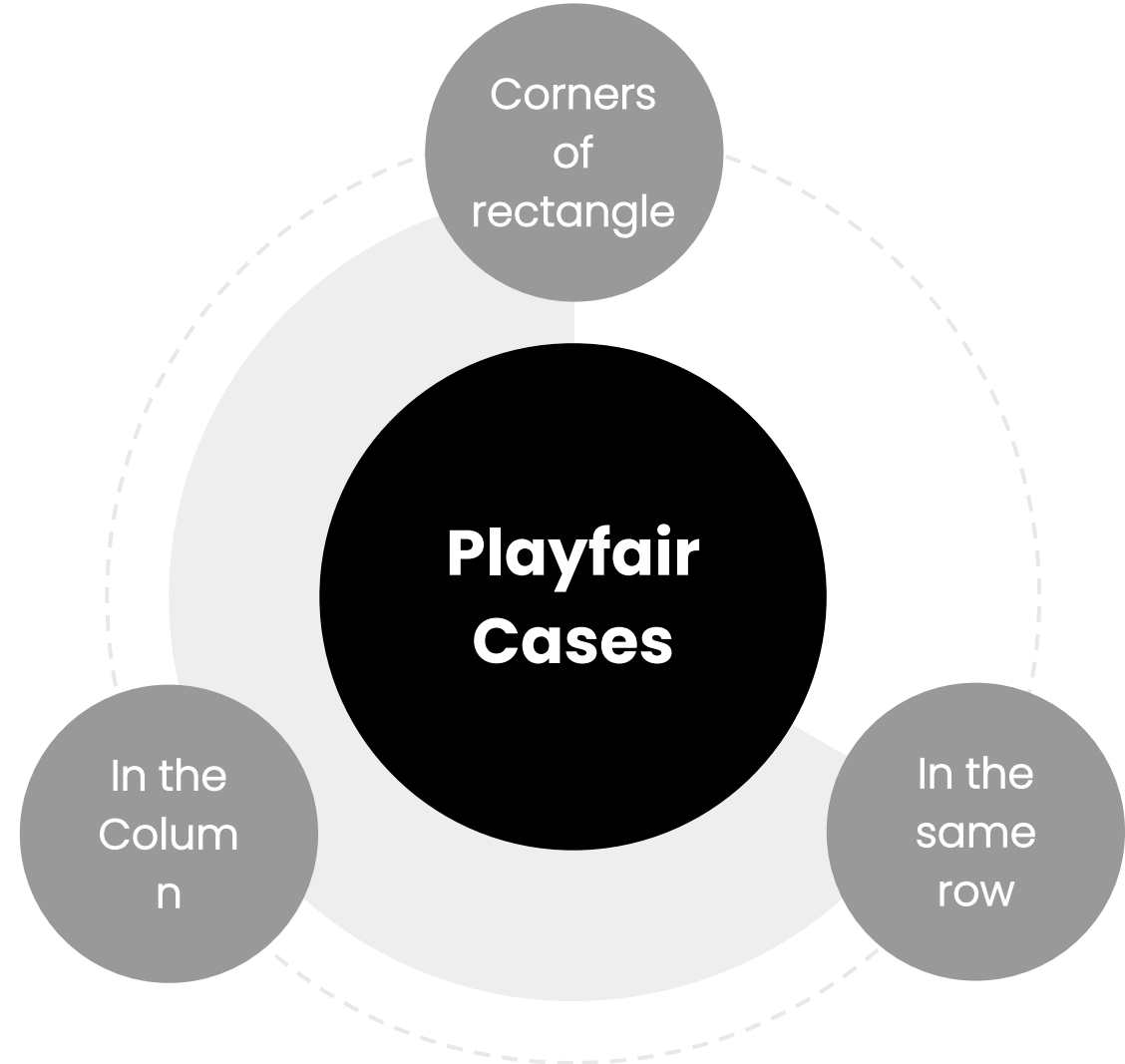
If there is only one letter in the last group, add an X to it.

THIS SECRET MESSAGE IS ENCRYPTED

TH IS SE CR ET ME **SX** SA GE IS EN CR YP TE **DX**



There are **three** possible cases for the letters of the pair



|   |   |   |   |   |
|---|---|---|---|---|
| . | . | N | ← | H |
| . | . | T | → | B |
| . | . | . | . | . |
| . | . | . | . | . |
| . | . | . | . | . |

|   |   |   |     |   |
|---|---|---|-----|---|
| M | A | N | C   | H |
| E | S | T | R   | B |
| D | F | G | I/J | K |
| L | O | P | Q   | U |
| V | W | X | Y   | Z |

TH IS SE CR ET ME SX SA GE IS EN CR YP TE DX  
BN

|   |   |   |     |   |
|---|---|---|-----|---|
| . | . | . | .   | . |
| . | S | . | R   | . |
| . | F | . | I/J | . |
| . | . | . | .   | . |
| . | . | . | .   | . |

|   |   |   |     |   |
|---|---|---|-----|---|
| M | A | N | C   | H |
| E | S | T | R   | B |
| D | F | G | I/J | K |
| L | O | P | Q   | U |
| V | W | X | Y   | Z |

TH IS SE CR ET ME SX SA GE IS EN CR YP TE DX  
BN FR

|   |   |   |   |   |
|---|---|---|---|---|
| . | . | . | . | . |
| E | S | T | . | . |
| . | . | . | . | . |
| . | . | . | . | . |
| . | . | . | . | . |

|   |   |   |     |   |
|---|---|---|-----|---|
| M | A | N | C   | H |
| E | S | T | R   | B |
| D | F | G | I/J | K |
| L | O | P | Q   | U |
| V | W | X | Y   | Z |

TH IS SE CR ET ME SX SA GE IS EN CR YP TE DX  
BN FR TS

|   |   |   |     |   |
|---|---|---|-----|---|
| . | . | . | C   | . |
| . | . | . | R   | . |
| . | . | . | I/J | . |
| . | . | . | .   | . |
| . | . | . | .   | . |

|   |   |   |     |   |
|---|---|---|-----|---|
| M | A | N | C   | H |
| E | S | T | R   | B |
| D | F | G | I/J | K |
| L | O | P | Q   | U |
| V | W | X | Y   | Z |

TH IS SE CR ET ME SX SA GE IS EN CR YP TE DX  
BN FR TS RI

Plaintext

TH IS SE CR ET ME SX SA GE IS EN CR YP TE DX

Ciphertext

BN FR TS RI SR ED TW FS DT FR TM RI XQ RS GV

## Playfair Cipher

To decrypt the message, simply **reverse** the process:

- If the two letters are in **different rows and columns**, take the letters in the opposite corners of their rectangle.
- In the **same row**, take the letters to the left.
- In the **same column**, take the letters above each of them.



## 2.

## Hill Cipher

- The message divided onto a number of blocks  $M$ , each block contains  $d$  letters.
- Then rearranges it in matrix of **one column and  $d$  rows**.
- And we use a **matrix  $K$  with the size  $d \times d$**  that contains numbers from the range between 0 and 25, then

$$C = KM \bmod 26$$

For example, if

$$K = \begin{bmatrix} 3 & 3 \\ 2 & 5 \end{bmatrix} \Rightarrow K^{-1} = \begin{bmatrix} 15 & 17 \\ 20 & 9 \end{bmatrix}$$

## 2.

## Hill Cipher

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

and we want to encipher the message **HELP**, then

$$M_1 = \begin{bmatrix} H \\ E \end{bmatrix} = \begin{bmatrix} 7 \\ 4 \end{bmatrix} \quad M_2 = \begin{bmatrix} L \\ P \end{bmatrix} = \begin{bmatrix} 11 \\ 15 \end{bmatrix}$$

$$C_1 = KM_1 = \begin{bmatrix} 3 & 3 \\ 2 & 5 \end{bmatrix} \begin{bmatrix} 7 \\ 4 \end{bmatrix} = \begin{bmatrix} 33 \\ 34 \end{bmatrix} = \begin{bmatrix} 7 \\ 8 \end{bmatrix} = \begin{bmatrix} H \\ I \end{bmatrix}$$

$$C_2 = KM_2 = \begin{bmatrix} 3 & 3 \\ 2 & 5 \end{bmatrix} \begin{bmatrix} 11 \\ 15 \end{bmatrix} = \begin{bmatrix} 78 \\ 97 \end{bmatrix} = \begin{bmatrix} 0 \\ 19 \end{bmatrix} = \begin{bmatrix} A \\ T \end{bmatrix}$$

so, the ciphertext is **HIAT**.

## 2.

## Hill Cipher

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

Now to decipher the word **HIAT**

$$C_1 = \begin{bmatrix} H \\ I \end{bmatrix} = \begin{bmatrix} 7 \\ 8 \end{bmatrix} \quad C_2 = \begin{bmatrix} A \\ T \end{bmatrix} = \begin{bmatrix} 0 \\ 19 \end{bmatrix}$$

$$M_1 = K^{-1}C_1 = \begin{bmatrix} 15 & 17 \\ 20 & 9 \end{bmatrix} \begin{bmatrix} 7 \\ 8 \end{bmatrix} = \begin{bmatrix} 241 \\ 212 \end{bmatrix} = \begin{bmatrix} 7 \\ 4 \end{bmatrix} = \begin{bmatrix} H \\ E \end{bmatrix}$$

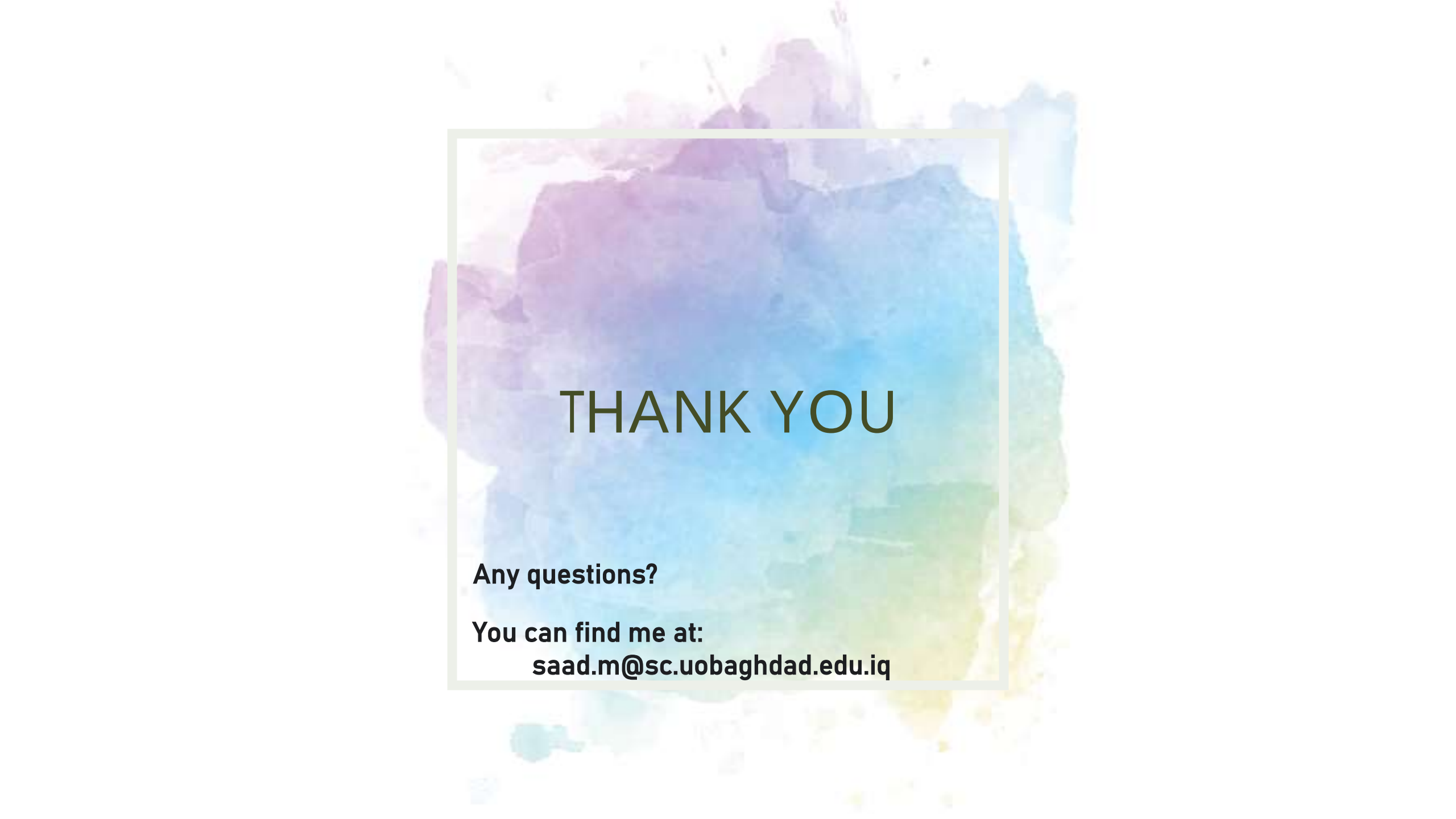
$$M_2 = K^{-1}C_2 = \begin{bmatrix} 15 & 17 \\ 20 & 9 \end{bmatrix} \begin{bmatrix} 0 \\ 19 \end{bmatrix} = \begin{bmatrix} 323 \\ 171 \end{bmatrix} = \begin{bmatrix} 11 \\ 15 \end{bmatrix} = \begin{bmatrix} L \\ P \end{bmatrix}$$

so, the original word is **HELP**.

Deciphering



Use K in the above example to calculate  $K^{-1}$ .



# THANK YOU

**Any questions?**

**You can find me at:**

**[saad.m@sc.uobaghdad.edu.iq](mailto:saad.m@sc.uobaghdad.edu.iq)**

# Introduction to Cipher Systems

**Saad Al-Momen**



**CIPHER SYSTEMS**

**Fourth Class**

**Department of Mathematics**

**College of Science - University of Baghdad**



# One-Time Pads



# One-Time Pads

During the war, an AT&T engineer **Gilbert Vernam** proposed a system called the One-Time Pad that has perfect security.

In this system **additive ciphers** are used to encipher each letter of the plaintext; however, **the shift is different for each letter!**

**Plaintext:** THE BRITISH HAVE FIFTY TANKS

**Key:** SHE LOVES HIM SO VERY MUCH NOW





# One-Time Pads

**Plaintext:** THE BRITISH HAVE FIFTY TANKS

**Key:** SHE LOVES HIM SO VERY MUCH NOW

|       |    |    |   |    |    |    |    |    |    |    |    |    |    |    |
|-------|----|----|---|----|----|----|----|----|----|----|----|----|----|----|
| m:    | T  | H  | E | B  | R  | I  | T  | I  | S  | H  | H  | A  | V  | E  |
|       | 19 | 7  | 4 | 1  | 17 | 8  | 19 | 8  | 18 | 7  | 7  | 0  | 21 | 4  |
| k:    | S  | H  | E | L  | O  | V  | E  | S  | H  | I  | M  | S  | O  | V  |
|       | 18 | 7  | 4 | 11 | 14 | 21 | 4  | 18 | 7  | 8  | 12 | 18 | 14 | 21 |
| Add : | 37 | 14 | 8 | 12 | 31 | 29 | 23 | 26 | 25 | 15 | 19 | 18 | 35 | 25 |
| Mod : | 11 | 14 | 8 | 12 | 5  | 3  | 23 | 0  | 25 | 15 | 19 | 18 | 9  | 25 |
|       | L  | O  | I | M  | F  | D  | X  | A  | Z  | P  | T  | S  | J  | Z  |





# One-Time Pads

- Different letters of ciphertext could correspond to the **same** plaintext letter, and vice versa.
- This cryptosystem is virtually **unbreakable**.
- The **weakness** is the key which must be immense. This must be shared by all communicants.
- Also, **statistical analysis may be possible if the key is a regular text**; for this reason some effort is usually made to choose keys which are truly random sequences of characters.

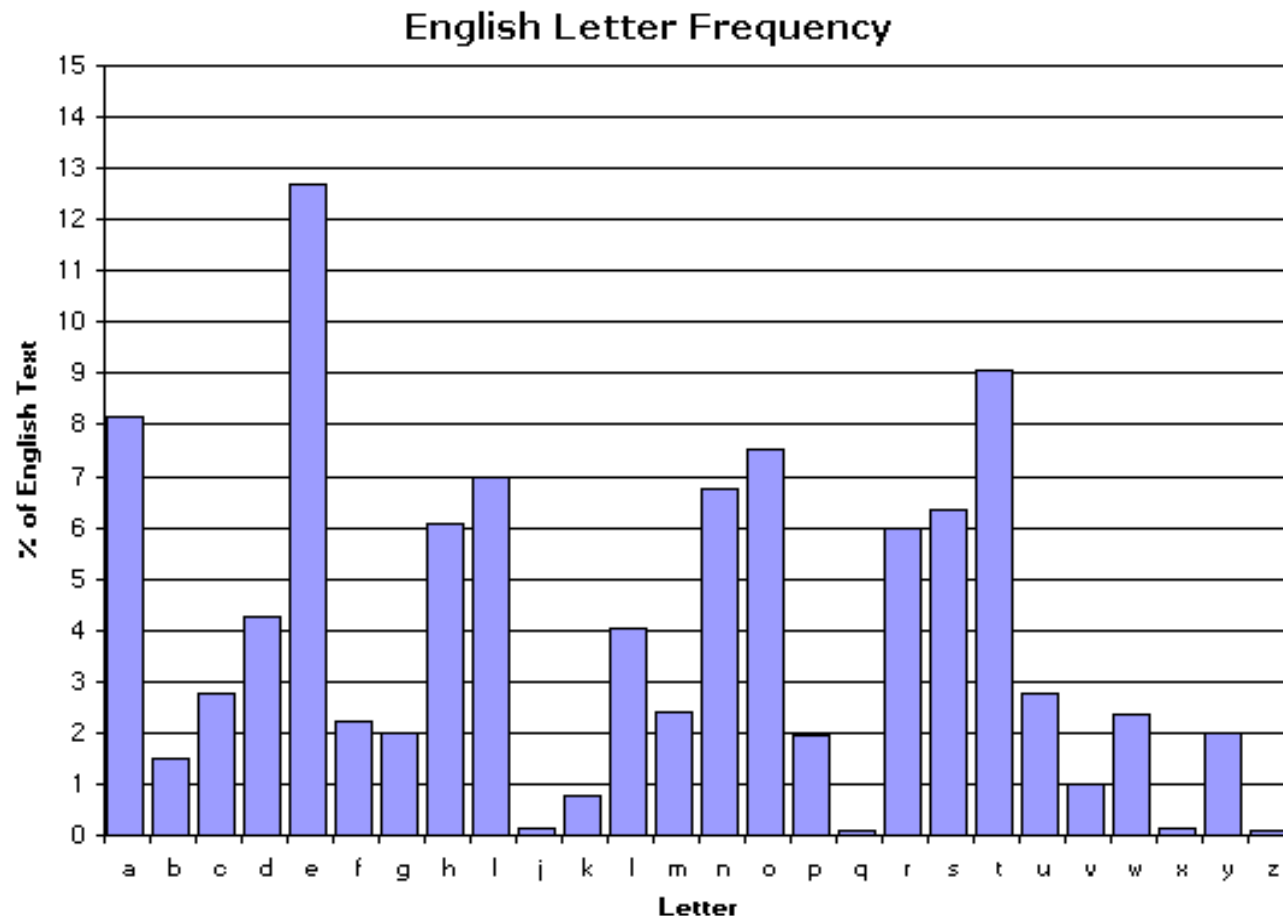




# **Some Concepts on Cryptanalysis**

# Frequency

Number of appearance of the letter in the ciphertext, where the frequencies of the ciphertext letters are compared with the frequencies of the Language.



| Letter | %      | Letter | %     |
|--------|--------|--------|-------|
| a      | 8.167  | n      | 6.749 |
| b      | 1.492  | o      | 7.507 |
| c      | 2.782  | p      | 1.929 |
| d      | 4.253  | q      | 0.095 |
| e      | 12.702 | r      | 5.987 |
| f      | 2.228  | s      | 6.327 |
| g      | 2.015  | t      | 9.056 |
| h      | 6.094  | u      | 2.758 |
| i      | 6.966  | v      | 0.978 |
| j      | 0.153  | w      | 2.360 |
| k      | 0.772  | x      | 0.150 |
| l      | 4.025  | y      | 1.974 |
| m      | 2.406  | z      | 0.074 |

## Repetition

It is the **similar parts** in the ciphertext that have length not less than three.

This helps us to **find the length of the key** (the number of alphabets that used to enciphering in the polyalphabetic systems).

## Index of Coincidence (IC)

It is the probability that **two letters** selected from the text are **identical**

$$IC = \frac{\sum_{i=1}^Z f_i(f_i - 1)}{n(n - 1)}$$

- The IC value **differs** from language to another.
- IC can be used to **discover** if the message were enciphered using Monoalphabetic system or polyalphabetic system.



# Coincidence

---

It is the **computing of the coincidence** of the ciphertexts, where two messages put one over the other, and the purpose is to discover if the two messages were enciphered using the same **key**.

In the two messages

7 coincidence letters between 100 → Same key

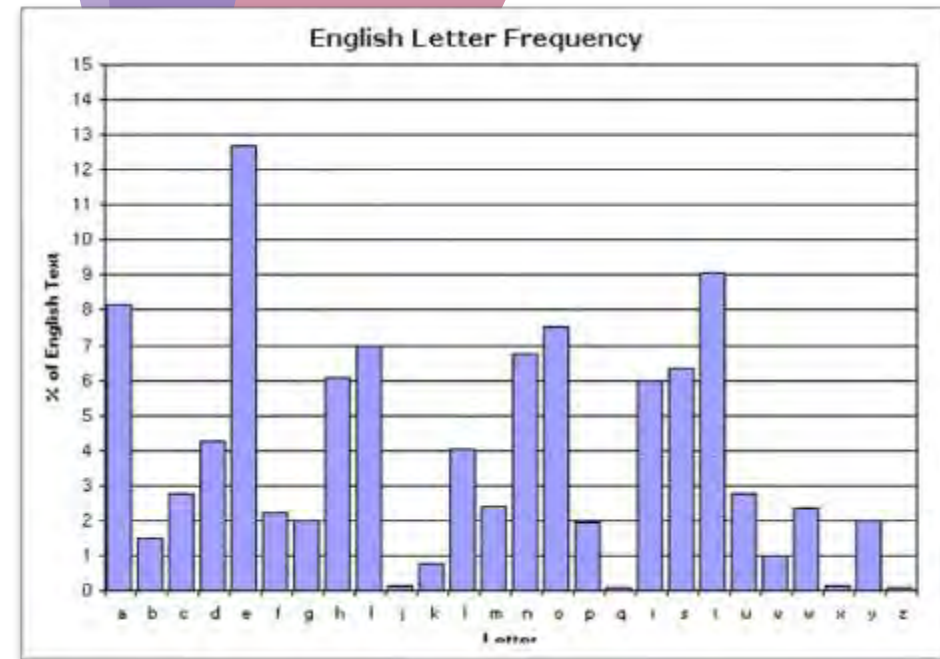
4 coincidence letters between 100 → different keys

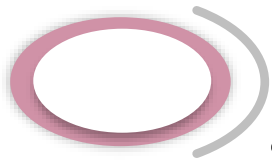


# **Cryptanalysis Examples**

First of all we must specified the type of the cipher system that was used.

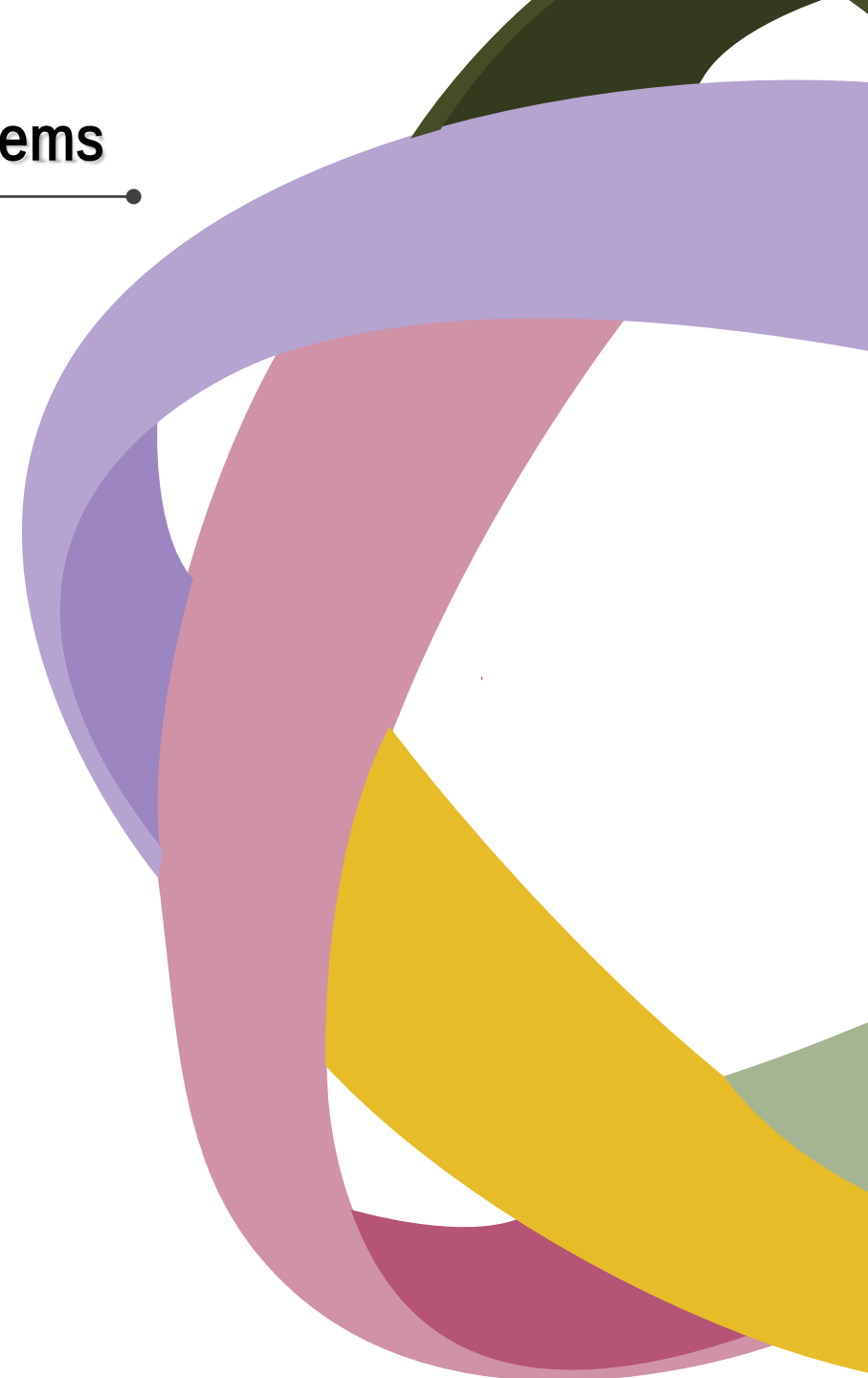
If the frequencies of the ciphertext are the **same** as the frequencies of the language then, **transposition** cipher system was used; **otherwise** a **substitution** cipher system was used.

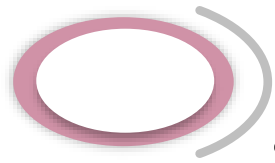




## Cryptanalysis of **Transposition** Cipher Systems

When we decide that a transposition cipher system were used, we put the cipher text in  $m \times n$  matrix,  $m$  and  $n$  depends on the length of the received ciphertext, for example if the length is 500 then one of the possible sizes is  $20 \times 25$ . Then we **rearrange** the columns to get some known patterns such as (and, the, ion, that,...) in addition to some expected word in the message.

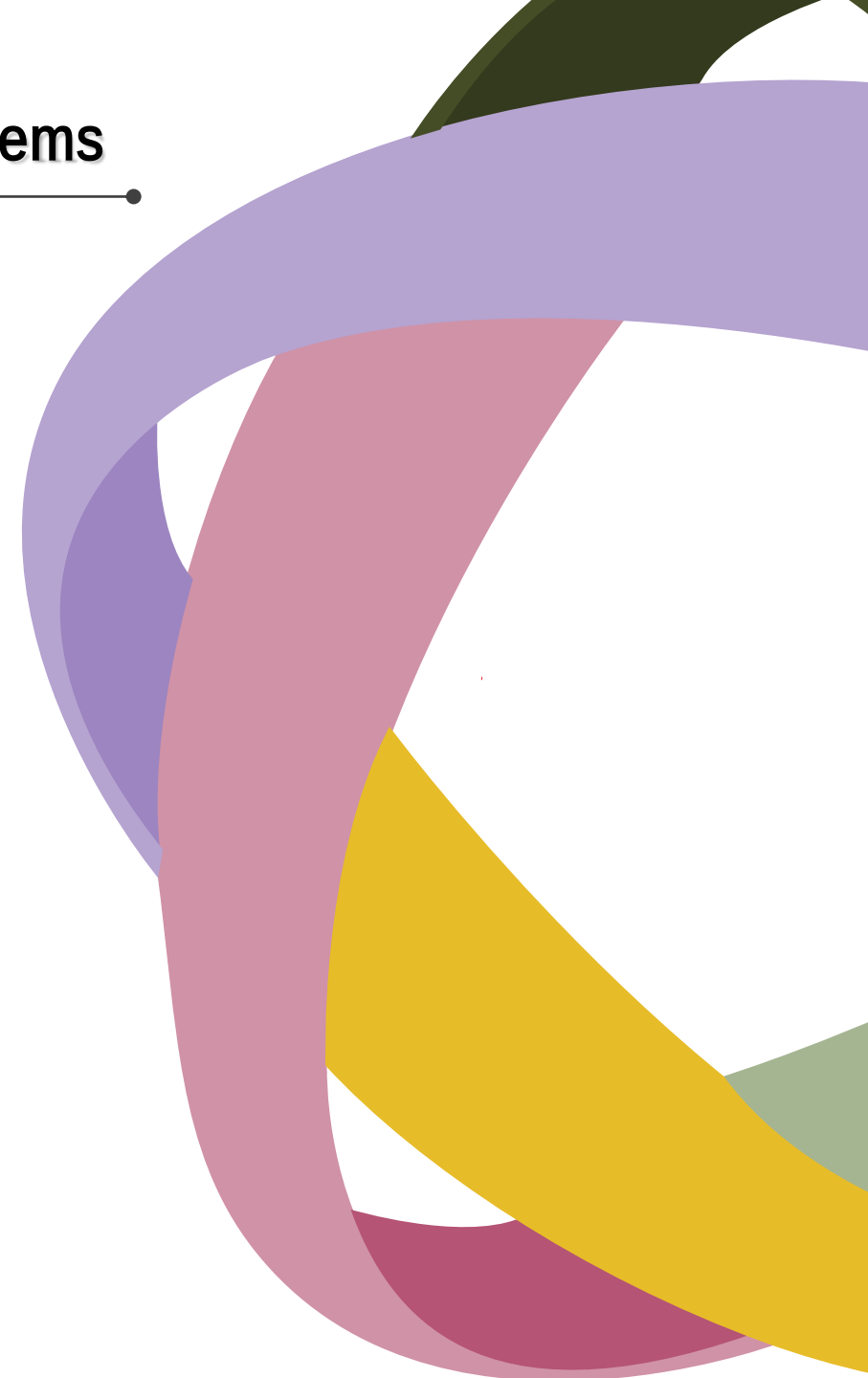




## Cryptanalysis of **Transposition** Cipher Systems

---

As we know there are two types of transposition cipher system: **simple** and **double** transposition, the cryptanalysis of the last one is more complicated because we lose the ability to find the known patterns.





## Columnar Transposition



Simple Transposition

Plaintext = UNIVERSITY OF BAGHDAD~~X~~

| 1 | 2 | 3 | 4 | 5 |
|---|---|---|---|---|
| U | N | I | V | E |
| R | S | I | T | Y |
| O | F | B | A | G |
| H | D | A | D | X |

If the key is (4,3,2,1,5)



| 4 | 3 | 2 | 1 | 5 |
|---|---|---|---|---|
| V | I | N | U | E |
| T | I | S | R | Y |
| A | B | F | O | G |
| D | A | D | H | X |

Ciphertext = VTADIIBANSFDUROHEYGX

# Double Columnar Transposition

2

Double Transposition

2 4 3 5 7 1 6  
D I G I T A L  
U N I V E R S  
I T Y O F B A  
G H D A D X X

Number the letters  
in the keyword in  
alphabetical order.

2 1 3 4  
B A C K  
R B X U  
I G I Y  
D N T H  
V O A S  
A X F E  
D X X X

Select and number a  
second keyword (example  
BACK), and write CT<sub>1</sub>  
under it in rows

First pick a keyword,  
such as DIGITAL, and  
then write the message  
under it in rows

D I G I T A L  
U N I V E R S  
I T Y O F B A  
G H D A D X X

Read the cipher off by  
columns, starting with  
the lowest-numbered  
column

CT<sub>1</sub> = RBXUIGIYDNTHVOASAXEFD

Take it off by columns  
again

CT<sub>2</sub> = BGNOXXRIDVADXITAFXUYHSEX

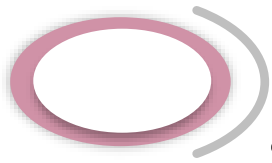
# Cryptanalysis of Substitution Cipher Systems

$$IC = \frac{141(141 - 1) + 36(36 - 1) + \dots + 23(23 - 1) + 0(0 - 1)}{1679(1679 - 1)} = \frac{184838}{2817362} \approx 0.0656.$$

| Letter | Count | Letter | count |
|--------|-------|--------|-------|
| A      | 141   | N      | 119   |
| B      | 36    | O      | 132   |
| C      | 36    | P      | 28    |
| D      | 103   | Q      | 1     |
| E      | 188   | R      | 95    |
| F      | 37    | S      | 64    |
| G      | 34    | T      | 182   |
| H      | 102   | U      | 59    |
| I      | 123   | V      | 13    |
| J      | 4     | W      | 55    |
| K      | 18    | X      | 3     |
| L      | 56    | Y      | 23    |
| M      | 27    | Z      | 0     |

$$IC = \frac{\sum_{i=1}^n f_i(f_i - 1)}{n(n - 1)}$$

Example 1

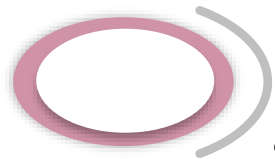


## Cryptanalysis of Substitution Cipher Systems

What is the index of coincidence for a collection of 2600 letters consisting of 100 A's, 100 B's, 100 C's, ..., 100 Z's?

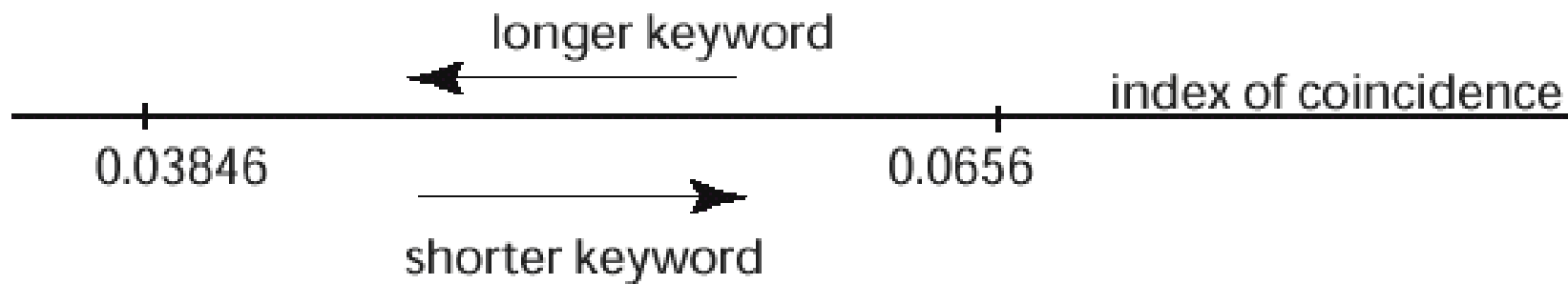
$$IC = \frac{100 \cdot 99 + 100 \cdot 99 + \dots + 100 \cdot 99 + 100 \cdot 99}{2600 \cdot 2599} \approx 0.0384615.$$

Example 2



## Cryptanalysis of Substitution Cipher Systems

Polyalphabeticity Measure for English



If the length of the text is  $n$ , we can quantify the connection between index of coincidence and keyword length  $k$ , (number of alphabets), where:

$$k \approx \frac{0.0265 \cdot n}{(0.065 - IC) + n(IC - 0.0385)}$$

# Cryptanalysis of Substitution Cipher Systems

$$IC = \frac{60 \cdot 59 + 50 \cdot 49 + \dots + 67 \cdot 66}{1282 \cdot 1281} = \frac{35761}{821121} \approx 0.04355.$$

| Letter | Count | Letter | count |
|--------|-------|--------|-------|
| A      | 60    | N      | 28    |
| B      | 50    | O      | 83    |
| C      | 42    | P      | 44    |
| D      | 64    | Q      | 69    |
| E      | 51    | R      | 13    |
| F      | 63    | S      | 29    |
| G      | 19    | T      | 66    |
| H      | 48    | U      | 87    |
| I      | 56    | V      | 63    |
| J      | 67    | W      | 19    |
| K      | 23    | X      | 43    |
| L      | 45    | Y      | 39    |
| M      | 44    | Z      | 67    |

Example 3

## Cryptanalysis of Substitution Cipher Systems

$$IC = \frac{60 \cdot 59 + 50 \cdot 49 + \dots + 67 \cdot 66}{1282 \cdot 1281} = \frac{35761}{821121} \approx 0.04355.$$

$$K = \frac{0.0265 \cdot 1282}{(0.065 - 0.04355) + 1282(0.04355 - 0.03846)} = 5.1892.$$

Based only on this evidence, a reasonably likely keyword length is **5**.

Example 3



# **Cryptanalysis Process**



# Cryptanalysis Process

Now, after the above tests if we conclude that a **monoalphabetic** cipher system was used, then:

- ❶ If a direct standard or reversed system were used, we **compare the frequencies** of the ciphertext with the frequencies of the English language, start by **putting E against the letter with the higher frequency** in the ciphertext, then we put the other letters **sequentially**.
- ❷ If a mixed cipher system was used (**Random**) then we **compare the frequencies** of the ciphertext with that frequency table of the language.





# Cryptanalysis Process

## 1. Direct Standard

Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

Ciphertext alpha.:

|   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |   |   |   |
|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|---|---|
| D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  | A | B | C |
| 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 0 | 1 | 2 |

As an example, if the message is: UNIVERSITY OF BAGHDAD, then

|   |   |   |   |   |   |   |   |   |   |  |   |   |  |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|---|--|---|---|--|---|---|---|---|---|---|---|
| U | N | I | V | E | R | S | I | T | Y |  | O | F |  | B | A | G | H | D | A | D |
| X | Q | L | Y | H | U | V | L | W | B |  | R | I |  | E | D | J | K | G | D | G |

As we see, in Caesar cipher the key is  $k=3$

We can choose a different value to the key in the range between 0 and 25.

$$c = E_k(m) = (m + k) \bmod 26$$





# Cryptanalysis Process

## 2. Standard Reverse

- This method is similar to the Direct standard, except that the ciphertext alphabet are written in **reversed order from Z to A**.

$$\text{Encipher: } c = E_k(m) = (25 - m + k) \bmod 26$$

For example if  $k=0$  then,

Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

Ciphertext alpha.:

|    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |   |   |   |   |   |   |   |   |   |   |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|---|---|---|---|---|---|---|---|---|
| 25 | 24 | 23 | 22 | 21 | 20 | 19 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
| Z  | Y  | X  | W  | V  | U  | T  | S  | R  | Q  | P  | O  | N  | M  | L  | K  | J | I | H | G | F | E | D | C | B | A |





# Cryptanalysis Process

## 2. Standard Reverse

- This method is similar to the Direct standard, except that the ciphertext alphabet are written in **reversed order from Z to A**.

$$\text{Encipher: } c = E_k(m) = (25 - m + k) \bmod 26$$

For example if  $k=0$  then,

Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

Ciphertext alpha.:

|    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |   |   |   |   |   |   |   |   |   |   |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|---|---|---|---|---|---|---|---|---|
| 25 | 24 | 23 | 22 | 21 | 20 | 19 | 18 | 17 | 16 | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
| Z  | Y  | X  | W  | V  | U  | T  | S  | R  | Q  | P  | O  | N  | M  | L  | K  | J | I | H | G | F | E | D | C | B | A |





# Cryptanalysis Process

## 3. Multiplicative Cipher

- Ciphers based on **multiply** each character by a key  $k$ ; that  
Encipher:  $c = E_k(m) = (m * k) \bmod 26$
- Where  $k$  and 26 are relatively prime ( **$GCD(k, 26) = 1$** ), so that the letters of the alphabet produce a complete set of residues, so that in this case the key must be an **odd number and not equal to 13**.

For example if  $k=9$  then,

Plaintext alpha.:

|   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |
|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| A | B | C | D | E | F | G | H | I | J | K  | L  | M  | N  | O  | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 |

Ciphertext alpha.:

|   |   |    |   |    |    |   |    |    |   |    |    |   |    |    |   |    |    |   |    |    |   |    |    |   |    |
|---|---|----|---|----|----|---|----|----|---|----|----|---|----|----|---|----|----|---|----|----|---|----|----|---|----|
| 0 | 9 | 18 | 1 | 10 | 19 | 2 | 11 | 20 | 3 | 12 | 21 | 4 | 13 | 22 | 5 | 14 | 23 | 6 | 15 | 24 | 7 | 16 | 25 | 8 | 17 |
| A | J | S  | B | K  | T  | C | L  | U  | D | M  | V  | E | N  | W  | F | O  | X  | G | P  | Y  | H | Q  | Z  | I | R  |





# Cryptanalysis Process

For advanced analysis we can use in addition to single letter frequencies, a table of **double letter frequencies** TH, HE, IN, ER, RE, ON, AN, EN,..., and triple letter frequencies THE, AND, TIO, ATI, FOR, THA, TER, RES,... and so on.





# Cryptanalysis Process

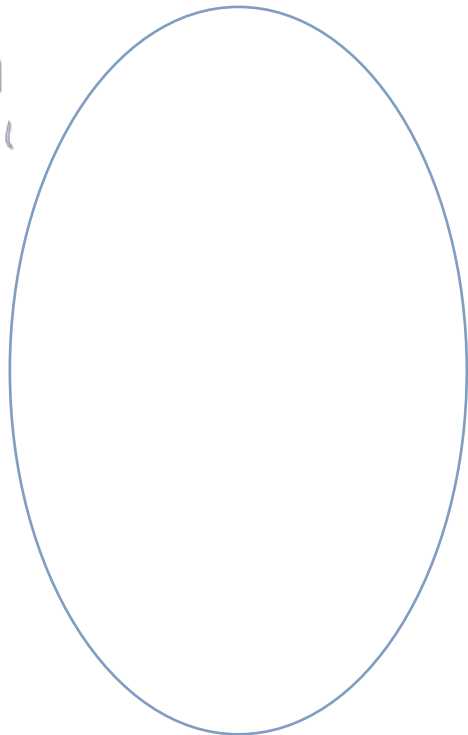
If a **polyalphabetic** cipher system was used then we will use the **Kasiski method** to find the length of the key  $k$  (number of alphabets). Then we **divide the ciphertext into  $k$  parts**, each part will analyze as in **②** above.



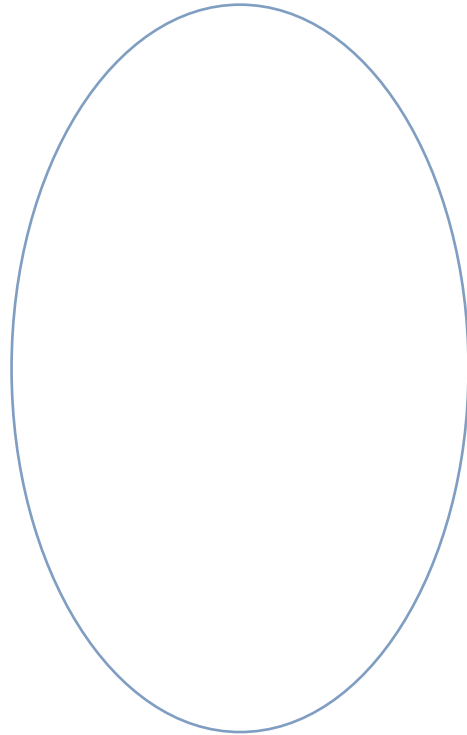


# Cryptanalysis Process

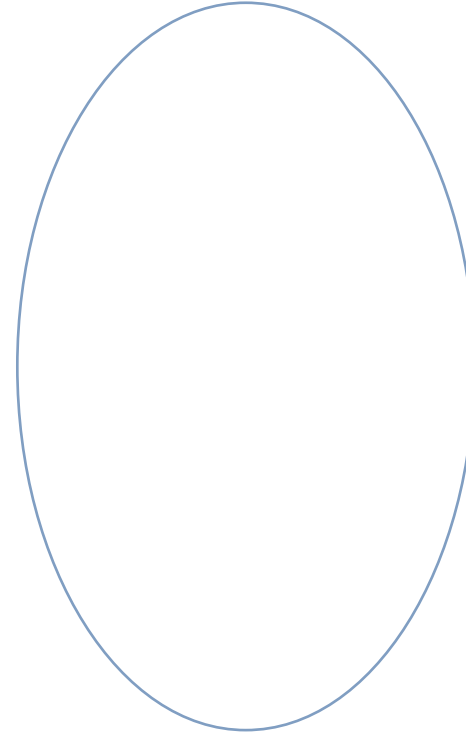
|    |   |   |   |   |   |   |   |   |   |   |   |   |   |
|----|---|---|---|---|---|---|---|---|---|---|---|---|---|
| K= | H | A | M | H | A | M | H | A | M | H | A | M | H |
| M= | T | O | B | E | O | R | N | O | T | T | O | B | E |
| C= | A | O | N | L | O | D | U | O | F | A | O | N | L |



H



A



M

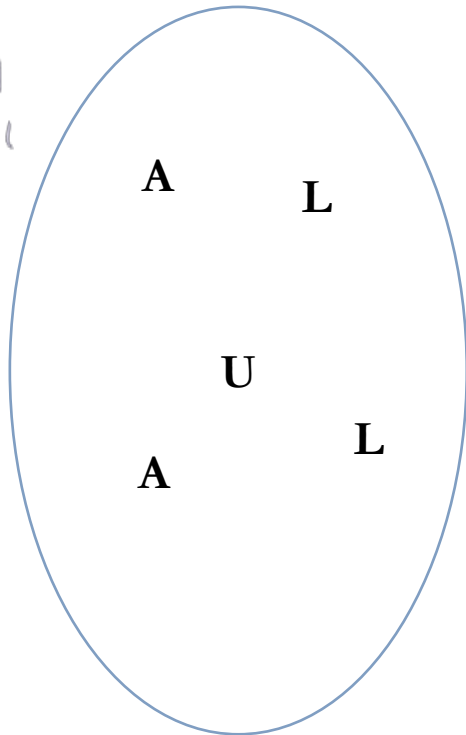


Polyalphabetic

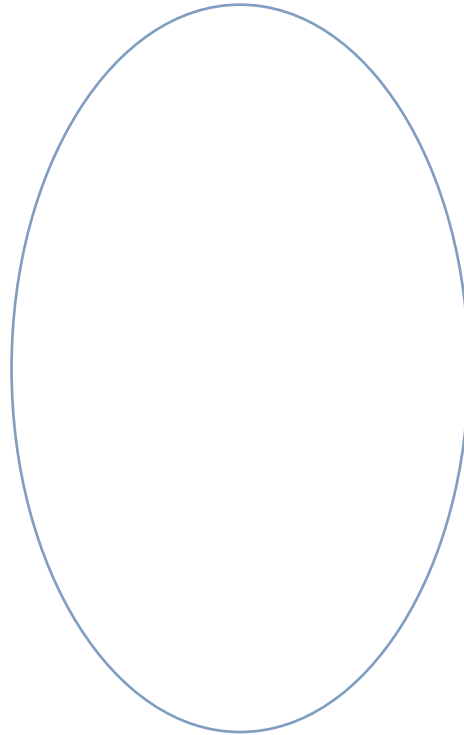


# Cryptanalysis Process

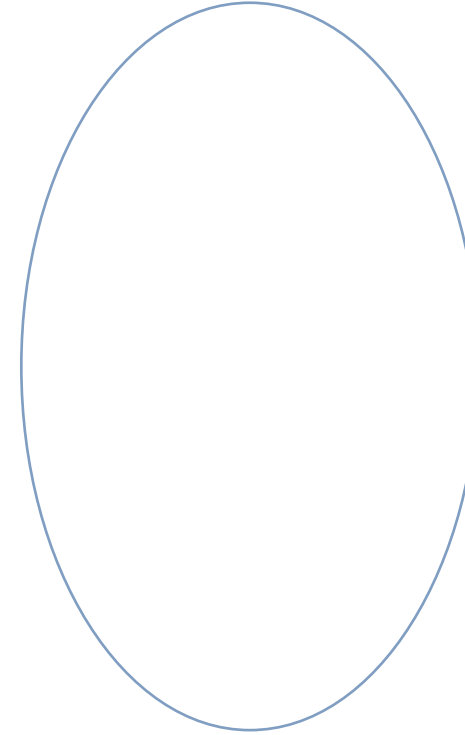
|    |   |   |   |   |   |   |   |   |   |   |   |   |   |
|----|---|---|---|---|---|---|---|---|---|---|---|---|---|
| K= | H | A | M | H | A | M | H | A | M | H | A | M | H |
| M= | T | O | B | E | O | R | N | O | T | T | O | B | E |
| C= |   | O | N |   | O | D |   | O | F |   | O | N |   |



H



A



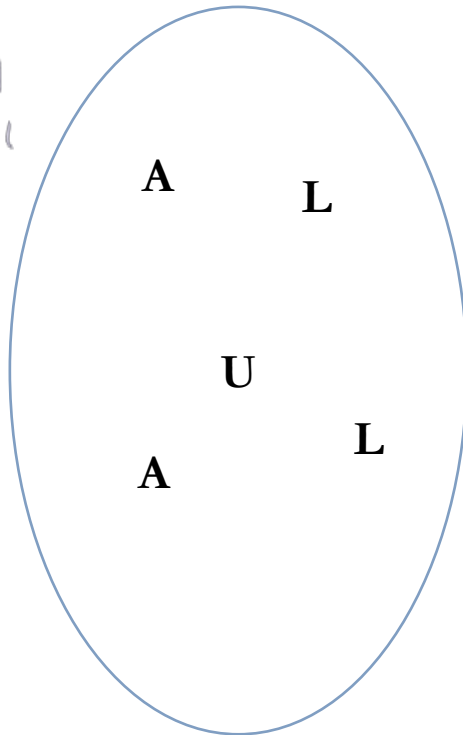
M



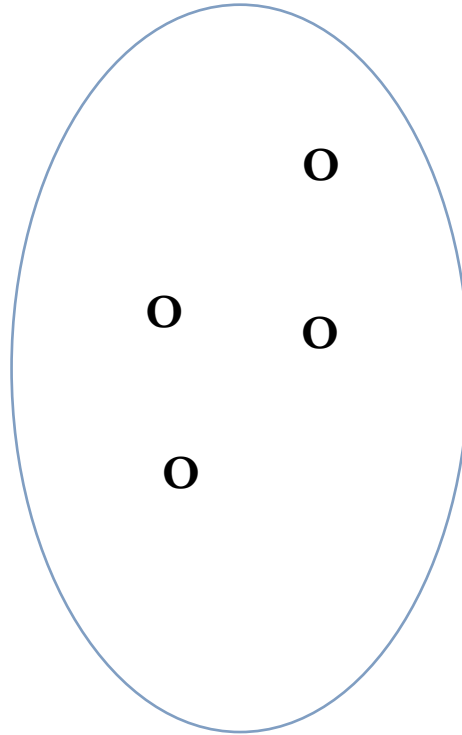


# Cryptanalysis Process

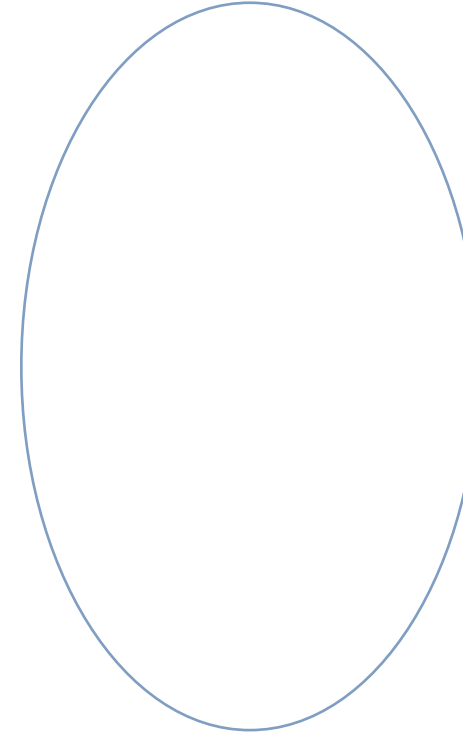
|    |   |   |   |   |   |   |   |   |   |   |   |   |   |
|----|---|---|---|---|---|---|---|---|---|---|---|---|---|
| K= | H | A | M | H | A | M | H | A | M | H | A | M | H |
| M= | T | O | B | E | O | R | N | O | T | T | O | B | E |
| C= |   |   | N |   |   | D |   |   | F |   |   | N |   |



H



A



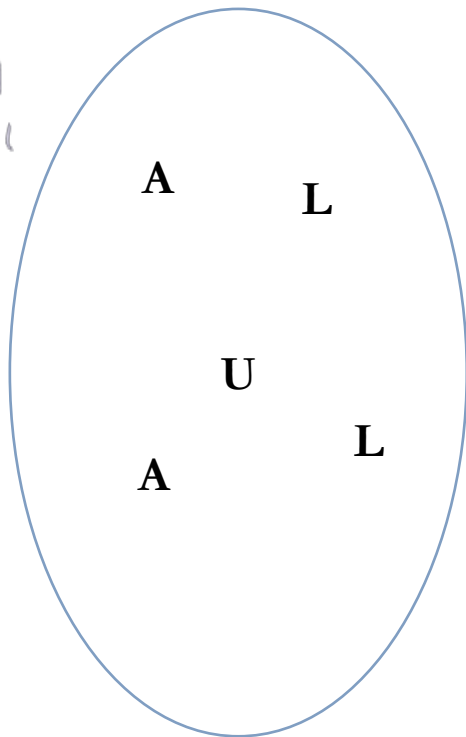
M



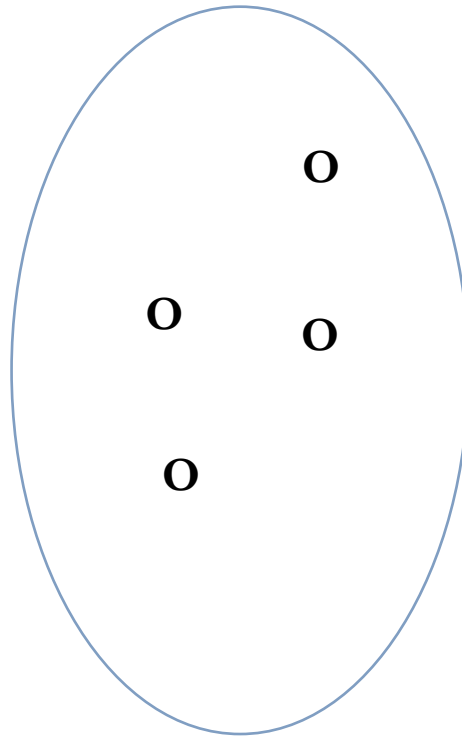


# Cryptanalysis Process

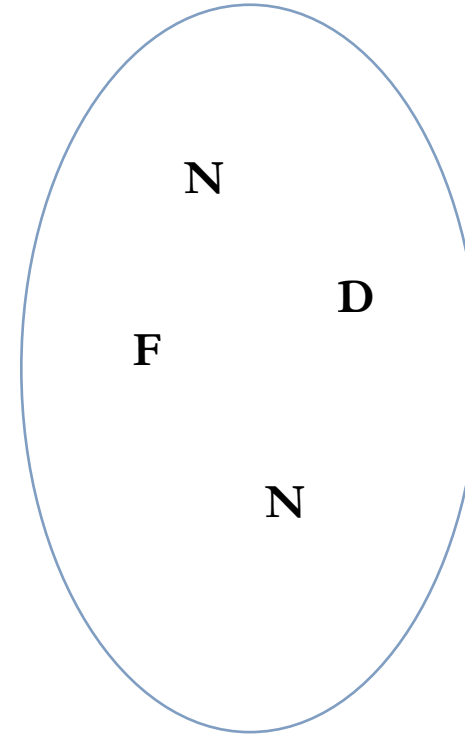
|    |   |   |   |   |   |   |   |   |   |   |   |   |   |
|----|---|---|---|---|---|---|---|---|---|---|---|---|---|
| K= | H | A | M | H | A | M | H | A | M | H | A | M | H |
| M= | T | O | B | E | O | R | N | O | T | T | O | B | E |
| C= |   |   |   |   |   |   |   |   |   |   |   |   |   |



H



A



M





# Kasiski Method

# Kasiski Method

The Kasiski method was introduced in 1863 by the Prussian military officer Friedrich W. Kasiski. The method analysis repetitions in the ciphertext to determine the period.

For example, consider the plaintext TO BE OR NOT TO BE enciphered with a Vigenere cipher with key HAM:

|    |   |   |   |   |   |   |   |   |   |   |   |   |   |
|----|---|---|---|---|---|---|---|---|---|---|---|---|---|
| K= | H | A | M | H | A | M | H | A | M | H | A | M | H |
| M= | T | O | B | E | O | R | N | O | T | T | O | B | E |
| C= | A | O | N | L | O | D | U | O | F | A | O | N | L |

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|    |   |   |   |   |   |   |   |   |   |   |   |   |   |
|----|---|---|---|---|---|---|---|---|---|---|---|---|---|
| K= | H | A | M | H | A | M | H | A | M | H | A | M | H |
| M= | T | O | B | E | O | R | N | O | T | T | O | B | E |
| C= | A | O | N | L | O | D | U | O | F | A | O | N | L |

9

The ciphertext contains two occurrences of the sequence AONL 9 characters apart, and the period could be 1,3 or 9 (we know it's 3).

Repetitions in the ciphertext more than two characters long are unlikely to occur by chance. They occur when the plaintext pattern repeats at a distance equal to a multiple of the period.

# Kasiski Method

If there are  $m$  ciphertext repetitions that occur at intervals  $I_j$  ( $1 \leq j \leq m$ ) the period is likely to be some number that divides most of the  $m$  intervals.

We shall use IC and Kasiski method to analyze the following ciphertext.

|               |       |               |              |               |       |       |       |              |              |
|---------------|-------|---------------|--------------|---------------|-------|-------|-------|--------------|--------------|
| ZHIME         | ZVELK | OJUBW         | CEYIN        | CUSML         | RAVSR | YARNH | CEARI | UTPGP        | VARDU        |
| QZCGR         | NNCAW | JALUH         | GJPJR        | YGEGQ         | FULUS | QFFPV | EYEDQ | <u>GOLKA</u> | <u>LVOSJ</u> |
| TFRTR         | YEJZS | RVNCI         | HYJNM        | ZDCRO         | DKHCR | MMLNR | FFLFN | <u>QGOLK</u> | <u>ALVOS</u> |
| <u>J</u> WMIK | QKUBP | SAYOJ         | RRQYI        | NRNYC         | YQZSY | EDNCA | LEILX | RCHUG        | IEBKO        |
| YTHGV         | VCKHC | JE <u>QGO</u> | <u>LKALV</u> | <u>OSJ</u> ED | WEAKS | GJHYC | LLFTY | IGSVT        | FVPMZ        |
| NRZOL         | CYUZS | FKOQR         | YRTAR        | ZFGKI         | QKRSV | IRCEY | USKVT | MKHCR        | MYQIL        |
| XRCRL         | GQARZ | OLKHY         | KSNFN        | RRNCZ         | TWUOC | JNMKC | MDEZP | IRJEJ        | W            |

When we calculate the frequency distribution, we will find that the  $IC=0.04343$ ,  $n=346$

$$k = \frac{0.0265 \cdot 346}{(0.065 - 0.04343) + 346(0.04343 - 0.03846)} = 5.2659$$

The IC indicates that this is a polyalphabetic cipher with a period of about 5.

Example 1

# Kasiski Method

If there are  $m$  ciphertext repetitions that occur at intervals  $I_j$  ( $1 \leq j \leq m$ ) the period is likely to be some number that divides most of the  $m$  intervals.

We shall use IC and Kasiski method to analyze the following ciphertext.

|               |       |               |              |               |       |       |       |              |              |
|---------------|-------|---------------|--------------|---------------|-------|-------|-------|--------------|--------------|
| ZHYME         | ZVELK | OJUBW         | CEYIN        | CUSML         | RAVSR | YARNH | CEARI | UTPGP        | VARDU        |
| QZCGR         | NNCAW | JALUH         | GJPJR        | YGEGQ         | FULUS | QFFPV | EYEDQ | <u>GOLKA</u> | <u>LVOSJ</u> |
| TFRTR         | YEJZS | RVNCI         | HYJNM        | ZDCRO         | DKHCR | MMLNR | FFLFN | <u>QGOLK</u> | <u>ALVOS</u> |
| <u>J</u> WMIK | QKUBP | SAYOJ         | RRQYI        | NRNYC         | YQZSY | EDNCA | LEILX | RCHUG        | IEBKO        |
| YTHGV         | VCKHC | JE <u>QGO</u> | <u>LKALV</u> | <u>OSJ</u> ED | WEAKS | GJHYC | LLFTY | IGSVT        | FVPMZ        |
| NRZOL         | CYUZS | FKOQR         | YRTAR        | ZFGKI         | QKRSV | IRCEY | USKVT | MKHCR        | MYQIL        |
| XRCRL         | GQARZ | OLKHY         | KSNFN        | RRNCZ         | TWUOC | JNMKC | MDEZP | IRJEJ        | W            |

We observe that there are 3 occurrences of the sequence QGOLKALVOSJ, the first two occurrences are separated by **51** and the last two by **72** characters (start to start); the only common divisor of 51 and 72 is **3** - the **period is almost certainly 3**.

Example 1

# Kasiski Method

When we calculate the **IC** of some ciphertext, we find that **k=9.34**. Also we observe that there is **NYX** appearance many times in the ciphertext and the distance between them are **30, 50, 90, 110**, and **33**.

$$30=2 \times 3 \times 5$$

$$50=2 \times 5 \times 5$$

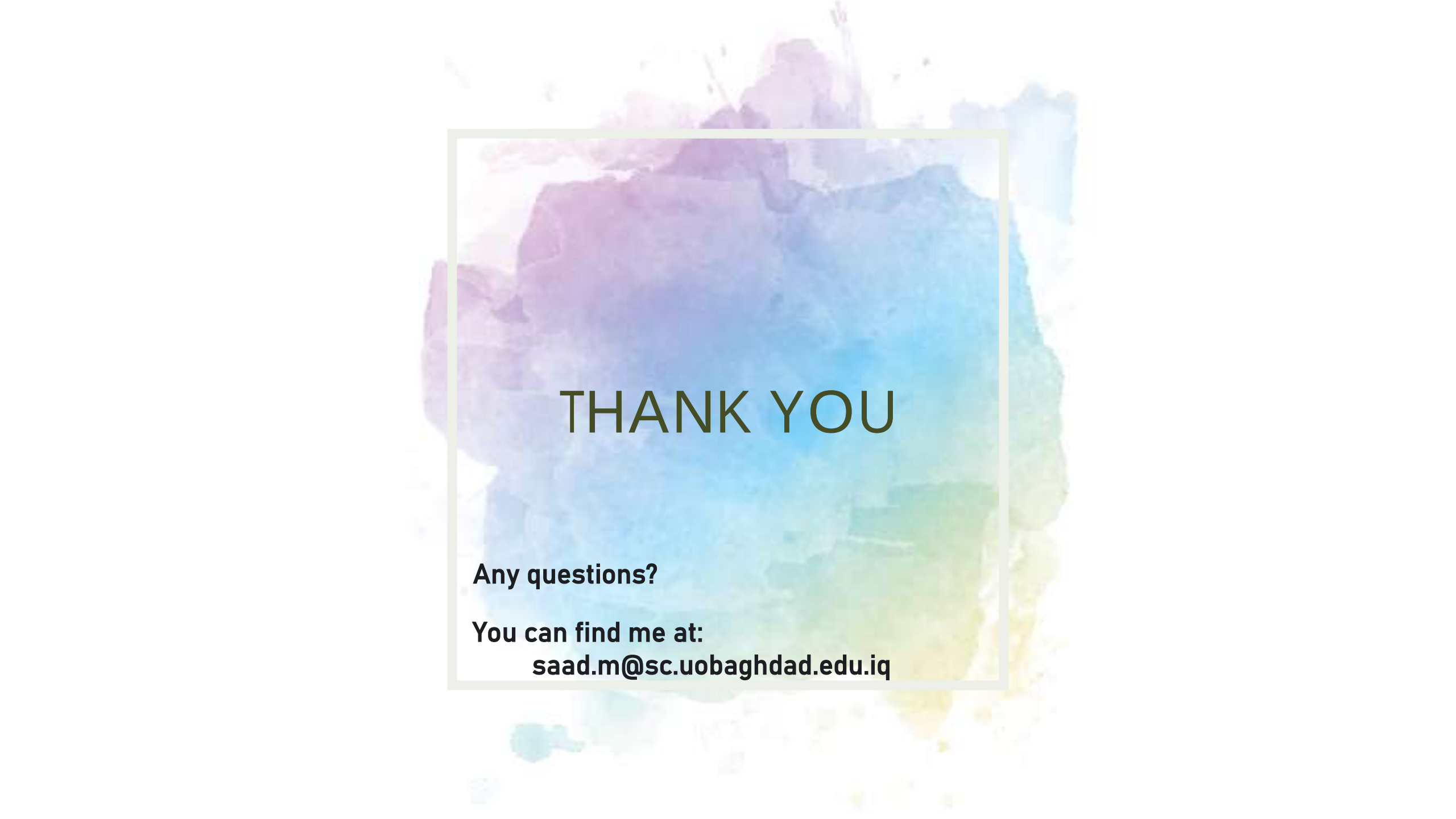
$$90=2 \times 3 \times 3 \times 5$$

$$110=2 \times 5 \times 11$$

$$33=3 \times 11$$

- There are a number of candidates for key length.
- 2 and 5 are popular factors among these distance followed by 3 and 11.
- Note that all but 33 have  $2 \times 5 = 10$  as a factor.
- The cryptanalyst might then disregard 33 as a pure coincidence.
- Discard that data in favor of conjecture that the key length is a multiple of 2 and/or 5.
- Combining this with data from the Friedman test that the key approximately 9 letters long, the cryptanalyst guesses that the key is 10 letters long, and not 2 or 5 letters long.

Example 2

A large, abstract watercolor splash in shades of purple, blue, and green serves as the background for the slide. A thin, light green rectangular border frames the central text area.

# THANK YOU

**Any questions?**

**You can find me at:**

**[saad.m@sc.uobaghdad.edu.iq](mailto:saad.m@sc.uobaghdad.edu.iq)**

Saad Al-Momen

# Practical Security

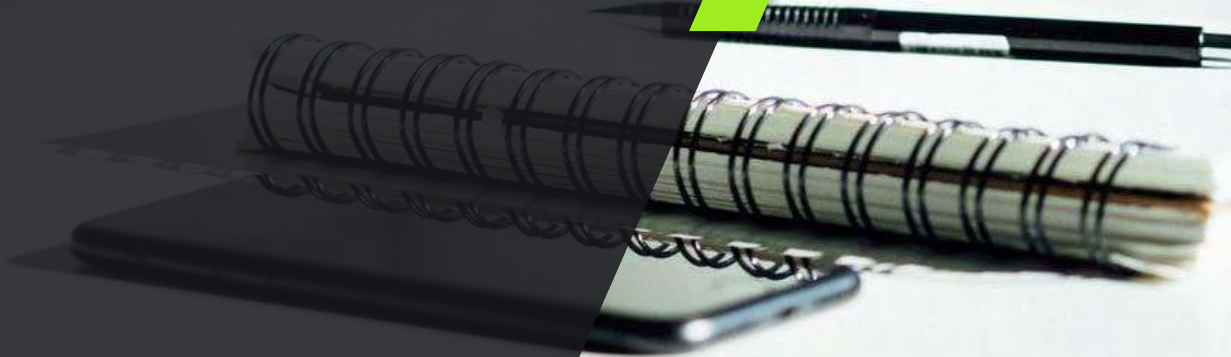
**CIPHER SYSTEMS**

**Fourth Class**  
**Department of Mathematics**  
**College of Science - University of Baghdad**

**7.**



# Introduction



The discussion of chapter one arise a certain **weakness of Monoalphabetic** cipher, the encipherment of a letter only involves using a small portion of the letters of key, exactly the one letter which is substituted for it. Then we can break this cipher system by **finding small portion of the message** and try to decipher them and by using these small portions we can find the way to decipher the overall message.

To make the system more secure, it seems desirable to use a considerable amount of keys to encipher each character of the message. And also it is probably helpful to **'spread' the statistical structure** of the ciphertext by enciphering a number of message characters simultaneously.



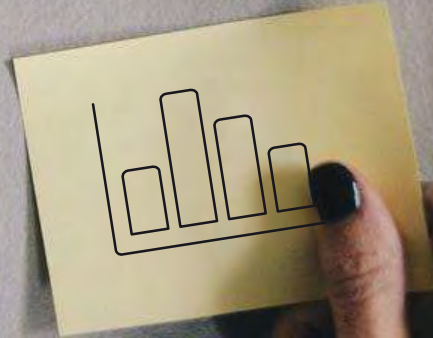
# Diffusion & Confusion

# Diffusion & Confusion.

In order to

- accommodate the points of using a considerable amount of key
- spread the statistical structure of ciphertext, and reduce the effectiveness of statistical attacks on ciphertext

Shannon suggests that the cryptographer uses two techniques which he calls **Diffusion** and **Confusion**.



The idea of diffusion is to spread the statistics of the message space into a statistical structure, which involves long combinations of the letter in the ciphertext.

To understand the idea of diffusion assume  $M = m_1 m_2 \dots$ , then we pick an integer  $s$  and replace  $m$  by the sequence  $y_1 y_2 \dots$  where

$$y_n = \sum_{i=0}^{s-1} m_{n+i} \bmod 26$$

Where  $n=1, 2, 3, \dots$ . By doing this we'll get the message space with letter frequencies of the new message space  $Y$  will become more equal than in  $M$ .

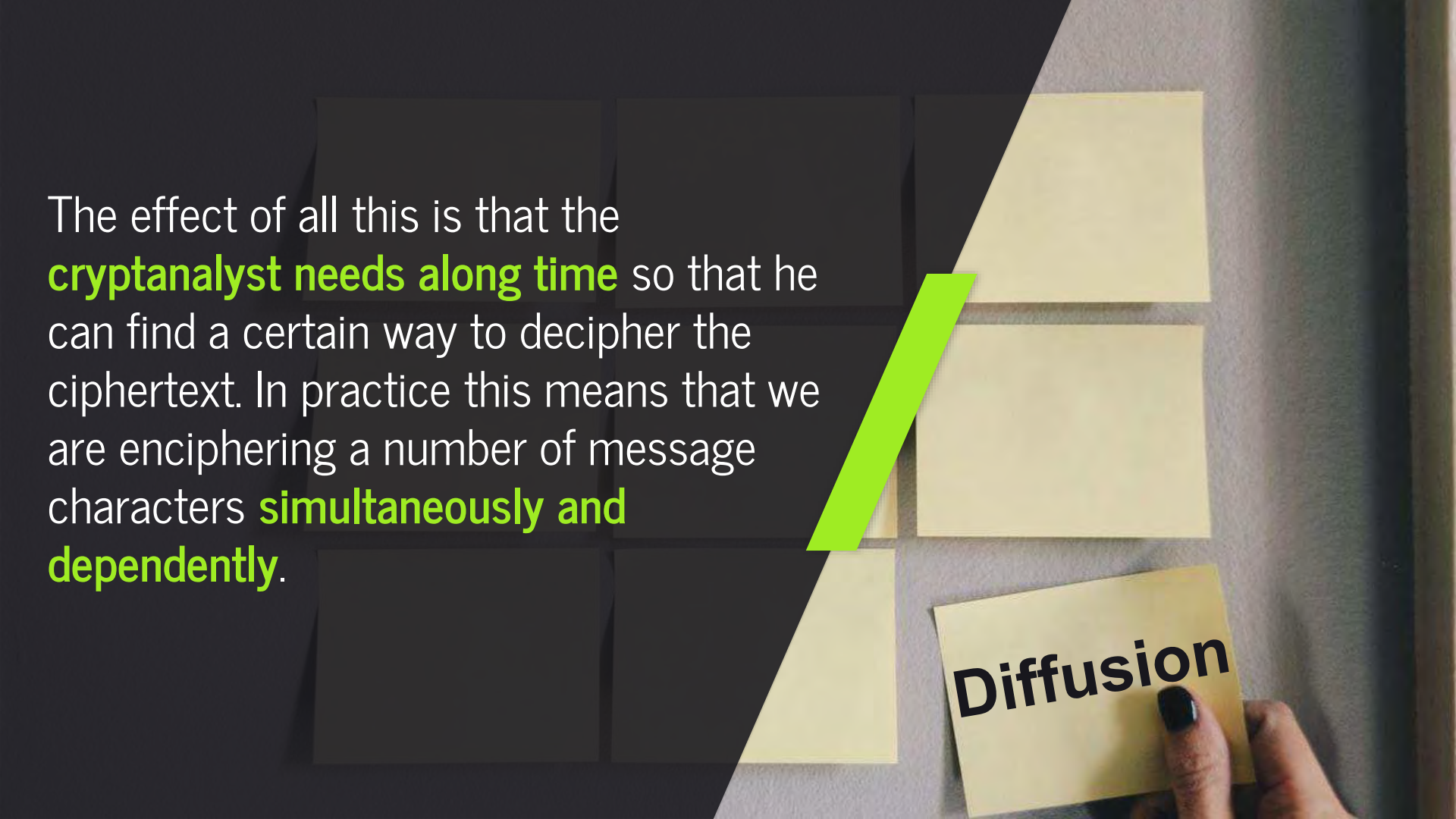
$$Y_1 = m_1 + m_2 + m_3$$

$$Y_2 = m_2 + m_3 + m_4$$

$$Y_3 = m_3 + m_4 + m_5$$

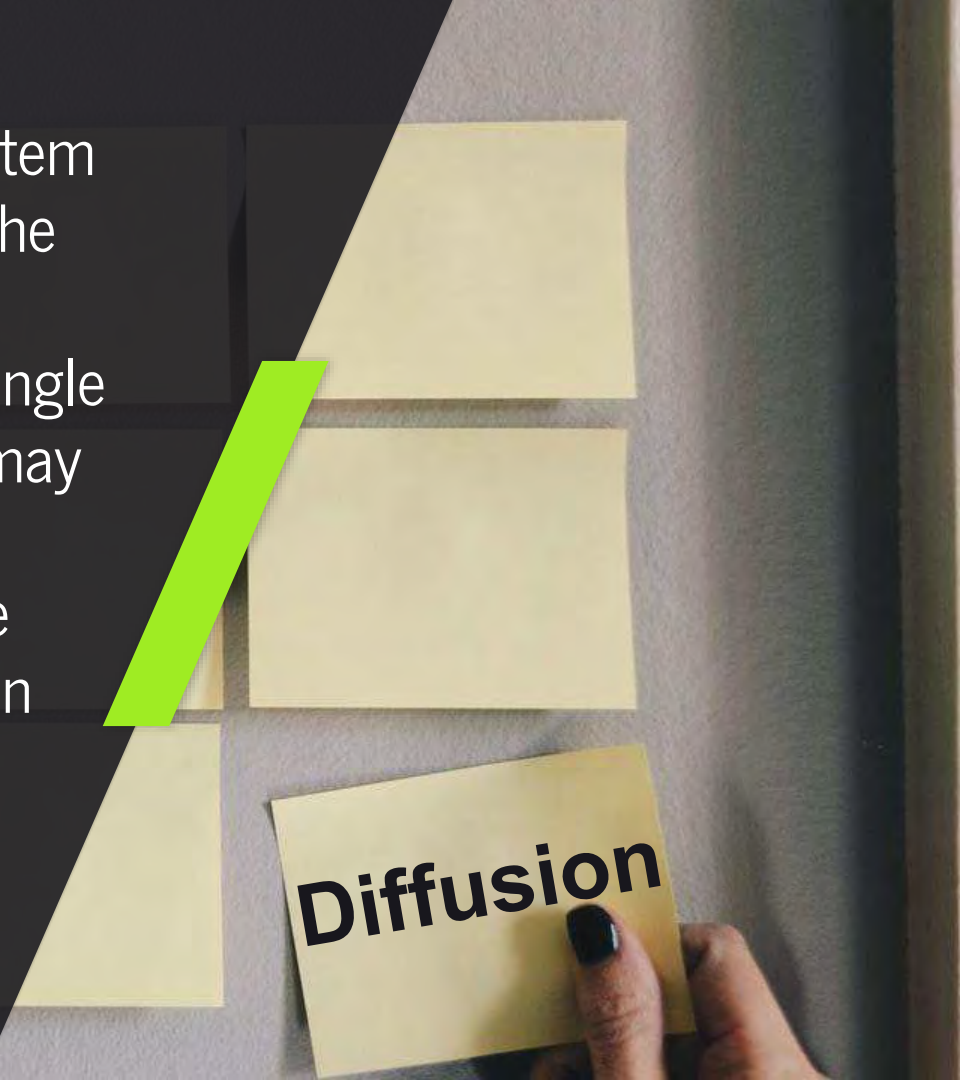
**Diffusion**

The effect of all this is that the **cryptanalyst needs along time** so that he can find a certain way to decipher the ciphertext. In practice this means that we are enciphering a number of message characters **simultaneously and dependently**.



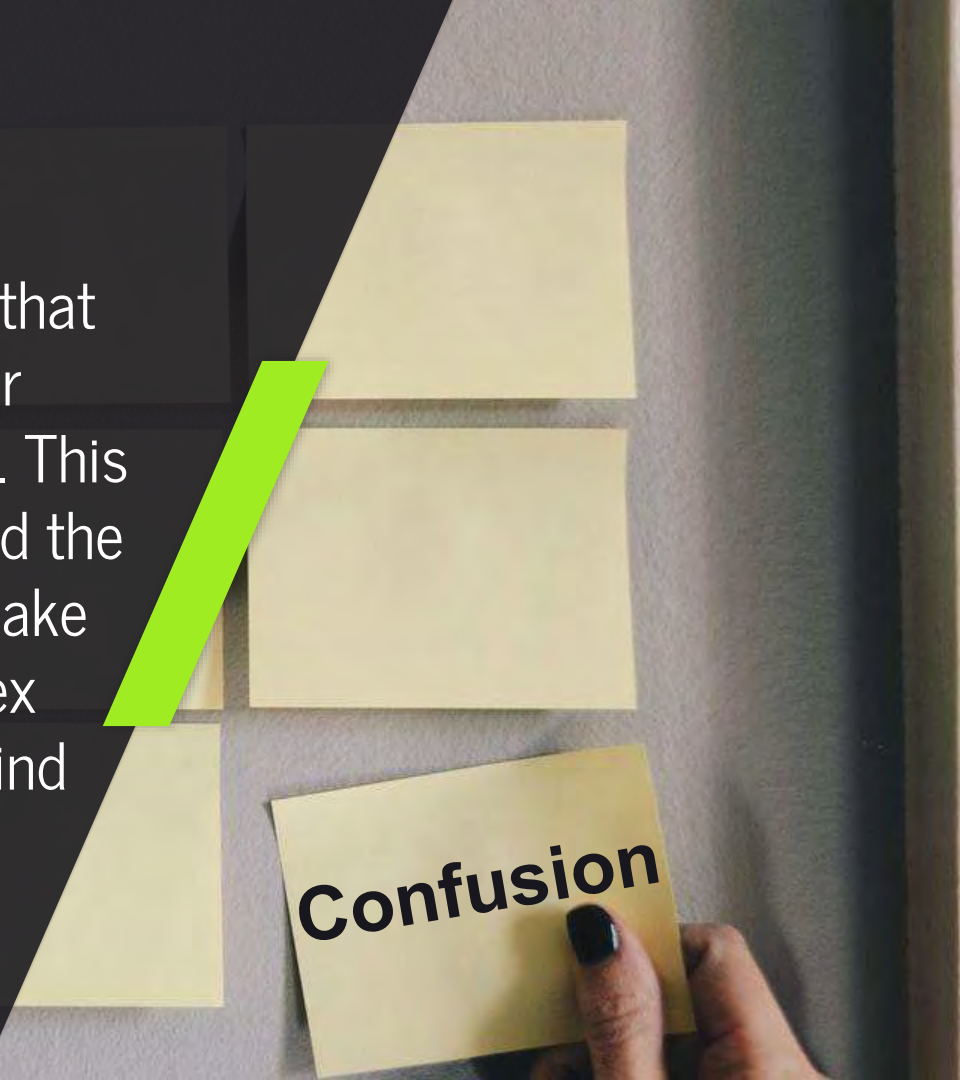
Diffusion

The **disadvantage** of this type of system is that, at the receiver, each part of the message **depends on a number of ciphertext characters**. Thus, if one single ciphertext is error transmitted, this may cause many errors in the received message. This diffusing effect of one error in transmission causing many in decipherment is usually called **error propagation**.

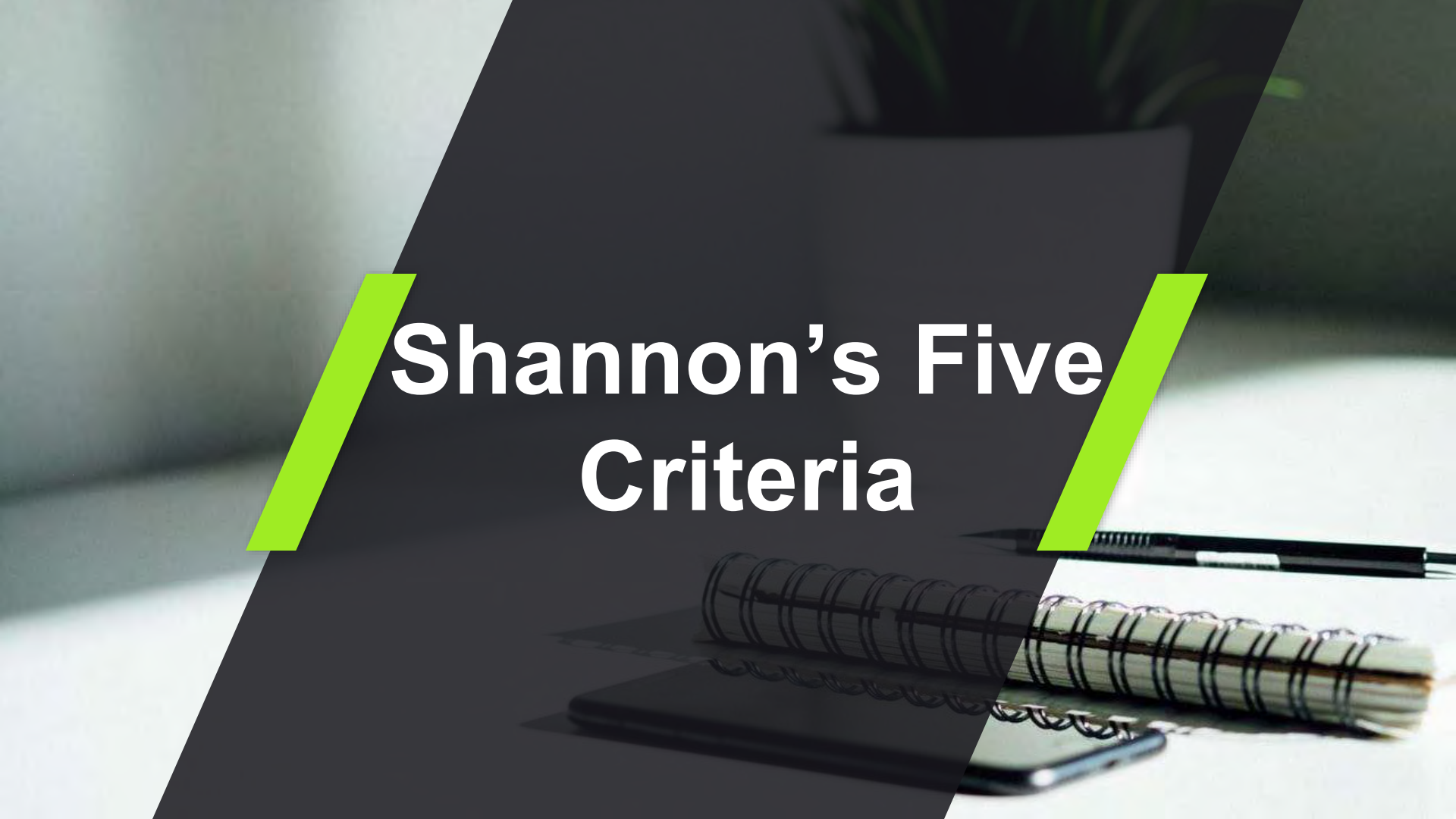


**Diffusion**

The idea of **confusion** is to **hide any relationship between the plaintext, ciphertext and the key**. This implies that the message characters will encipher depending on virtually the entire key. This idea will force the cryptanalyst to find the whole key simultaneously and will make him solve considerably more complex equation than when he was able to find the key piece by piece.



**Confusion**



# Shannon's Five Criteria

Shannon suggests five important criteria to evaluate the cipher systems, which are:

It is clear that any system has a higher security will be superior than any other system. If the system theoretically can be broken, it might, practically impossible to do so; because there might not be a certain way to analyze the code so that an intruder can't take the original plaintext from the ciphertext.

**The amount of  
secrecy offered**

Some of cipher systems generate a key space i.e. it take all the possibilities of the keys that may solve the problem.

**The size of the  
key**

**2**

A good cipher system has to have a simple encipher and decipher algorithms but the analysis of the key has to be a very complicated one;

i.e. the time taken to encipher and decipher the message must be a polynomial time while the time taken by the cryptanalyst to break the message must be an exponential time.

**The simplicity of the enciphering and deciphering operations**

In many ciphering systems, the error might be propagate and damage or garbled the information, hence we have cut this propagation of errors

## **The propagation of errors**

If the message being a very long, it might be broken, hence the cipher system has to be unbreakable in spite of the message is long.

## **Extension of the message**



# Concept of Randomness

Let  $S = s_0, s_1, s_2, \dots$  be an **infinite sequence**. The subsequence consisting of the first  $n$  terms of  $s$  is denoted by  $S^n = s_0, s_1, \dots, s_{n-1}$ .

**Example:**

$S = \text{afrsgwfsvdsw}\dots$

$S^5 = \text{afrsg}$

$S^7 = \text{afrsgwf}$

Let  $S = s_0, s_1, s_2, \dots$  be an infinite sequence. The subsequence consisting of the first  $n$  terms of  $s$  is denoted by  $S^n = s_0, s_1, \dots, s_n$ .

**Example:**

$S = 0110101100101\dots$

$S^3 = 011$

$S^6 = 011010$

The sequence  $s = s_0, s_1, s_2, \dots$  is said to be *N-periodic* if  $s_i = s_{i+N}$  for all  $i \geq 0$ .

1001010010100101001010...

Periodic  
Sequences

The sequence  $s = s_0, s_1, s_2, \dots$  is said to be *N-periodic* if  $s_i = s_{i+N}$  for all  $i \geq 0$ .

5-periodic      period=5

1001010010100101001010...

The sequence  $s$  is *periodic* if it is  $N$ -periodic for some positive integer  $N$ .

The *period* of a periodic sequence  $s$  is the smallest positive integer  $N$  for which  $s$  is  $N$ -periodic.

Periodic  
Sequences

The sequence  $s = s_0, s_1, s_2, \dots$  is said to be *N-periodic* if  $s_i = s_{i+N}$  for all  $i \geq 0$ .

5-periodic      period=5

1001010010100101001010...

If  $s$  is a periodic sequence of period  $N$ , then the *cycle* of  $s$  is the subsequence  $s^N$ .

10010

Periodic  
Sequences

110110010001000011

Run

11 0 11 00 1 000 1 0000 11

Gap

11 0 11 00 1 000 1 0000 11

Block

11 0 11 00 1 000 1 0000 11

Run , Gap & Block

$$C(t) = \frac{1}{N} \sum_{i=0}^{N-1} (2s_i - 1) \cdot (2s_{i+t} - 1), \text{ for } 0 \leq t \leq N - 1.$$

Example:

Consider the following sequence: 01011010110101101011

As we see  $N=5$ ,  $s^N=01011$

$S_0 = 0 \ 1 \ 0 \ 1 \ 1$   
 $S_1 = 1 \ 0 \ 1 \ 1 \ 0$   
 $S_2 = 0 \ 1 \ 1 \ 0 \ 1$   
 $S_3 = 1 \ 1 \ 0 \ 1 \ 0$   
 $S_4 = 1 \ 0 \ 1 \ 0 \ 1$

**Autocorrelation**  
function

$$C(t) = \frac{1}{N} \sum_{i=0}^{N-1} (2s_i - 1) \cdot (2s_{i+t} - 1), \text{ for } 0 \leq t \leq N - 1.$$

$$c(t) = \frac{1}{5} \sum_{i=0}^4 (2s_i - 1)(2s_{i+t} - 1)$$

$$c(t) = \frac{1}{5} [(2s_0 - 1)(2s_{0+t} - 1) + (2s_1 - 1)(2s_{1+t} - 1) + \\ (2s_2 - 1)(2s_{2+t} - 1) + (2s_3 - 1)(2s_{3+t} - 1) + \\ (2s_4 - 1)(2s_{4+t} - 1)]$$

$$C(t) = \frac{A - D}{N}, \quad 0 \leq t \leq N - 1$$

**Autocorrelation  
function**

$$C(t) = \frac{1}{N} \sum_{i=0}^{N-1} (2s_i - 1) \cdot (2s_{i+t} - 1), \text{ for } 0 \leq t \leq N - 1.$$

Example:

Consider the following sequence: 01011010110101101011

As we see  $N=5$ ,  $s^N=01011$

$S_0 = 0 \ 1 \ 0 \ 1 \ 1$

$S_1 = 1 \ 0 \ 1 \ 1 \ 0$

$S_2 = 0 \ 1 \ 1 \ 0 \ 1$

$S_3 = 1 \ 1 \ 0 \ 1 \ 0$

$S_4 = 1 \ 0 \ 1 \ 0 \ 1$

(1)

$S = 0 \ 1 \ 0 \ 1 \ 1$

$S_0 = 0 \ 1 \ 0 \ 1 \ 1$

$A=5, D=0$

$$\Rightarrow c(0) = \frac{5-0}{5} = 1$$

Autocorrelation  
function

$$C(t) = \frac{1}{N} \sum_{i=0}^{N-1} (2s_i - 1) \cdot (2s_{i+t} - 1), \text{ for } 0 \leq t \leq N - 1.$$

Example:

Consider the following sequence: 01011010110101101011

As we see  $N=5$ ,  $s^N=01011$

$S_0 = 0 \ 1 \ 0 \ 1 \ 1$

$S_1 = 1 \ 0 \ 1 \ 1 \ 0$

$S_2 = 0 \ 1 \ 1 \ 0 \ 1$

$S_3 = 1 \ 1 \ 0 \ 1 \ 0$

$S_4 = 1 \ 0 \ 1 \ 0 \ 1$

(2)

$S = 0 \ 1 \ 0 \ 1 \ 1$

$S_1 = 1 \ 0 \ 1 \ 1 \ 0$

$A=1, D=4$

$$\Rightarrow c(1) = \frac{1-4}{5} = -\frac{3}{5}$$

Autocorrelation  
function

$$C(t) = \frac{1}{N} \sum_{i=0}^{N-1} (2s_i - 1) \cdot (2s_{i+t} - 1), \text{ for } 0 \leq t \leq N - 1.$$

Example:

Consider the following sequence: 01011010110101101011

As we see  $N=5$ ,  $s^N=01011$

$S_0 = 0 \ 1 \ 0 \ 1 \ 1$

$S_1 = 1 \ 0 \ 1 \ 1 \ 0$

$S_2 = 0 \ 1 \ 1 \ 0 \ 1$

$S_3 = 1 \ 1 \ 0 \ 1 \ 0$

$S_4 = 1 \ 0 \ 1 \ 0 \ 1$

(3)

$S = 0 \ 1 \ 0 \ 1 \ 1$

$S_2 = 0 \ 1 \ 1 \ 0 \ 1$

$A=3, D=2$

$$\Rightarrow c(2) = \frac{3-2}{5} = \frac{1}{5}$$

Autocorrelation  
function

$$C(t) = \frac{1}{N} \sum_{i=0}^{N-1} (2s_i - 1) \cdot (2s_{i+t} - 1), \text{ for } 0 \leq t \leq N - 1.$$

Example:

Consider the following sequence: 01011010110101101011

As we see  $N=5$ ,  $s^N=01011$

$S_0 = 0 \ 1 \ 0 \ 1 \ 1$

$S_1 = 1 \ 0 \ 1 \ 1 \ 0$

$S_2 = 0 \ 1 \ 1 \ 0 \ 1$

$S_3 = 1 \ 1 \ 0 \ 1 \ 0$

$S_4 = 1 \ 0 \ 1 \ 0 \ 1$

(4)

$S = 0 \ 1 \ 0 \ 1 \ 1$

$S_3 = 1 \ 1 \ 0 \ 1 \ 0$

$A=3, D=2$

$$\Rightarrow c(3) = \frac{3-2}{5} = \frac{1}{5}$$

**Autocorrelation  
function**

$$C(t) = \frac{1}{N} \sum_{i=0}^{N-1} (2s_i - 1) \cdot (2s_{i+t} - 1), \text{ for } 0 \leq t \leq N - 1.$$

Example:

Consider the following sequence: 01011010110101101011

As we see  $N=5$ ,  $s^N=01011$

$S_0 = 0 \ 1 \ 0 \ 1 \ 1$

$S_1 = 1 \ 0 \ 1 \ 1 \ 0$

$S_2 = 0 \ 1 \ 1 \ 0 \ 1$

$S_3 = 1 \ 1 \ 0 \ 1 \ 0$

$S_4 = 1 \ 0 \ 1 \ 0 \ 1$

(5)

$S = 0 \ 1 \ 0 \ 1 \ 1$

$S_4 = 1 \ 0 \ 1 \ 0 \ 1$

$A=1, D=4$

$$\Rightarrow c(4) = \frac{1-4}{5} = -\frac{3}{5}$$

**Autocorrelation  
function**

The background of the slide features a photograph of a minimalist desk setup. On the right, a white desk lamp with a gold-colored adjustable arm and a white spherical base is visible. Next to it is a small green plant in a white ceramic pot. In the upper center, a round analog clock with a dark face and gold hands is partially visible. The entire scene is overlaid with a large, dark gray diagonal shape that runs from the top-left towards the bottom-right. Two bright green diagonal bars are positioned on either side of the central text, creating a frame-like effect.

# **Golomb's Randomness Postulates**

Let  $s$  be a periodic sequence of period  $N$ . *Golomb's randomness postulates* are the following.

**R1**

In the cycle  $s^N$  of  $s$ , the number of 1's differs from the number of 0's by at most 1. In other word if  $N$  is an even number then the number of 1's and 0's are equal, while if  $N$  is an odd number, then the number of 1's either more by one or less by one than the number of 0's.

For example

if the length of the sequence is 80 then  
no. of 1: 40 and no. of 0: 40

if the length of the sequence is 81 then

Either: no. of 1: 40 and no. of 0: 41  
Or: no. of 1: 41 and no. of 0: 40

Let  $s$  be a periodic sequence of period  $N$ . *Golomb's randomness postulates* are the following.

**R<sub>2</sub>**

In the cycle  $s^N$ , at least half the runs have length 1, at least one-fourth have length 2, at least one-eighth have length 3, in general, at least  $1/2^i$  have length  $i$ . Moreover, for each of these lengths, there are (almost) equally many gaps and blocks.

| Length of Run | Quantity             |
|---------------|----------------------|
| 1             | $\frac{1}{2}$ Runs   |
| 2             | $\frac{1}{4}$ Runs   |
| 3             | $\frac{1}{8}$ Runs   |
| $\vdots$      | $\vdots$             |
| $n$           | $\frac{1}{2^n}$ Runs |

Let  $s$  be a periodic sequence of period  $N$ . *Golomb's randomness postulates* are the following.

**R3**

The autocorrelation function  $C(t)$  is two-valued. That is for some integer  $K$ ,

$$N \cdot C(t) = \sum_{i=0}^{N-1} (2s_i - 1) \cdot (2s_{i+t} - 1) = \begin{cases} N, & \text{if } t = 0, \\ K, & \text{if } 1 \leq t \leq N-1. \end{cases}$$

A binary sequence which satisfies Golomb's randomness postulates is called a **pseudo-noise sequence** or a **pn-sequence**.

Golomb's randomness postulates are **necessary** conditions for a periodic pseudo random sequence to look random, but they are not **sufficient**.



Consider the periodic sequence  $s$  of period  $N = 15$  with cycle

$$s^{15} = 0 \ 1 \ 1 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1 \ 1 \ 1 \ 0 \ 1$$

The following shows that the sequence  $s$  satisfies Golomb's randomness postulates.

**Example**  
pn-sequence

Consider the periodic sequence  $s$  of period  $N = 15$  with cycle

$$s^{15} = 0 \ 1 \ 1 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1 \ 1 \ 1 \ 0 \ 1$$

The following shows that the sequence  $s$  satisfies Golomb's randomness postulates.

R1: The number of 0's in  $s^{15}$  is 7, while the number of 1's is 8.

Example  
pn-sequence

Consider the periodic sequence  $s$  of period  $N = 15$  with cycle

$$s^{15} = 0 \ 1 \ 1 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1 \ 1 \ 1 \ 0 \ 1$$


The following shows that the sequence  $s$  satisfies Golomb's randomness postulates.

R2:  $s^{15}$  has 8 runs. There are 4 runs of length 1 (2 gaps and 2 blocks), 2 runs of length 2 (1 gap and 1 block), 1 run of length 3 (1 gap), and 1 run of length 4 (1 block).

Example  
pn-sequence

Consider the periodic sequence  $s$  of period  $N = 15$  with cycle

$s^{15} = \underline{0} \ 1 \ 1 \ 0 \ 0 \ \underline{1} \ 0 \ 0 \ 0 \ 1 \ 1 \ 1 \ 1 \ \underline{0} \ \underline{1}$

The following shows that the sequence  $s$  satisfies Golomb's randomness postulates.

R2:  $s^{15}$  has 8 runs. There are 4 runs of length 1 (2 gaps and 2 blocks), 2 runs of length 2 (1 gap and 1 block), 1 run of length 3 (1 gap), and 1 run of length 4 (1 block).

Example  
pn-sequence

Consider the periodic sequence  $s$  of period  $N = 15$  with cycle

$$s^{15} = 0 \quad \underline{1} \quad \underline{1} \quad \underline{0} \quad \underline{0} \quad 1 \quad 0 \quad 0 \quad 0 \quad 1 \quad 1 \quad 1 \quad 1 \quad 0 \quad 1$$

The following shows that the sequence  $s$  satisfies Golomb's randomness postulates.

R2:  $s^{15}$  has 8 runs. There are 4 runs of length 1 (2 gaps and 2 blocks), 2 runs of length 2 (1 gap and 1 block), 1 run of length 3 (1 gap), and 1 run of length 4 (1 block).

Example  
pn-sequence

Consider the periodic sequence  $s$  of period  $N = 15$  with cycle

$$s^{15} = 0 \ 1 \ 1 \ 0 \ 0 \ 1 \ \underline{0 \ 0 \ 0} \ 1 \ 1 \ 1 \ 1 \ 0 \ 1$$

The following shows that the sequence  $s$  satisfies Golomb's randomness postulates.

R2:  $s^{15}$  has 8 runs. There are 4 runs of length 1 (2 gaps and 2 blocks), 2 runs of length 2 (1 gap and 1 block), 1 run of length 3 (1 gap), and 1 run of length 4 (1 block).

Example  
pn-sequence

Consider the periodic sequence  $s$  of period  $N = 15$  with cycle

$$s^{15} = 0 \ 1 \ 1 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ \underline{1 \ 1 \ 1 \ 1} \ 0 \ 1$$

The following shows that the sequence  $s$  satisfies Golomb's randomness postulates.

R2:  $s^{15}$  has 8 runs. There are 4 runs of length 1 (2 gaps and 2 blocks), 2 runs of length 2 (1 gap and 1 block), 1 run of length 3 (1 gap), and 1 run of length 4 (1 block).

Example  
pn-sequence

Consider the periodic sequence  $s$  of period  $N = 15$  with cycle

$$s^{15} = 0 \ 1 \ 1 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1 \ 1 \ 1 \ 0 \ 1$$

The following shows that the sequence  $s$  satisfies Golomb's randomness postulates.

R3: The autocorrelation function  $C(t)$  takes on two values:

$$C(0) = 1 \text{ and} \\ C(t) = -\frac{1}{15} \quad 1 \leq t \leq 14.$$

Hence,  $s$  is a pn-sequence.

**Example**  
pn-sequence



**THANK YOU**

**Any questions?**

**You can find me at:**

**[saad.m@sc.uobaghdad.edu.iq](mailto:saad.m@sc.uobaghdad.edu.iq)**

Saad Al-Momen

# Practical Security

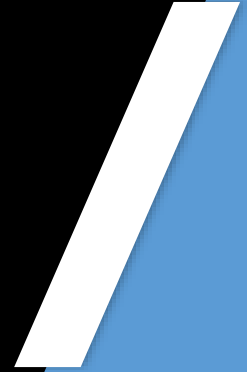
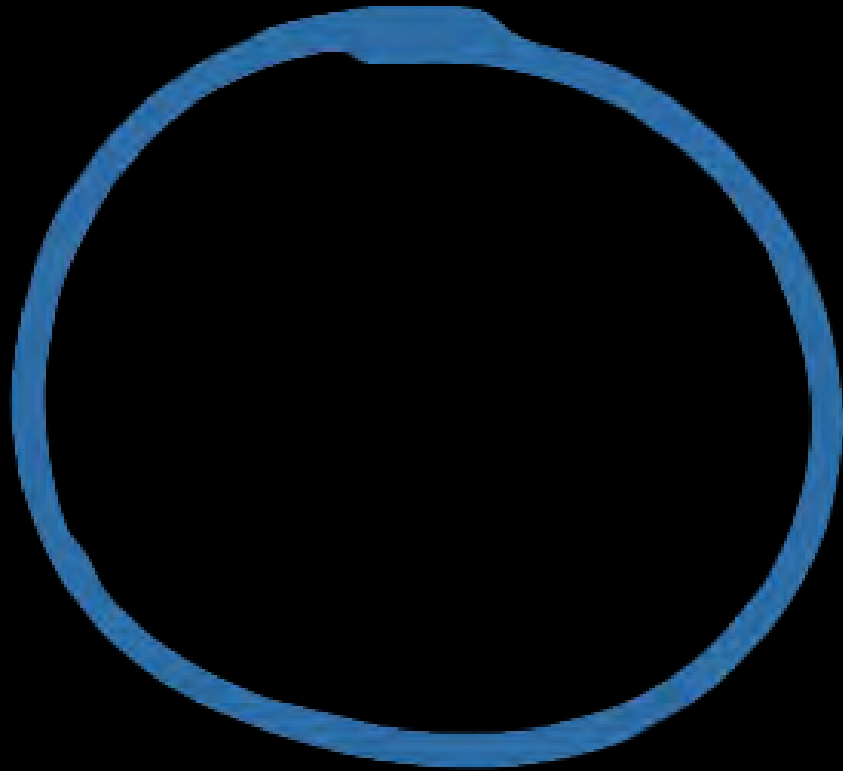
**CIPHER SYSTEMS**

**Fourth Class**  
**Department of Mathematics**  
**College of Science - University of Baghdad**

**8.**



# Statistical Test for Randomness



# Example 1



1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$n=160$

Example 1



# Frequency Test

# Frequency Test

1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$n_0=84$     $n_1=76$

Example 1

# Frequency Test

$$n_0=84 \quad n_1=76 \quad n=160$$

(i) (frequency test)  $n_0=84$ ,  $n_1=76$ , and the value of the statistic  $X_1$  is 0.4.

$$X_1 = \frac{(n_0 - n_1)^2}{n}$$

$$X_1 = \frac{(84 - 76)^2}{160} = 0.4.$$

Example 1

# $\chi^2$ (chi-square) distribution

| $v$ | $\alpha$ |         |         |         |         |         |
|-----|----------|---------|---------|---------|---------|---------|
|     | 0.100    | 0.050   | 0.025   | 0.010   | 0.005   | 0.001   |
| 1   | 2.7055   | 3.8415  | 5.0239  | 6.6349  | 7.8794  | 10.8276 |
| 2   | 4.6052   | 5.9915  | 7.3778  | 9.2103  | 10.5966 | 13.8155 |
| 3   | 6.2514   | 7.8147  | 9.3484  | 11.3449 | 12.8382 | 16.2662 |
| 4   | 7.7794   | 9.4877  | 11.1433 | 13.2767 | 14.8603 | 18.4668 |
| 5   | 9.2364   | 11.0705 | 12.8325 | 15.0863 | 16.7496 | 20.5150 |
| 6   | 10.6446  | 12.5916 | 14.4494 | 16.8119 | 18.5476 | 22.4577 |
| 7   | 12.0170  | 14.0671 | 16.0128 | 18.4753 | 20.2777 | 24.3219 |
| 8   | 13.3616  | 15.5073 | 17.5345 | 20.0902 | 21.9550 | 26.1245 |
| 9   | 14.6837  | 16.9190 | 19.0228 | 21.6660 | 23.5894 | 27.8772 |
| 10  | 15.9872  | 18.3070 | 20.4832 | 23.2093 | 25.1882 | 29.5883 |
| 11  | 17.2750  | 19.6751 | 21.9200 | 24.7250 | 26.7568 | 31.2641 |
| 12  |          |         |         |         |         | 32.9095 |
| 13  |          |         |         |         |         | 34.5659 |
| 14  |          |         |         |         |         | 36.1909 |
| 15  |          |         |         |         |         | 37.7966 |
| 16  | 23.5418  | 26.2962 | 28.8454 | 31.9999 | 34.2672 | 39.2524 |

**Frequency Test: degree of freedom  
 $v=1$**

**Example 1**

# Serial Test

The image features a dark blue, semi-transparent geometric overlay in the shape of a large triangle pointing downwards, which contains the text 'Serial Test' in white. Two parallel blue diagonal lines intersect the sides of this dark shape. The background is a blurred photograph of a desk with a spiral-bound notebook, a black pen, and a smartphone.

## Serial Test

1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$n_0=84$     $n_1=76$

Example 1

## Serial Test

1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$n_0=84$     $n_1=76$

Example 1

## Serial Test

1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$n_0=84$     $n_1=76$

Example 1

## Serial Test

1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$n_0=84$     $n_1=76$

Example 1

## Serial Test

1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$n_0=84$     $n_1=76$

Example 1

## Serial Test

1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$n_0=84$     $n_1=76$

Example 1

## Serial Test

1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$n_0=84$     $n_1=76$

Example 1

## Serial Test

1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$n_0=84$     $n_1=76$

Example 1

## Serial Test

1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$n_0=84$     $n_1=76$

Example 1

## Serial Test

1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$n_0=84$     $n_1=76$

Example 1

## Serial Test

1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$$n_0=84 \quad n_1=76$$

Example 1

## Serial Test

1110001100010001010011101111001001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$$n_{00}=44$$

$$n_0=84 \quad n_1=76$$

Example 1

## Serial Test

111000111000110001010011101111001001001001  
111000111000110001010011101111001001001001  
111000111000110001010011101111001001001001  
111000111000110001010011101111001001001001

$n_{00}=44$ ,  $n_{01}=40$

$n_0=84$      $n_1=76$

Example 1

## Serial Test

1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$n_{00}=44$ ,  $n_{01}=40$ ,  $n_{10}=40$

$n_0=84$      $n_1=76$

Example 1

## Serial Test

11100011000010001010011101111001001001001  
11100011000010001010011101111001001001001  
11100011000010001010011101111001001001001  
11100011000010001010011101111001001001001

$n_{00}=44$ ,  $n_{01}=40$ ,  $n_{10}=40$ ,  $n_{11}=35$

$n_0=84$      $n_1=76$

Example 1

# Serial Test

(ii) (serial test)  $n_{00}=44$ ,  $n_{01}=40$ ,  $n_{10}=40$ ,  $n_{11}=35$ , and the value of the statistic  $X_2$  is 0.6252.

$$\begin{aligned}X_2 &= \frac{4}{n-1} \sum_{i=0}^1 \sum_{j=0}^1 n_{ij}^2 - \frac{2}{n} \sum_{i=0}^1 n_i^2 + 1 \\&= \frac{4}{n-1} (n_{00}^2 + n_{01}^2 + n_{10}^2 + n_{11}^2) - \frac{2}{n} (n_0^2 + n_1^2) + 1 \\&= \frac{4}{159} (44^2 + 40^2 + 40^2 + 35^2) - \frac{2}{160} (84^2 + 76^2) + 1 \\&= \frac{4}{159} (1936 + 1600 + 1600 + 1225) - \frac{2}{160} (7056 + 5776) + 1 \\&= \frac{4}{159} (6361) - \frac{2}{160} (12832) + 1 \\&= 160.0252 - 160.4 + 1 = 0.6252.\end{aligned}$$

# $\chi^2$ (chi-square) distribution

| $v$ | $\alpha$ |         |         |         |         |         |
|-----|----------|---------|---------|---------|---------|---------|
|     | 0.100    | 0.050   | 0.025   | 0.010   | 0.005   | 0.001   |
| 1   | 2.7055   | 3.8415  | 5.0239  | 6.6349  | 7.8794  | 10.8276 |
| 2   | 4.6052   | 5.9915  | 7.3778  | 9.2103  | 10.5966 | 13.8155 |
| 3   | 6.2514   | 7.8147  | 9.3484  | 11.3449 | 12.8382 | 16.2662 |
| 4   | 7.7794   | 9.4877  | 11.1433 | 13.2767 | 14.8603 | 18.4668 |
| 5   | 9.2364   | 11.0705 | 12.8325 | 15.0863 | 16.7496 | 20.5150 |
| 6   | 10.6446  | 12.5916 | 14.4494 | 16.8119 | 18.5476 | 22.4577 |
| 7   | 12.0170  | 14.0671 | 16.0128 | 18.4753 | 20.2777 | 24.3219 |
| 8   | 13.3616  | 15.5073 | 17.5345 | 20.0902 | 21.9550 | 26.1245 |
| 9   | 14.6837  | 16.9190 | 19.0228 | 21.6660 | 23.5894 | 27.8772 |
| 10  | 15.9872  | 18.3070 | 20.4832 | 23.2093 | 25.1882 | 29.5883 |
| 11  | 17.2750  | 19.6751 | 21.9200 | 24.7250 | 26.7568 | 31.2641 |
| 12  |          |         |         |         |         | 32.9095 |
| 13  |          |         |         |         |         | 34.5659 |
| 14  |          |         |         |         |         | 36.1909 |
| 15  |          |         |         |         |         | 37.7953 |
| 16  | 23.5418  | 26.2962 | 28.8454 | 31.9999 | 34.2672 | 39.2524 |

**Serial Test: degree of freedom  $v=2$**

**Example 1**



# Poker Test

# Poker Test

Let  $m$  be a positive integer such that  $\left\lfloor \frac{n}{m} \right\rfloor \geq 5 \cdot 2^m$ , and let  $k = \left\lfloor \frac{n}{m} \right\rfloor$ .

$$\lfloor 10.5 \rfloor = 10$$

$$\lfloor 0.4 \rfloor = 0$$

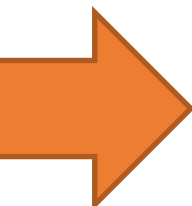
$$\lfloor 8.9 \rfloor = 8$$

$$\lfloor 12.999999999999999999 \rfloor = 12$$

Example 1

# Poker Test

$$\left\lfloor \frac{n}{m} \right\rfloor \geq 5 \cdot 2^m$$



|       |                                                  |     |                    |
|-------|--------------------------------------------------|-----|--------------------|
| $m=1$ | $\left\lfloor \frac{160}{1} \right\rfloor = 160$ | $>$ | $5 \cdot 2^1 = 10$ |
| $m=2$ | $\left\lfloor \frac{160}{2} \right\rfloor = 80$  | $>$ | $5 \cdot 2^2 = 20$ |
| $m=3$ | $\left\lfloor \frac{160}{3} \right\rfloor = 53$  | $>$ | $5 \cdot 2^3 = 40$ |
| $m=4$ | $\left\lfloor \frac{160}{4} \right\rfloor = 40$  | $<$ | $5 \cdot 2^4 = 80$ |

Example 1

# Poker Test

Type of blocks of length 3

$2^m$



Example 1

# Poker Test

Type of blocks of length 3

23



Example 1

# Poker Test

Type of blocks of length 3

000

001

010

011

100

101

110

111

8

Example 1

# Poker Test

111-000-110-001-000-101-001-110-111-100-100-100-100-1  
11-100-011-000-100-010-100-111-011-110-010-010-010-01  
1-110-001-100-010-001-010-011-101-111-001-001-001-001  
-111-000-110-001-000-101-001-110-111-100-100-100-100-1

Example 1

# Poker Test

111-000-110-001-000-101-001-110-111-100-100-100-100-1  
11-100-011-000-100-010-100-111-011-110-010-010-010-01  
1-110-001-100-010-001-010-011-101-111-001-001-001-001  
-111-000-110-001-000-101-001-110-111-100-100-100-100-1

Example 1

# Poker Test

111-000-110-001-000-101-001-110-111-100-100-100-100-1  
11-100-011-000-100-010-100-111-011-110-010-010-010-01  
1-110-001-100-010-001-010-011-101-111-001-001-001-001  
-111-000-110-001-000-101-001-110-111-100-100-100-100-1

Example 1

# Poker Test

Type of blocks of length 3

$$n_{000} = 5$$

$$n_{001} = 10$$

$$n_{010} = 6$$

$$n_{011} = 4$$

$$n_{100} = 12$$

$$n_{101} = 3$$

$$n_{110} = 6$$

$$n_{111} = 7$$

Example 1

# Poker Test

Here  $m=3$  and  $k=53$ . The blocks 000, 001, 010, 011, 100, 101, 110, 111 appear 5, 10, 6, 4, 12, 3, 6, and 7 times, respectively, and the value of the statistic  $X_3$  is 9.6415.

$$X_3 = \frac{2^m}{k} \left( \sum_{i=1}^{2^m} n_i^2 \right) - k$$

$$\begin{aligned} X_3 &= \frac{2^3}{53} (5^2 + 10^2 + 6^2 + 4^2 + 12^2 + 3^2 + 6^2 + 7^2) - 53 \\ &= \frac{8}{53} (25 + 100 + 36 + 16 + 144 + 9 + 36 + 49) - 53 = 9.6415 \end{aligned}$$

Example 1

# $\chi^2$ (chi-square) distribution

| $v$ | $\alpha$ |         |         |         |         |         |
|-----|----------|---------|---------|---------|---------|---------|
|     | 0.100    | 0.050   | 0.025   | 0.010   | 0.005   | 0.001   |
| 1   | 2.7055   | 3.8415  | 5.0239  | 6.6349  | 7.8794  | 10.8276 |
| 2   | 4.6052   | 5.9915  | 7.3778  | 9.2103  | 10.5966 | 13.8155 |
| 3   | 6.2514   | 7.8147  | 9.3484  | 11.3449 | 12.8382 | 16.2662 |
| 4   | 7.7794   | 9.4877  | 11.1433 | 13.2767 | 14.8603 | 18.4668 |
| 5   | 9.2364   | 11.0705 | 12.8325 | 15.0863 | 16.7496 | 20.5150 |
| 6   | 10.6446  | 12.5916 | 14.4494 | 16.8119 | 18.5476 | 22.4577 |
| 7   | 12.0170  | 14.0671 | 16.0128 | 18.4753 | 20.2777 | 24.3219 |
| 8   | 13.3616  | 15.5073 | 17.5345 | 20.0902 | 21.9550 | 26.1245 |
| 9   | 14.6837  | 16.9190 | 19.0228 | 21.6660 | 23.5894 | 27.8772 |
| 10  | 15.9872  | 18.3070 | 20.4832 | 23.2093 | 25.1882 | 29.5883 |
| 11  | 17.2750  | 19.6751 | 21.9200 | 24.7250 | 26.7568 | 31.2641 |
| 12  |          |         |         |         |         | 32.9095 |
| 13  |          |         |         |         |         | 34.5659 |
| 14  |          |         |         |         |         | 36.1909 |
| 15  |          |         |         |         |         | 37.7953 |
| 16  | 23.5418  | 26.2962 | 28.8454 | 31.9999 | 34.2672 | 39.2524 |

**Poker Test: degree of freedom  $v=2^m-1$**

Example 1



# Runs Test

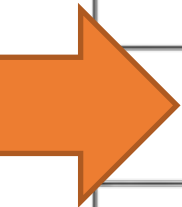
## Runs Test

$$X_4 = \sum_{i=1}^k \frac{(B_i - e_i)^2}{e_i} + \sum_{i=1}^k \frac{(G_i - e_i)^2}{e_i}$$

$$e_i = \frac{(n - i + 3)}{2^{i+2}} \geq 5$$

Example 1

# Runs Test



| i | $e_i = (n-i+3)/2^{i+2}$                    |   |   |
|---|--------------------------------------------|---|---|
| 1 | $(160-1+3)/2^3 = \frac{162}{8} = 20.25$    | > | 5 |
| 2 | $(160-2+3)/2^4 = \frac{161}{16} = 10.0625$ | > | 5 |
| 3 | $(160-3+3)/2^5 = \frac{160}{32} = 5$       | = | 5 |
| 4 | $(160-4+3)/2^6 = \frac{159}{64} = 2.4843$  | < | 5 |



Example 1

## Runs Test

1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$B_1 = 25$

Example 1

## Runs Test

11100011000010001010011101111001001001001

11100011000010001010011101111001001001001

11100011000010001010011101111001001001001

11100011000010001010011101111001001001001

$B_1=25$   $B_2=4$

Example 1

## Runs Test

1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$B_1=25$   $B_2=4$   $B_3=5$

## Runs Test

1110001100010001010011101111001001001001

1110001100010001010011101111001001001001

1110001100010001010011101111001001001001

1110001100010001010011101111001001001001

$B_1=25$   $B_2=4$   $B_3=5$

$G_1=8$

Example 1

## Runs Test

1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001  
1110001100010001010011101111001001001001

$B_1=25$   $B_2=4$   $B_3=5$

$G_1=8$   $G_2=20$

Example 1

## Runs Test

1110001100010001010011101111001001001001

1110001100010001010011101111001001001001

1110001100010001010011101111001001001001

1110001100010001010011101111001001001001

$B_1=25$   $B_2=4$   $B_3=5$

$G_1=8$   $G_2=20$   $G_3=12$

Example 1

# Runs Test

Here  $k=3$ . There are 25, 4, 5 blocks of lengths 1, 2, 3, respectively, and 8, 20, 12 gaps of lengths 1, 2, 3, respectively. The value of the statistic  $X_4$  is 31.7913.

$$X_4 = \sum_{i=1}^k \frac{(B_i - e_i)^2}{e_i} + \sum_{i=1}^k \frac{(G_i - e_i)^2}{e_i}$$

$$X_4 = \frac{(B_1 - e_1)^2}{e_1} + \frac{(B_2 - e_2)^2}{e_2} + \frac{(B_3 - e_3)^2}{e_3} + \frac{(G_1 - e_1)^2}{e_1} + \frac{(G_2 - e_2)^2}{e_2} + \frac{(G_3 - e_3)^2}{e_3}$$

$$X_4 = \frac{(25 - 20.25)^2}{20.25} + \frac{(4 - 10.0625)^2}{10.0625} + \frac{(5 - 5)^2}{5} + \frac{(8 - 20.25)^2}{20.25} + \frac{(20 - 10.0625)^2}{10.0625} + \frac{(12 - 5)^2}{5}$$

$$X_4 = 31.7913.$$

Example 1

# $\chi^2$ (chi-square) distribution

| $v$ | $\alpha$ |         |         |         |         |         |
|-----|----------|---------|---------|---------|---------|---------|
|     | 0.100    | 0.050   | 0.025   | 0.010   | 0.005   | 0.001   |
| 1   | 2.7055   | 3.8415  | 5.0239  | 6.6349  | 7.8794  | 10.8276 |
| 2   | 4.6052   | 5.9915  | 7.3778  | 9.2103  | 10.5966 | 13.8155 |
| 3   | 6.2514   | 7.8147  | 9.3484  | 11.3449 | 12.8382 | 16.2662 |
| 4   | 7.7794   | 9.4877  | 11.1433 | 13.2767 | 14.8603 | 18.4668 |
| 5   | 9.2364   | 11.0705 | 12.8325 | 15.0863 | 16.7496 | 20.5150 |
| 6   | 10.6446  | 12.5916 | 14.4494 | 16.8119 | 18.5476 | 22.4577 |
| 7   | 12.0170  | 14.0671 | 16.0128 | 18.4753 | 20.2777 | 24.3219 |
| 8   | 13.3616  | 15.5073 | 17.5345 | 20.0902 | 21.9550 | 26.1245 |
| 9   | 14.6837  | 16.9190 | 19.0228 | 21.6660 | 23.5894 | 27.8772 |
| 10  | 15.9872  | 18.3070 | 20.4832 | 23.2093 | 25.1882 | 29.5883 |
| 11  | 17.2750  | 19.6751 | 21.9200 | 24.7250 | 26.7568 | 31.2641 |
| 12  |          |         |         |         |         | 32.9095 |
| 13  |          |         |         |         |         | 34.5659 |
| 14  |          |         |         |         |         | 36.1909 |
| 15  |          |         |         |         |         | 37.7953 |
| 16  | 23.5418  | 26.2962 | 28.8454 | 31.9999 | 34.2672 | 39.2524 |

**Runs Test: degree of freedom  $v=2k-2$**

Example 1



# Results Discussion

# $\chi^2$ (chi-square) distribution

| $v$ | $\alpha$ |         |         |         |         |         |
|-----|----------|---------|---------|---------|---------|---------|
|     | 0.100    | 0.050   | 0.025   | 0.010   | 0.005   | 0.001   |
| 1   | 2.7055   | 3.8415  | 5.0239  | 6.6349  | 7.8794  | 10.8276 |
| 2   | 4.6052   | 5.9915  | 7.3778  | 9.2103  | 10.5966 | 13.8155 |
| 3   | 6.2514   | 7.8147  | 9.3484  | 11.3449 | 12.8382 | 16.2662 |
| 4   | 7.7794   | 9.4877  | 11.1433 | 13.2767 | 14.8603 | 18.4668 |
| 5   | 9.2364   | 11.0705 | 12.8325 | 15.0863 | 16.7496 | 20.5150 |
| 6   | 10.6446  | 12.5916 | 14.4494 | 16.8119 | 18.5476 | 22.4577 |
| 7   | 12.0170  | 14.0671 | 16.0128 | 18.4753 | 20.2777 | 24.3219 |
| 8   | 13.3616  | 15.5073 | 17.5345 | 20.0902 | 21.9550 | 26.1245 |
| 9   | 14.6837  | 16.9190 | 19.0228 | 21.6660 | 23.5894 | 27.8772 |
| 10  | 15.9872  | 18.3070 | 20.4832 | 23.2093 | 25.1882 | 29.5883 |

- 3.8415 (for one degree of freedom)
- 5.9915 (for two degree of freedom)
- 14.0671 (for seven degree of freedom, since  $2^m - 1 = 2^3 - 1 = 7$ )
- 9.4877 (for four degree of freedom, since  $2k - 2 = 2(3) - 2 = 4$ )

Example 1

## Results Discussion

For a significance level of  $\alpha = 0.05$ , the threshold values for  $X_1$ ,  $X_2$ ,  $X_3$ , and  $X_4$  are:

$$X_1 = 0.4 < 3.8415$$

$$X_2 = 0.6252 < 5.9915$$

$$X_3 = 9.6415 < 14.0671$$

$$X_4 = 31.7913 > 9.4877$$

## Results Discussion

Hence, the given sequence  $s$  passes the **frequency**, **serial**, and **poker** tests, but fails the **runs** test.

So,  $s$  is **not a pn-sequence** i.e. it is not random sequence

# Example 2



0101011101100011111001101001000  
0101011101100011111001101001000  
0101011101100011111001101001000  
0101011101100011111001101001000

n=124

Example 2



# Frequency Test

# Frequency Test

0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0

$n=124$

$n_0=60$

Example 2

# Frequency Test

0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0

$n=124$

$n_0=60$     $n_1=64$

Example 2

# Frequency Test

(i) (frequency test)  $n_0=60$ ,  $n_1=64$ , and the value of the statistic  $X_1$  is 0.1290.

$$X_1 = \frac{(60 - 64)^2}{124} = 0.1290 < 3.84,$$

so the sequence pass this test.

# Serial Test

The background of the slide features a blurred photograph of a desk. On the desk, there is a spiral-bound notebook with a black cover and a black pen. A dark blue diagonal shape covers the center of the image, and two light blue diagonal bars are positioned on either side of the text.

# Serial Test

0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0

$n=124$

$n_0=60$     $n_1=64$

$n_{00}=27$

Example 2

# Serial Test

0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0

$n=124$

$n_0=60$     $n_1=64$

$n_{00}=27, n_{01}=32$

Example 2

# Serial Test

0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0

$n=124$

$n_0=60$     $n_1=64$

$n_{00}=27$ ,  $n_{01}=32$ ,  $n_{10}=32$

Example 2

# Serial Test

01010111011000011111001101001000  
01010111011000011111001101001000  
01010111011000011111001101001000  
01010111011000011111001101001000

$n=124$

$n_0=60$     $n_1=64$

$n_{00}=27$ ,  $n_{01}=32$ ,  $n_{10}=32$ ,  $n_{11}=32$

Example 2

# Serial Test

$$X_2 = \frac{4}{n-1} \sum_{i=0}^1 \sum_{j=0}^1 n_{ij}^2 - \frac{2}{n} \sum_{i=0}^1 n_i^2 + 1$$

(ii) (serial test)  $n_{00}=27$ ,  $n_{01}=32$ ,  $n_{10}=32$ ,  $n_{11}=32$ , and the value of the statistic  $X_2$  is

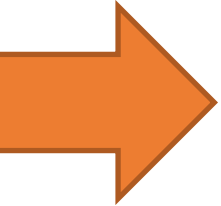
$$\begin{aligned} X_2 &= \frac{4}{123} (27^2 + 32^2 + 32^2 + 32^2) - \frac{2}{124} (60^2 + 64^2) + 1 \\ &= \frac{4}{123} (3801) - \frac{2}{124} (7696) + 1 \\ &= 123.6097 - 124.1290 + 1 = 0.4807 < 5.99, \end{aligned}$$

so the sequence pass this test also.

# Poker Test

The image shows a desk with a spiral-bound notebook, a black pen, and a smartphone. A dark blue geometric overlay, consisting of a large triangle and two smaller parallelograms, is positioned over the desk. The text "Poker Test" is written in white on the dark blue area.

# Poker Test



|       |                                                  |     |                    |
|-------|--------------------------------------------------|-----|--------------------|
| $m=1$ | $\left\lfloor \frac{124}{1} \right\rfloor = 124$ | $>$ | $5 \cdot 2^1 = 10$ |
| $m=2$ | $\left\lfloor \frac{124}{2} \right\rfloor = 62$  | $>$ | $5 \cdot 2^2 = 20$ |
| $m=3$ | $\left\lfloor \frac{124}{3} \right\rfloor = 41$  | $>$ | $5 \cdot 2^3 = 40$ |
| $m=4$ | $\left\lfloor \frac{124}{4} \right\rfloor = 31$  | $<$ | $5 \cdot 2^4 = 80$ |



Example 2

# Poker Test

Here  $m=3$  and  $k=41$ .

$$X_3 = \frac{2^m}{k} \left( \sum_{i=1}^{2^m} n_i^2 \right) - k$$

|     |     |     |     |     |     |     |     |     |     |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 010 | 101 | 110 | 110 | 001 | 111 | 100 | 110 | 100 | 100 |
| 001 | 010 | 111 | 011 | 000 | 111 | 110 | 011 | 010 | 010 |
| 000 | 101 | 011 | 101 | 100 | 011 | 111 | 001 | 101 | 001 |
| 000 | 010 | 101 | 110 | 110 | 001 | 111 | 100 | 110 | 100 |
| 100 | 0   |     |     |     |     |     |     |     |     |

The blocks 000, 001, 010, 011, 100, 101, 110, 111 appear 3, 5, 5, 4, 7, 5, 7, and 5 times, respectively, and the value of the statistic  $X_3$  is

$$\begin{aligned}
 X_3 &= \frac{2^3}{41} (3^2 + 5^2 + 5^2 + 4^2 + 7^2 + 5^2 + 7^2 + 5^2) - 41 \\
 &= \frac{8}{41} (9 + 25 + 25 + 16 + 49 + 25 + 49 + 25) - 41 = 2.5122
 \end{aligned}$$

The degree of freedom here is  $2^3 - 1 = 7$ , so  $\chi^2 = 14.0671$ . And since  $2.5122 < 14.0671$ , so the sequence pass this test also.

Example 2



# Runs Test

# Runs Test

| i | $e_i = (n - i + 3) / 2^{i+2}$                   |   |   |
|---|-------------------------------------------------|---|---|
| 1 | $(124 - 1 + 3) / 2^3 = \frac{126}{8} = 15.75$   | > | 5 |
| 2 | $(124 - 2 + 3) / 2^4 = \frac{125}{16} = 7.8125$ | > | 5 |
| 3 | $(124 - 3 + 3) / 2^5 = \frac{124}{32} = 3.875$  | < | 5 |

Example 2

# Runs Test

0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0

$G_1=17$

Example 2

# Runs Test

0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0

0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0

0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0

0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0

$G_1=17$     $G_2=8$

Example 2

# Runs Test

0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 0 1 0 0 0  
0 1 0 1 0 1 1 1 0 1 1 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 0 1 0 0 0

$G_1=17$     $G_2=8$

$B_1=16$

Example 2

# Runs Test

0 1 0 1 0 1 1 1 0 1 1 0 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0

0 1 0 1 0 1 1 1 0 1 1 0 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0

0 1 0 1 0 1 1 1 0 1 1 0 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0

0 1 0 1 0 1 1 1 0 1 1 0 0 0 0 1 1 1 1 1 0 0 1 1 0 1 0 0 1 0 0 0

$G_1=17$     $G_2=8$

$B_1=16$     $B_2=8$

Example 2

# Runs Test

Here  $k=2$ .

| $i$ | $B_i$ | $G_i$ |
|-----|-------|-------|
| 1   | 16    | 17    |
| 2   | 8     | 8     |

There are 16, 8 blocks of lengths 1, 2, respectively, and 17, 8 gaps of lengths 1, 2, respectively. The value of the statistic  $X_4$  is

$$X_4 = \frac{(B_1 - e_1)^2}{e_1} + \frac{(B_2 - e_2)^2}{e_2} + \frac{(G_1 - e_1)^2}{e_1} + \frac{(G_2 - e_2)^2}{e_2}$$
$$X_4 = \frac{(16 - 15.75)^2}{15.75} + \frac{(8 - 7.8125)^2}{7.8125} + \frac{(17 - 15.75)^2}{15.75} + \frac{(8 - 7.8125)^2}{7.8125}$$
$$X_4 = 0.11213.$$

The degree of freedom here is  $2(2)-2=2$ , so  $\chi^2=5.99$ . And since  $0.11213 < 5.99$ , so the sequence pass this test also.

Example 2



# Results Discussion

## Results Discussion

Hence, the given sequence  $s$  passes the **frequency**, **serial**, **poker** and **runs** test.

So,  $s$  is **a pn-sequence** i.e. it is not random sequence



**THANK YOU**

**Any questions?**

**You can find me at:**  
**[saad.m@sc.uobaghdad.edu.iq](mailto:saad.m@sc.uobaghdad.edu.iq)**

**Saad Al-Momen**

# Stream Ciphers

**CIPHER SYSTEMS**

**Fourth Class  
Department of Mathematics  
College of Science - University of Baghdad**

**9.**

# Introduction



# Introduction

- ✓ Encrypt **individual** characters (usually binary digits) of a plaintext message **one at a time**.
- ✓ **Faster** than block ciphers in hardware.
- ✓ **Less complex** hardware circuitry.
- ✓ **More appropriate**, and in some cases mandatory when **buffering is limited**.
- ✓ Have **limited** or **no** error propagation.

# One Time Pad



# One Time Pad





# Unconditional Security

A cryptosystem is unconditionally secure if it **cannot be broken** even with infinite computational resources.



# OTP

$$|M| = |C| = |K|$$

$$m_i; c_i; z_i \in \{0,1\}$$

Encryption:  $c_i = e_{z_i}(m_i) = m_i \oplus z_i$

Decryption:  $m_i = d_{z_i}(c_i) = c_i \oplus z_i$



# XOR

| a | b | $a \oplus b$ |
|---|---|--------------|
| 0 | 0 | 0            |
| 0 | 1 | 1            |
| 1 | 0 | 1            |
| 1 | 1 | 0            |



# Encryption and decryption are the same operation (XOR)

Decryption:

$$c_i \oplus z_i$$



# Encryption and decryption are the same operation (XOR)

Decryption:

$$c_i \oplus z_i = (m_i \oplus z_i) \oplus z_i$$



# Encryption and decryption are the same operation (XOR)

Decryption:

$$c_i \oplus z_i = (m_i \oplus z_i) \oplus z_i = m_i \oplus (z_i \oplus z_i)$$



## Encryption and decryption are the same operation (XOR)

Decryption:

$$c_i \oplus z_i = (m_i \oplus z_i) \oplus z_i = m_i \oplus \overset{\text{0}}{\cancel{z_i \oplus z_i}}$$

Since,  $z_i \oplus z_i = 0$  for  $z_i = 0$  and for  $z_i = 1$



## Encryption and decryption are the same operation (XOR)

Decryption:

$$c_i \oplus z_i = (m_i \oplus z_i) \oplus z_i = m_i \oplus (\cancel{z_i} \oplus z_i) = m_i$$

The diagram shows a red arrow pointing from the  $z_i$  term in the expression  $(\cancel{z_i} \oplus z_i)$  to a bold **0** above it, indicating that  $z_i \oplus z_i = 0$ .

Since,  $z_i \oplus z_i = 0$  for  $z_i = 0$  and for  $z_i = 1$

# Example



# Example

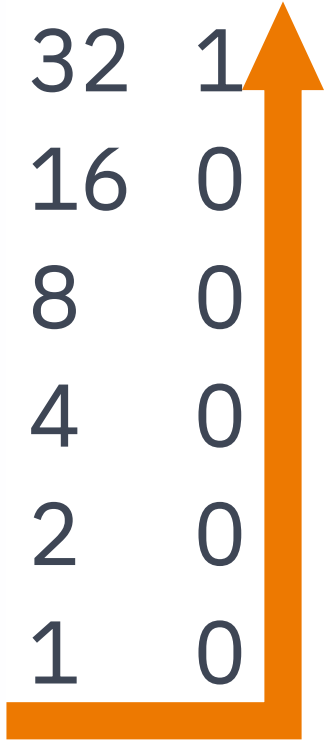
Encryption of the letter **A** by Alice.

**A** is given in ASCII code as  $65_{10} = 1000001_2$ .

Let's assume that the first key stream bits are  
 $z_1, \dots, z_7 = 0101101$

# Decimal to Binary

|         |   |
|---------|---|
| 65      |   |
| 32      | 1 |
| 16      | 0 |
| 8       | 0 |
| 4       | 0 |
| 2       | 0 |
| 1       | 0 |
| 1000001 |   |



# Example

Encryption by Alice:

Plaintext  $m_i$  : 

|   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 0 | 1 |
|---|---|---|---|---|---|---|

 = **A** (ASCII symbol)

Key stream  $z_i$ : 

|   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|
| 0 | 1 | 0 | 1 | 1 | 0 | 1 |
|---|---|---|---|---|---|---|

Ciphertext  $c_i$  : 

|   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|
| 1 | 1 | 0 | 1 | 1 | 0 | 0 |
|---|---|---|---|---|---|---|

 = **ℓ** (ASCII symbol)

Remember:

5632

$5000 + 600 + 30 + 2$

$5 * 1000 + 6 * 100 + 3 * 10 + 2 * 1$

$5 * 10^3 + 6 * 10^2 + 3 * 10^1 + 2 * 10^0$

In Binary System

|       |       |       |       |       |       |       |
|-------|-------|-------|-------|-------|-------|-------|
| 1     | 1     | 0     | 1     | 1     | 0     | 0     |
| $2^6$ | $2^5$ | $2^4$ | $2^3$ | $2^2$ | $2^1$ | $2^0$ |
| 64    | 32    | 16    | 8     | 4     | 2     | 1     |

In Binary System

|   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|
| 1 | 1 | 0 | 1 | 1 | 0 | 0 |
|---|---|---|---|---|---|---|

|    |    |    |   |   |   |   |
|----|----|----|---|---|---|---|
| 64 | 32 | 16 | 8 | 4 | 2 | 1 |
|----|----|----|---|---|---|---|

$$64 + 32 + 8 + 4 = 108$$

# ASCII - Binary Character Table

| Letter | ASCII Code | Binary   | Letter | ASCII Code | Binary   |
|--------|------------|----------|--------|------------|----------|
| a      | 097        | 01100001 | A      | 065        | 01000001 |
| b      | 098        | 01100010 | B      | 066        | 01000010 |
| c      | 099        | 01100011 | C      | 067        | 01000011 |
| d      | 100        | 01100100 | D      | 068        | 01000100 |
| e      | 101        | 01100101 | E      | 069        | 01000101 |
| f      | 102        | 01100110 | F      | 070        | 01000110 |
| g      | 103        | 01100111 | G      | 071        | 01000111 |
| h      | 104        | 01101000 | H      | 072        | 01001000 |
| i      | 105        | 01101001 | I      | 073        | 01001001 |
| j      | 106        | 01101010 | J      | 074        | 01001010 |
| k      | 107        | 01101011 | K      | 075        | 01001011 |
| l      | 108        | 01101100 | L      | 076        | 01001100 |
| m      | 109        | 01101101 | M      | 077        | 01001101 |
| n      | 110        | 01101110 | N      | 078        | 01001110 |
| o      | 111        | 01101111 | O      | 079        | 01001111 |
| p      | 112        | 01110000 | P      | 080        | 01010000 |
| q      | 113        | 01110001 | Q      | 081        | 01010001 |
| r      | 114        | 01110010 | R      | 082        | 01010010 |
| s      | 115        | 01110011 | S      | 083        | 01010011 |
| t      | 116        | 01110100 | T      | 084        | 01010100 |
| u      | 117        | 01110101 | U      | 085        | 01010101 |
| v      | 118        | 01110110 | V      | 086        | 01010110 |
| w      | 119        | 01110111 | W      | 087        | 01010111 |
| x      | 120        | 01111000 | X      | 088        | 01011000 |
| y      | 121        | 01111001 | Y      | 089        | 01011001 |
| z      | 122        | 01111010 | Z      | 090        | 01011010 |



Decryption by Bob:

Ciphertext  $c_i$ : 

|   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|
| 1 | 1 | 0 | 1 | 1 | 0 | 0 |
|---|---|---|---|---|---|---|

 = **ℓ** (ASCII symbol)

Key stream  $z_i$ : 

|   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|
| 0 | 1 | 0 | 1 | 1 | 0 | 1 |
|---|---|---|---|---|---|---|

Plaintext  $m_i$ : 

|   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 0 | 1 |
|---|---|---|---|---|---|---|

 = **A** (ASCII symbol)

“

*The OTP is  
unconditionally  
secure if keys are  
only used once.*





1.

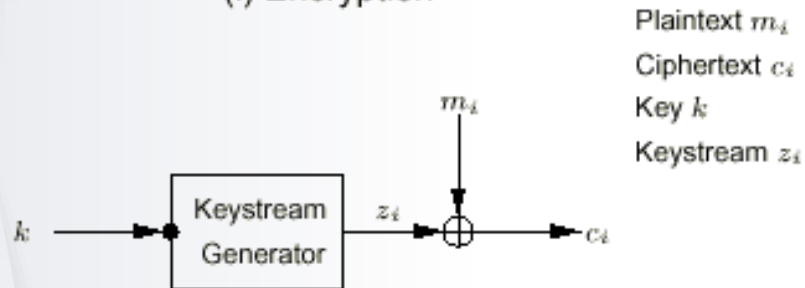
# Synchronous Stream Ciphers

## ***Synchronous Stream***

Cipher in which the **keystream** is generated **independently** of the **plaintext** and of the **ciphertext**.



### (i) Encryption



General model of a binary additive synchronous stream cipher

# Properties of synchronous stream ciphers

## *Synchronization requirements*

Both the sender and receiver must be *synchronized* – using the **same key and operating at the same position** (state) within that key – to allow for proper decryption.

If **synchronization is lost** due to ciphertext digits being **inserted** or **deleted** during transmission, then decryption **fails** and can only be restored through additional techniques for re-synchronization.

Encryption

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $m_1$ | $m_2$ | $m_3$ | $m_4$ | $m_5$ | $m_6$ | $m_7$ | $m_8$ | $m_9$ | $m_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $k_1$ | $k_2$ | $k_3$ | $k_4$ | $k_5$ | $k_6$ | $k_7$ | $k_8$ | $k_9$ | $k_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $c_1$ | $c_2$ | $c_3$ | $c_4$ | $c_5$ | $c_6$ | $c_7$ | $c_8$ | $c_9$ | $c_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

Decryption

---

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $c_1$ | $c_2$ | $c_3$ | $c_4$ | $c_5$ | $c_6$ | $c_7$ | $c_8$ | $c_9$ | $c_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

Encryption

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $m_1$ | $m_2$ | $m_3$ | $m_4$ | $m_5$ | $m_6$ | $m_7$ | $m_8$ | $m_9$ | $m_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $k_1$ | $k_2$ | $k_3$ | $k_4$ | $k_5$ | $k_6$ | $k_7$ | $k_8$ | $k_9$ | $k_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $c_1$ | $c_2$ | $c_3$ | $c_4$ | $c_5$ | $c_6$ | $c_7$ | $c_8$ | $c_9$ | $c_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

Decryption

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $c_1$ | $c_2$ | $c_3$ | $c_4$ | $c_5$ | $c_6$ | $c_7$ | $c_8$ | $c_9$ | $c_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

# Encryption

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $m_1$ | $m_2$ | $m_3$ | $m_4$ | $m_5$ | $m_6$ | $m_7$ | $m_8$ | $m_9$ | $m_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $k_1$ | $k_2$ | $k_3$ | $k_4$ | $k_5$ | $k_6$ | $k_7$ | $k_8$ | $k_9$ | $k_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $c_1$ | $c_2$ | $c_3$ | $c_4$ | $c_5$ | $c_6$ | $c_7$ | $c_8$ | $c_9$ | $c_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

# Decryption

|       |       |       |       |       |       |          |          |          |          |
|-------|-------|-------|-------|-------|-------|----------|----------|----------|----------|
| $c_1$ | $c_2$ | $c_3$ | $c_7$ | $c_8$ | $c_9$ | $c_{10}$ | $c_{11}$ | $c_{12}$ | $c_{13}$ |
|-------|-------|-------|-------|-------|-------|----------|----------|----------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $k_1$ | $k_2$ | $k_3$ | $k_4$ | $k_5$ | $k_6$ | $k_7$ | $k_8$ | $k_9$ | $k_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |   |   |   |   |   |   |   |
|-------|-------|-------|---|---|---|---|---|---|---|
| $m_1$ | $m_2$ | $m_3$ | x | x | x | x | x | x | x |
|-------|-------|-------|---|---|---|---|---|---|---|

# Encryption

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $m_1$ | $m_2$ | $m_3$ | $m_4$ | $m_5$ | $m_6$ | $m_7$ | $m_8$ | $m_9$ | $m_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $k_1$ | $k_2$ | $k_3$ | $k_4$ | $k_5$ | $k_6$ | $k_7$ | $k_8$ | $k_9$ | $k_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $c_1$ | $c_2$ | $c_3$ | $c_4$ | $c_5$ | $c_6$ | $c_7$ | $c_8$ | $c_9$ | $c_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

# Decryption

|       |       |       |   |       |       |       |          |          |          |
|-------|-------|-------|---|-------|-------|-------|----------|----------|----------|
| $c_1$ | $c_2$ | $c_3$ | X | $c_7$ | $c_8$ | $c_9$ | $c_{10}$ | $c_{11}$ | $c_{12}$ |
|-------|-------|-------|---|-------|-------|-------|----------|----------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $k_1$ | $k_2$ | $k_3$ | $k_4$ | $k_5$ | $k_6$ | $k_7$ | $k_8$ | $k_9$ | $k_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |   |   |   |   |   |   |   |
|-------|-------|-------|---|---|---|---|---|---|---|
| $m_1$ | $m_2$ | $m_3$ | X | X | X | X | X | X | X |
|-------|-------|-------|---|---|---|---|---|---|---|

# Encryption

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $m_1$ | $m_2$ | $m_3$ | $m_4$ | $m_5$ | $m_6$ | $m_7$ | $m_8$ | $m_9$ | $m_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $k_1$ | $k_2$ | $k_3$ | $k_4$ | $k_5$ | $k_6$ | $k_7$ | $k_8$ | $k_9$ | $k_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $c_1$ | $c_2$ | $c_3$ | $c_4$ | $c_5$ | $c_6$ | $c_7$ | $c_8$ | $c_9$ | $c_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

# Decryption

|       |       |       |   |   |       |       |       |          |          |
|-------|-------|-------|---|---|-------|-------|-------|----------|----------|
| $c_1$ | $c_2$ | $c_3$ | X | X | $c_7$ | $c_8$ | $c_9$ | $c_{10}$ | $c_{11}$ |
|-------|-------|-------|---|---|-------|-------|-------|----------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $k_1$ | $k_2$ | $k_3$ | $k_4$ | $k_5$ | $k_6$ | $k_7$ | $k_8$ | $k_9$ | $k_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |   |   |   |   |   |   |   |
|-------|-------|-------|---|---|---|---|---|---|---|
| $m_1$ | $m_2$ | $m_3$ | X | X | X | X | X | X | X |
|-------|-------|-------|---|---|---|---|---|---|---|

# Encryption

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $m_1$ | $m_2$ | $m_3$ | $m_4$ | $m_5$ | $m_6$ | $m_7$ | $m_8$ | $m_9$ | $m_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $k_1$ | $k_2$ | $k_3$ | $k_4$ | $k_5$ | $k_6$ | $k_7$ | $k_8$ | $k_9$ | $k_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $c_1$ | $c_2$ | $c_3$ | $c_4$ | $c_5$ | $c_6$ | $c_7$ | $c_8$ | $c_9$ | $c_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

# Decryption

|       |       |       |   |   |   |       |       |       |          |
|-------|-------|-------|---|---|---|-------|-------|-------|----------|
| $c_1$ | $c_2$ | $c_3$ | X | X | X | $c_7$ | $c_8$ | $c_9$ | $c_{10}$ |
|-------|-------|-------|---|---|---|-------|-------|-------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $k_1$ | $k_2$ | $k_3$ | $k_4$ | $k_5$ | $k_6$ | $k_7$ | $k_8$ | $k_9$ | $k_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |   |   |   |   |   |   |   |
|-------|-------|-------|---|---|---|---|---|---|---|
| $m_1$ | $m_2$ | $m_3$ | X | X | X | X | X | X | X |
|-------|-------|-------|---|---|---|---|---|---|---|

# Properties of synchronous stream ciphers

## *No error propagation*

A ciphertext digit that is modified (but not deleted) during transmission does not affect the decryption of other ciphertext digits.

# Encryption

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $m_1$ | $m_2$ | $m_3$ | $m_4$ | $m_5$ | $m_6$ | $m_7$ | $m_8$ | $m_9$ | $m_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $k_1$ | $k_2$ | $k_3$ | $k_4$ | $k_5$ | $k_6$ | $k_7$ | $k_8$ | $k_9$ | $k_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $c_1$ | $c_2$ | $c_3$ | $c_4$ | $c_5$ | $c_6$ | $c_7$ | $c_8$ | $c_9$ | $c_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

# Decryption

|       |       |       |       |   |       |       |       |       |          |
|-------|-------|-------|-------|---|-------|-------|-------|-------|----------|
| $c_1$ | $c_2$ | $c_3$ | $c_4$ | X | $c_6$ | $c_7$ | $c_8$ | $c_9$ | $c_{10}$ |
|-------|-------|-------|-------|---|-------|-------|-------|-------|----------|

|       |       |       |       |       |       |       |       |       |          |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|
| $k_1$ | $k_2$ | $k_3$ | $k_4$ | $k_5$ | $k_6$ | $k_7$ | $k_8$ | $k_9$ | $k_{10}$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|----------|

|       |       |       |       |   |       |       |       |       |          |
|-------|-------|-------|-------|---|-------|-------|-------|-------|----------|
| $m_1$ | $m_2$ | $m_3$ | $m_4$ | X | $m_6$ | $m_7$ | $m_8$ | $m_9$ | $m_{10}$ |
|-------|-------|-------|-------|---|-------|-------|-------|-------|----------|

# Properties of synchronous stream ciphers

## *Active attacks*

Insertion, deletion, or replay of ciphertext digits by an active adversary causes immediate loss of synchronization, and hence might possibly be detected by the decryptor.

because the decryption mapping depends only on a fixed number of preceding ciphertext characters.

2.

# Asynchronous Stream Ciphers

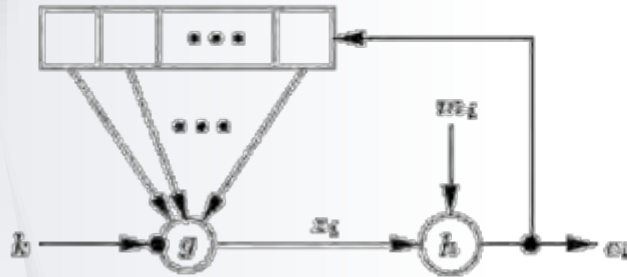
Self-Synchronizing Stream  
Cipher

## ***Asynchronous Stream***

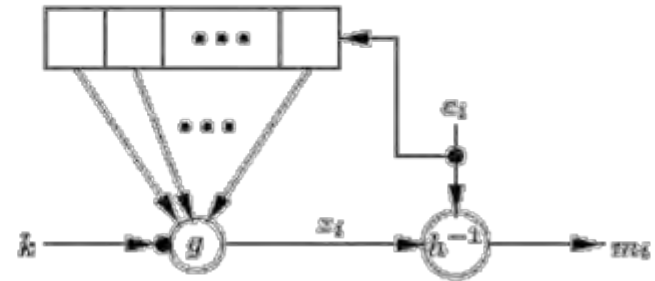
Cipher in which the **keystream** is generated as a function of the key and a fixed number of previous ciphertext digits.



(i) Encryption



(ii) Decryption



General model of a self-synchronizing stream cipher

# Properties of asynchronous stream ciphers

## *self-synchronization*

Its capable of re-establishing proper decryption automatically after loss of synchronization, with only a fixed number of plaintext characters unrecoverable.

# Properties of asynchronous stream ciphers

## *Limited error propagation*

If a single ciphertext digit is **modified** (or even **deleted** or **inserted**) during transmission, then decryption of up to **t** **subsequent** ciphertext digits may be **incorrect**.

**After** which correct decryption resumes.

# Properties of asynchronous stream ciphers

## *Active attacks*

**Modification** of ciphertext digits by an active adversary causes **several other** ciphertext digits to be decrypted **incorrectly**. It is likely of being detected by the decryptor.

It is **more difficult** to detect **insertion**, **deletion**, or **replay** of ciphertext digits by an active adversary.

# Properties of asynchronous stream ciphers

## *Diffusion of plaintext statistics*

The statistical properties of the plaintext are **dispersed** through the ciphertext.

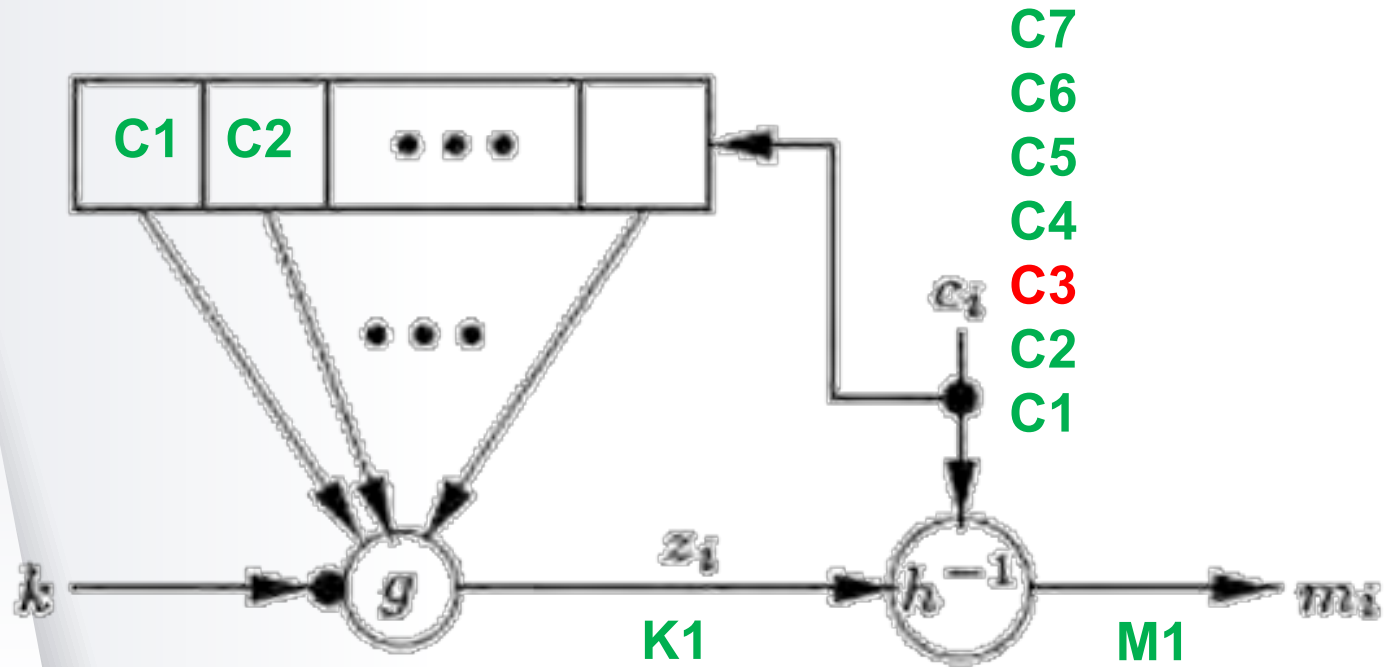
self-synchronizing stream ciphers may be **more resistant** than synchronous stream ciphers **against attacks based on plaintext redundancy**.

# Decleration

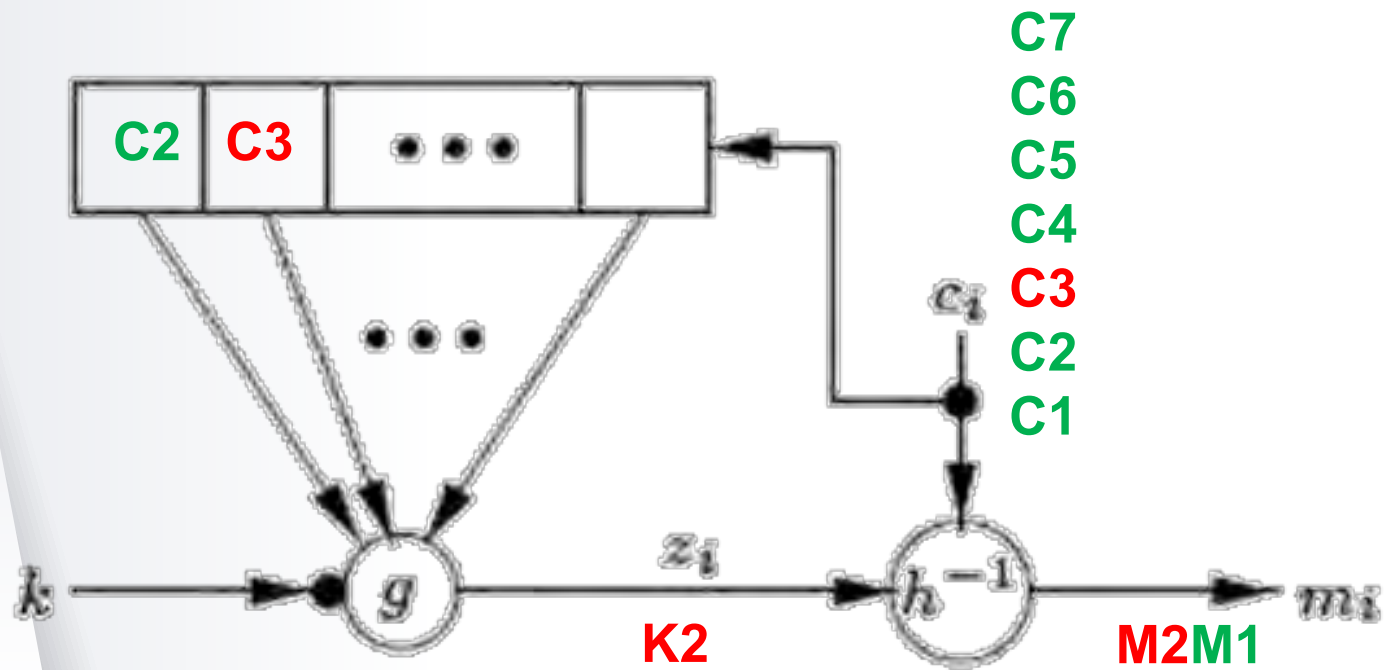
for Asynchronous cipher



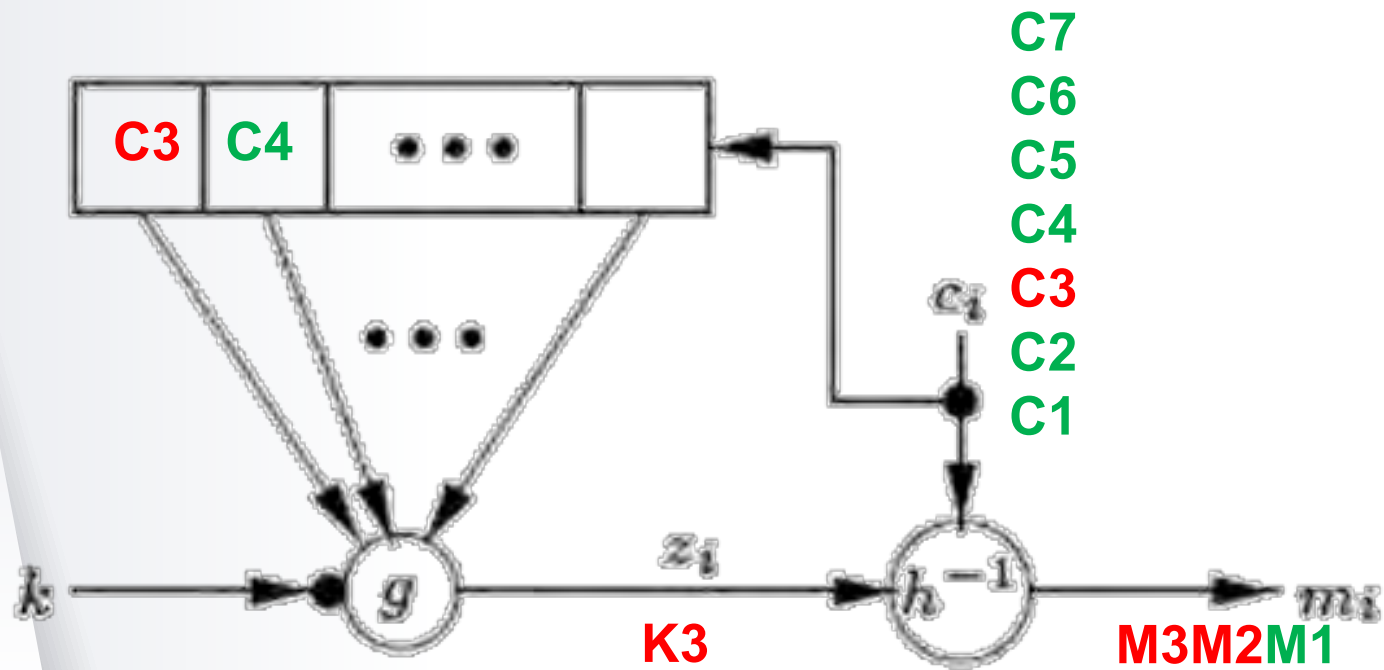
# Decleration



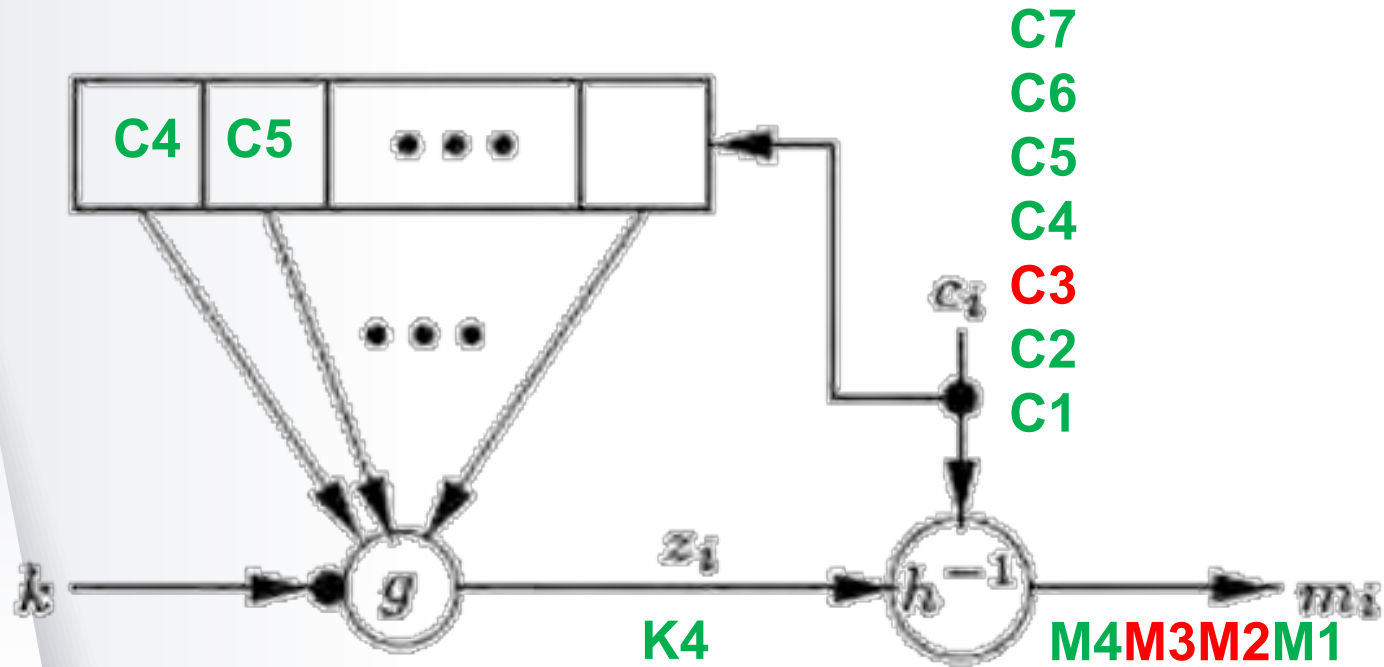
# Decleration



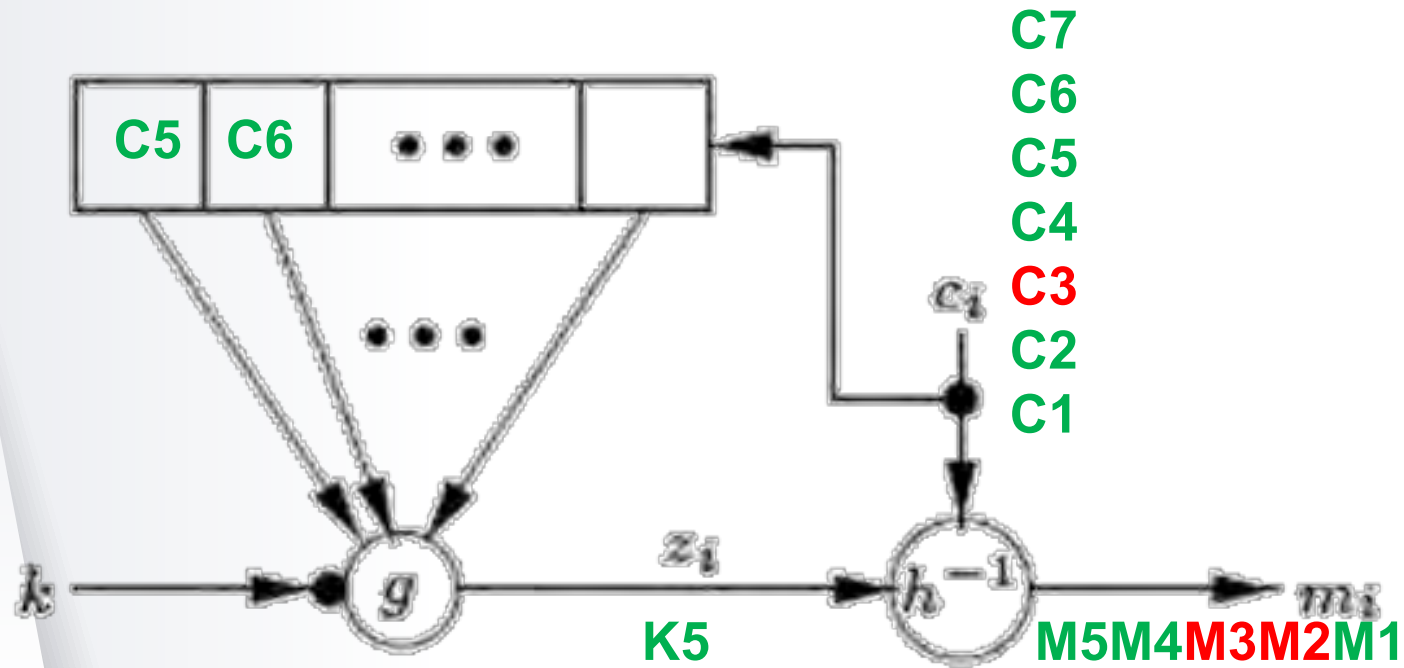
# Decleration



# Declaration



# Declaration



# THANK YOU

**Any questions?**

**You can find me at:**

**[saad.m@sc.uobaghdad.edu.iq](mailto:saad.m@sc.uobaghdad.edu.iq)**

**Saad Al-Momen**

# Stream Ciphers

**CIPHER SYSTEMS**

**Fourth Class**  
**Department of Mathematics**  
**College of Science - University of Baghdad**

**10.**

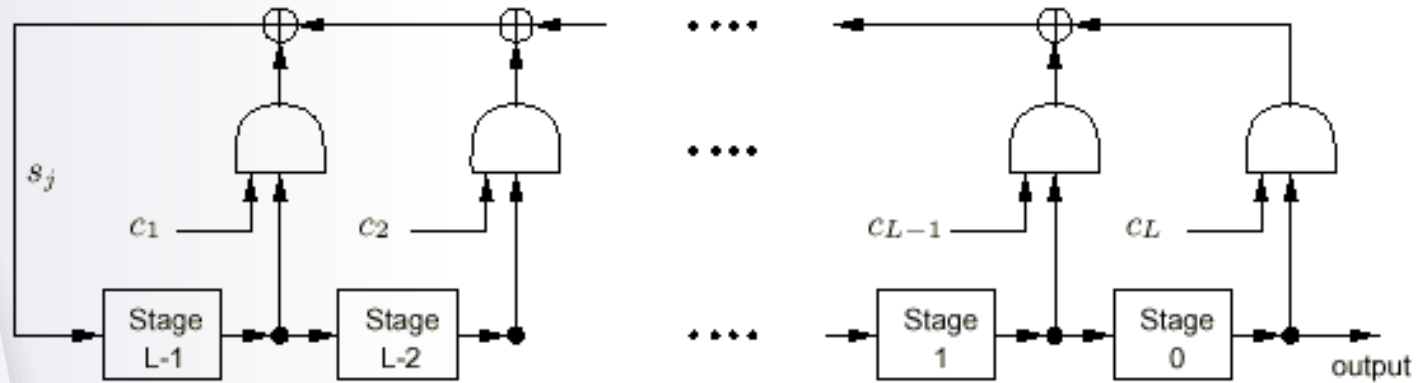
# Linear Feedback Shift Register (LFSR)



## *Linear Feedback Shift Register*

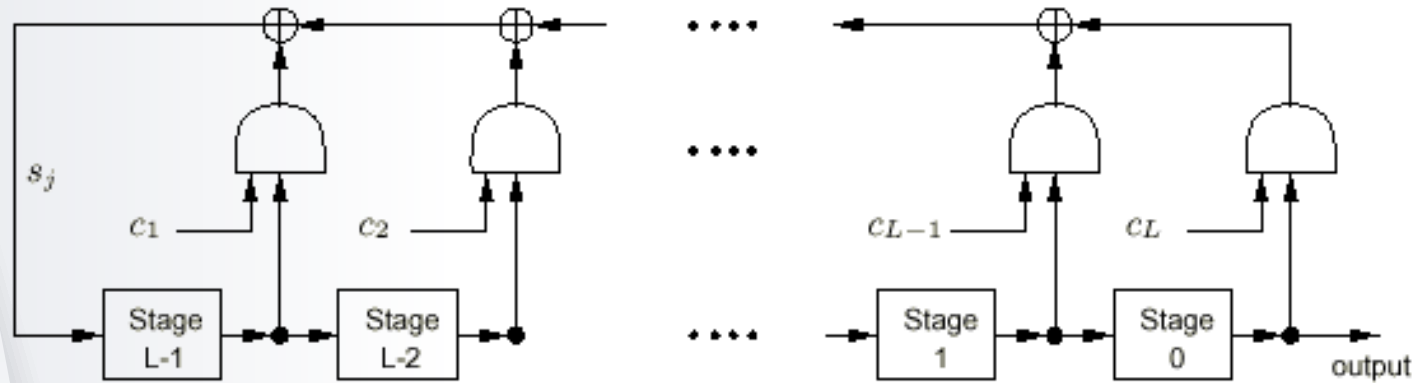
LFSR of length  $L$  consists of  $L$  stages (or delay elements) numbered  $0, 1, \dots, L-1$ , each capable of storing **one bit** and having **one input** and **one output**; and a clock which controls the movement of data.





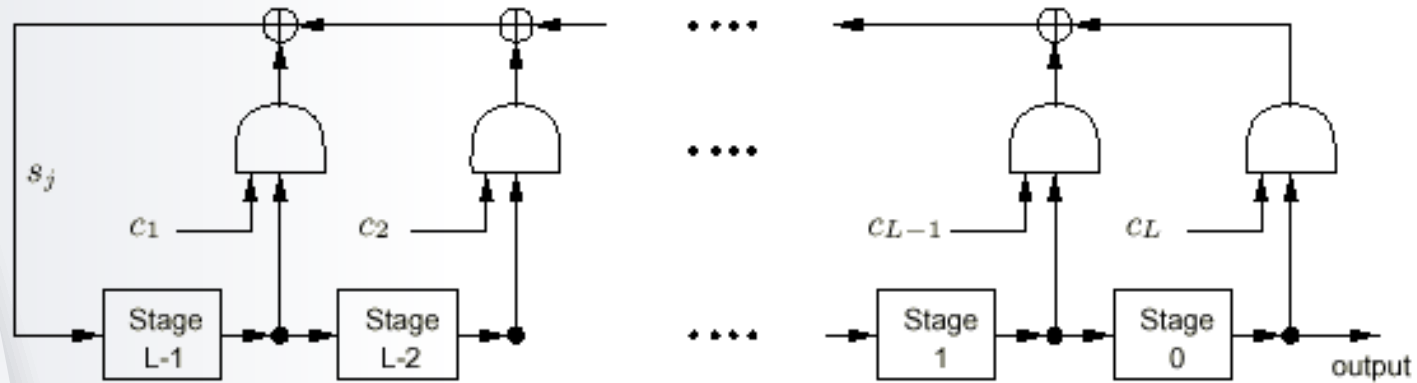


(ii) The content of stage  $i$  is **moved** to stage  $i-1$  for each  $i$ .  
 $1 \leq i \leq L-1$



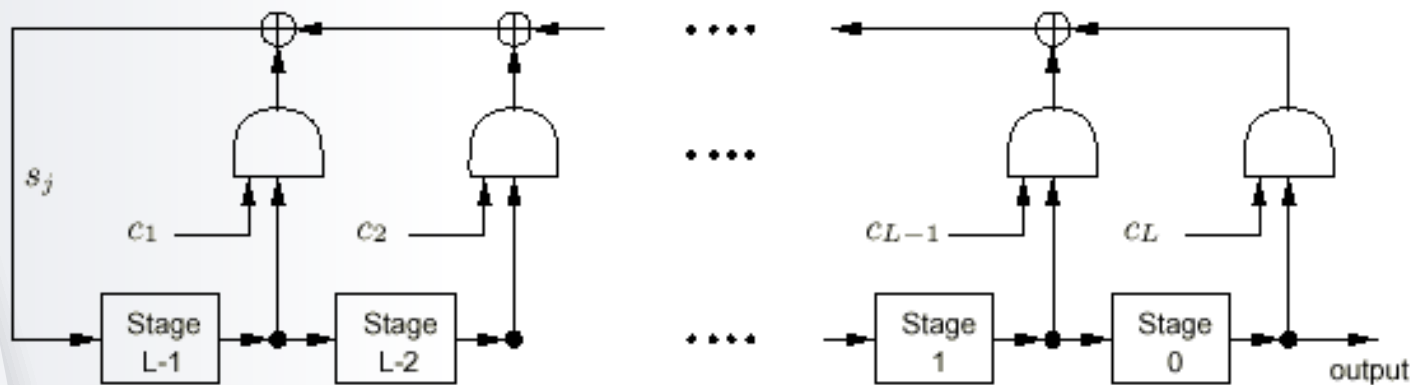


(iii) The new content of stage **L-1** is the *feedback bit*  $s_j$  which is **calculated** by adding together modulo 2 the previous contents of **a fixed subset of stages 0,1, ...,L-1**.





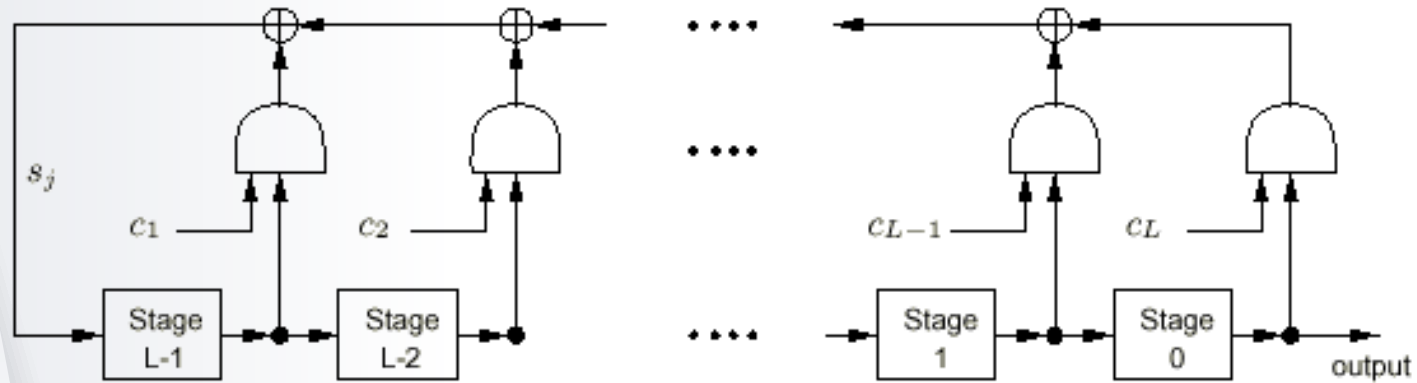
The LFSR is denoted  $\langle L, C(D) \rangle$ , where  
$$C(D) = 1 + c_1 D + c_2 D^2 + \dots + c_L D^L \in \mathbb{Z}_2[D]$$
  
is the *connection polynomial*.





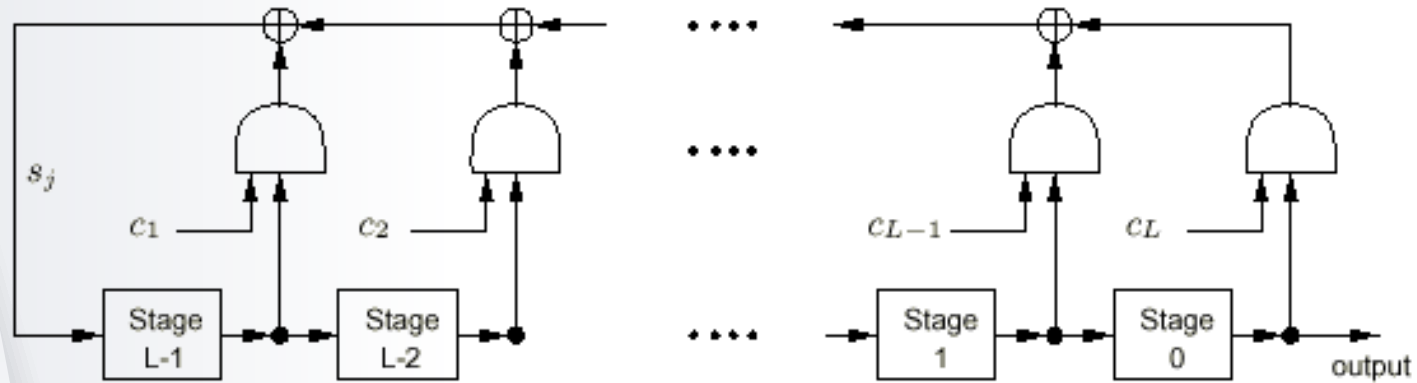
The LFSR is said to be **non-singular** if the degree of  $C(D)$  is  $L$  (that is  $\mathbf{c}_L=1$ ).

$$C(D) = 1 + c_1 D + c_2 D^2 + \dots + c_L D^L \in \mathbb{Z}_2[D]$$



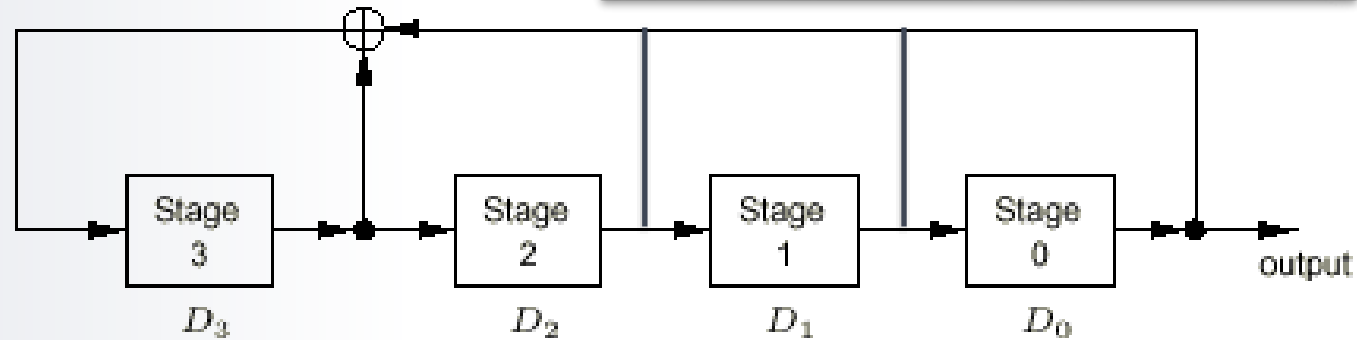
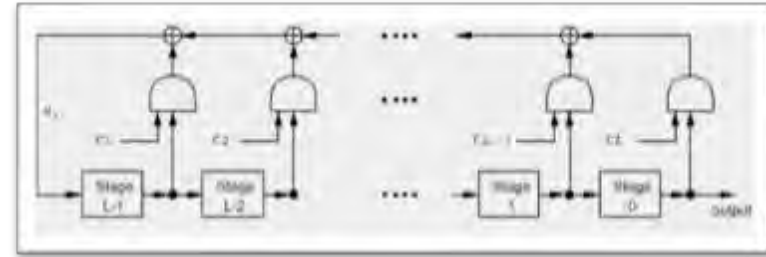


If the initial content of stage  $i$  is  $s_i \in \{0,1\}$  for each  $i$ ,  $0 \leq i \leq L-1$ , then  $[s_{L-1}, \dots, s_1, s_0]$  is called the *initial state* of the LFSR.



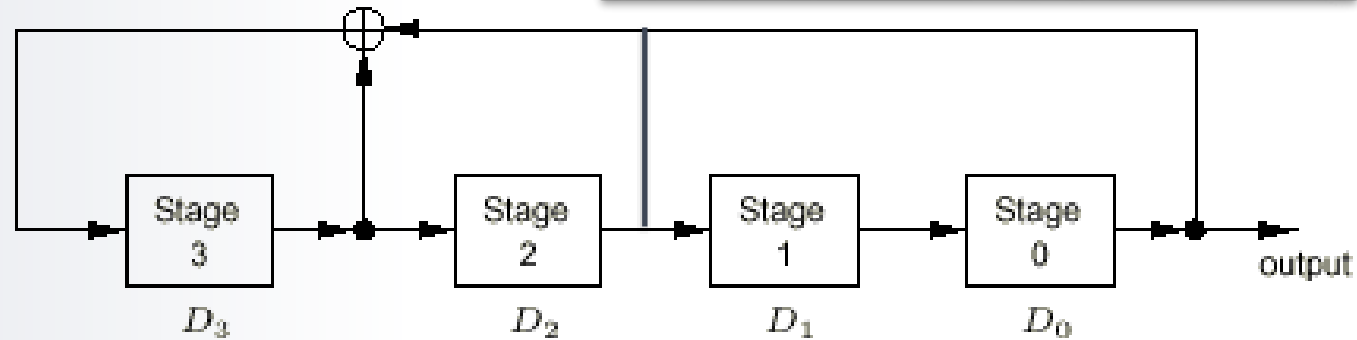
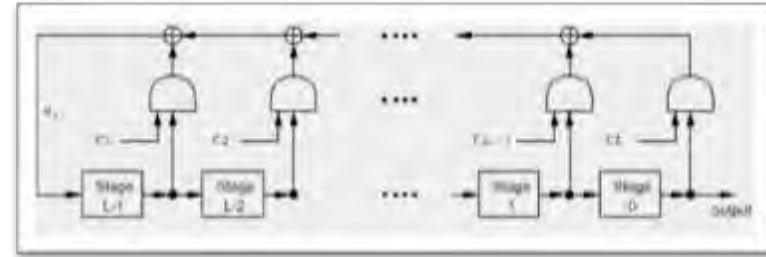
# Example

Consider the LFSR  $\langle 4, 1 + D + D^4 \rangle$ , depicted in the figure below.



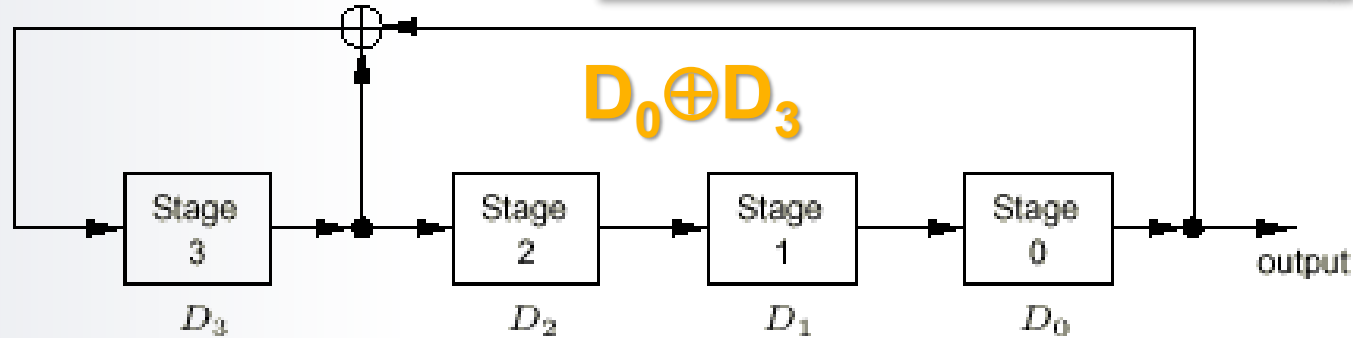
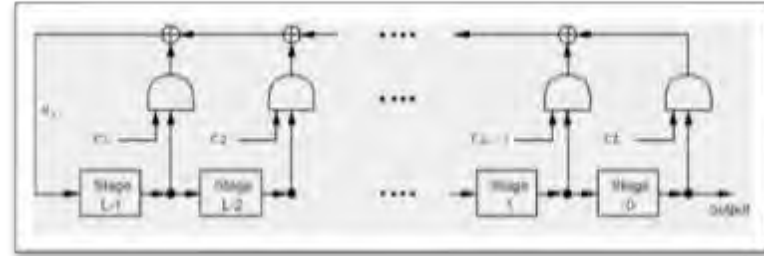
# Example

Consider the LFSR  $\langle 4, 1 + D + D^4 \rangle$ , depicted in the figure below.



# Example

Consider the LFSR  $\langle 4, 1 + D + D^4 \rangle$ , depicted in the figure below.



If the initial state of the LFSR is  $[0, 0, 0, 0]$ , the output sequence is the zero sequence.

## Example

If the initial state of the LFSR is  $[0, 1, 1, 0]$ , The output sequence is

$s = 0, 1, 1, 0, 0, 1, 0, 0, 0, 1, 1, 1, 1, 0, 1, \dots$ ,

and is periodic with period **15**.



| t | D3 | D2 | D1 | D0 |
|---|----|----|----|----|
| 0 | 0  | 1  | 1  | 0  |

## Example

If the initial state of the LFSR is  $[0, 1, 1, 0]$ , The output sequence is

$$s = 0, 1, 1, 0, 0, 1, 0, 0, 0, 1, 1, 1, 1, 0, 1, \dots,$$

and is periodic with period **15**.

| t | D3 | D2 | D1 | D0 |
|---|----|----|----|----|
| 0 | 0  | 1  | 1  | 0  |
| 1 |    | 0  | 1  | 1  |

## Example

If the initial state of the LFSR is  $[0, 1, 1, 0]$ , The output sequence is

$s = 0, 1, 1, 0, 0, 1, 0, 0, 0, 1, 1, 1, 1, 0, 1, \dots$ ,

and is periodic with period **15**.

| t | D3 | D2 | D1 | D0 |
|---|----|----|----|----|
| 0 | 0  | 1  | 1  | 0  |
| 1 | 0  | 0  | 1  | 1  |

## Example

If the initial state of the LFSR is  $[0, 1, 1, 0]$ , The output sequence is

$$s = 0, 1, 1, 0, 0, 1, 0, 0, 0, 1, 1, 1, 1, 0, 1, \dots,$$

and is periodic with period **15**.

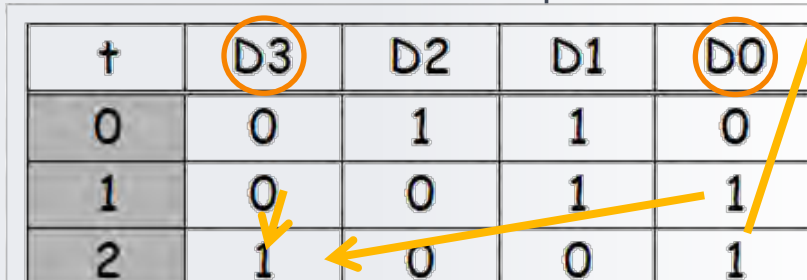
| t | D3 | D2 | D1 | D0 |
|---|----|----|----|----|
| 0 | 0  | 1  | 1  | 0  |
| 1 | 0  | 0  | 1  | 1  |
| 2 |    | 0  | 0  | 1  |

## Example

If the initial state of the LFSR is  $[0, 1, 1, 0]$ , The output sequence is

$$s = 0, 1, 1, 0, 0, 1, 0, 0, 0, 1, 1, 1, 1, 0, 1, \dots,$$

and is periodic with period **15**.



| t | D3 | D2 | D1 | D0 |
|---|----|----|----|----|
| 0 | 0  | 1  | 1  | 0  |
| 1 | 0  | 0  | 1  | 1  |
| 2 | 1  | 0  | 0  | 1  |

## Example

If the initial state of the LFSR is  $[0, 1, 1, 0]$ , The output sequence is

$$s = 0, 1, 1, 0, 0, 1, 0, 0, 0, 1, 1, 1, 1, 0, 1, \dots,$$

and is periodic with period **15**.

| t | D3 | D2 | D1 | D0 |
|---|----|----|----|----|
| 0 | 0  | 1  | 1  | 0  |
| 1 | 0  | 0  | 1  | 1  |
| 2 | 1  | 0  | 0  | 1  |
| 3 | 0  | 1  | 0  | 0  |
| 4 | 0  | 0  | 1  | 0  |
| 5 | 0  | 0  | 0  | 1  |
| 6 | 1  | 0  | 0  | 0  |
| 7 | 1  | 1  | 0  | 0  |

| t  | D3 | D2 | D1 | D0 |
|----|----|----|----|----|
| 8  | 1  | 1  | 1  | 0  |
| 9  | 1  | 1  | 1  | 1  |
| 10 | 0  | 1  | 1  | 1  |
| 11 | 1  | 0  | 1  | 1  |
| 12 | 0  | 1  | 0  | 1  |
| 13 | 1  | 0  | 1  | 0  |
| 14 | 1  | 1  | 0  | 1  |
| 15 | 0  | 1  | 1  | 0  |

The background features a large orange area on the left and a white area on the right, separated by a diagonal line. On the right side, there are several overlapping, semi-transparent white shapes that resemble folded paper or layered planes, creating a sense of depth and movement.

# Facts

# Facts

Every output sequence (i.e., for all possible initial states) of an LFSR is **periodic if and only** if the connection polynomial  $C(D)$  has **degree**  $L$ .



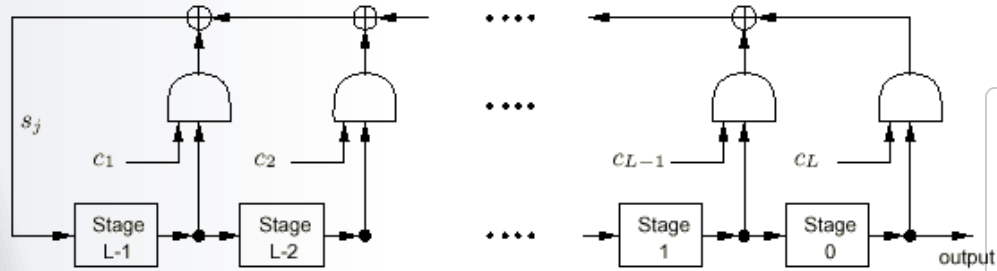
# Facts

If an LFSR is *singular* (i.e.,  $C(D)$  has degree less than  $L$ ), then **not all output sequences are periodic.**



# Facts

For the remainder of this chapter, it will be **assumed** that all LFSRs are **non-singular**.



$$C(D) = 1 + c_1 D + c_2 D^2 + \dots + c_L D^L$$



# Facts

*Periods of LFSR output sequences.* Let  $C(D) \in \mathbb{Z}_2[D]$  be a connection polynomial of degree  $L$ .

(i) If  $C(D)$  is **irreducible** over  $\mathbb{Z}_2$ , then each of the  $2^L - 1$  non-zero initial states of the **non-singular** LFSR  $\langle L, C(D) \rangle$  produces an output sequence with period equal to the **least positive integer  $N$**  such that  **$C(D)$  divides  $1 + D^N$**  in  $\mathbb{Z}_2[D]$ .

Note: it is always the case that this  $N$  is a divisor of  $2^L - 1$



# Facts

*Periods of LFSR output sequences.* Let  $C(D) \in \mathbb{Z}_2[D]$  be a connection polynomial of degree  $L$ .

(ii) If  $C(D)$  is a **primitive** polynomial, then each of the  $2^L - 1$  non-zero initial states of the **non-singular** LFSR  $\langle L, C(D) \rangle$  produces an output sequence with **maximum possible period  $2^L - 1$** .



## Definition

If  $C(D) \in \mathbb{Z}_2[D]$  is a primitive polynomial of degree  $L$ , then  $\langle L, C(D) \rangle$  is called a *maximum-length LFSR*.

The output of a maximum-length LFSR with non-zero initial state is called an *m-sequence*.

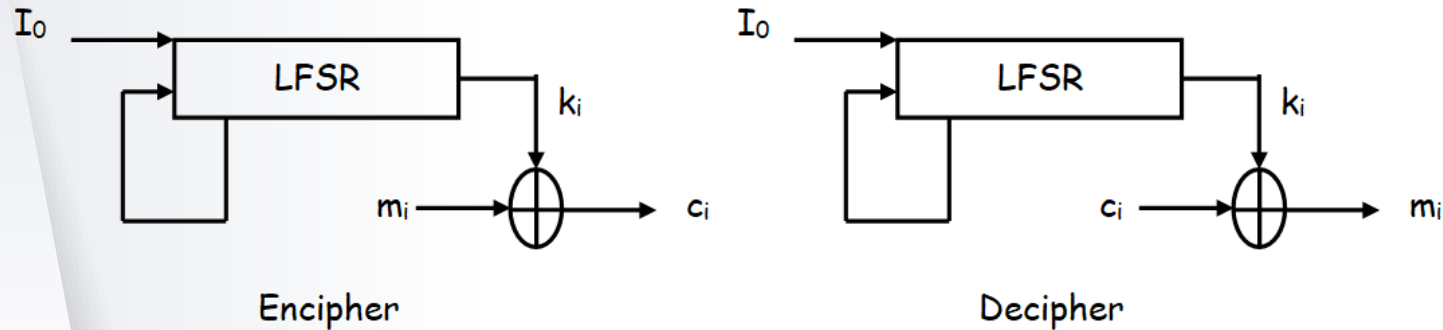


# Facts

A binary message stream  $M=m_1 m_2 \dots$  is enciphered by computing:

$$c_i = m_i \oplus k_i$$

As the bits of the key stream are generated as shown in the following figure:



Encryption with LFSR

# THANK YOU

**Any questions?**

**You can find me at:**

**[saad.m@sc.uobaghdad.edu.iq](mailto:saad.m@sc.uobaghdad.edu.iq)**

**Saad Al-Momen**

# Stream Ciphers

**CIPHER SYSTEMS**

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**Department of Mathematics**  
**College of Science - University of Baghdad**

**11.**

# Stream Cipher Algorithms



# *Stream Cipher Algorithms*

In this part, we'll discuss some of stream cipher algorithms. We'll explain those algorithms in details so that we can recognize their registers and also the type of connections or functions of connections.





# 1. Exclusive-OR Algorithm



$$z_i = a_i \oplus b_i$$

$$Z = A \oplus B = \bar{A}B + A\bar{B}$$

When the  **$\gcd(M, N) = 1$** , the period length of the final sequence is  **$(2^M - 1)(2^N - 1)$** , which is the **maximum period**.

| $A$ | $B$ | $A \oplus B$ | $\bar{A}$ | $\bar{B}$ | $\bar{A}B$ | $A\bar{B}$ | $\bar{A}B + A\bar{B}$ |
|-----|-----|--------------|-----------|-----------|------------|------------|-----------------------|
|     |     |              |           |           |            |            |                       |
|     |     |              |           |           |            |            |                       |
|     |     |              |           |           |            |            |                       |
|     |     |              |           |           |            |            |                       |

| $A$ | $B$ | $A \oplus B$ | $\bar{A}$ | $\bar{B}$ | $\bar{A}B$ | $A\bar{B}$ | $\bar{A}B + A\bar{B}$ |
|-----|-----|--------------|-----------|-----------|------------|------------|-----------------------|
| 0   |     |              |           |           |            |            |                       |
| 0   |     |              |           |           |            |            |                       |
| 1   |     |              |           |           |            |            |                       |
| 1   |     |              |           |           |            |            |                       |

| $A$ | $B$ | $A \oplus B$ | $\bar{A}$ | $\bar{B}$ | $\bar{A}B$ | $A\bar{B}$ | $\bar{A}B + A\bar{B}$ |
|-----|-----|--------------|-----------|-----------|------------|------------|-----------------------|
| 0   | 0   |              |           |           |            |            |                       |
| 0   | 1   |              |           |           |            |            |                       |
| 1   | 0   |              |           |           |            |            |                       |
| 1   | 1   |              |           |           |            |            |                       |

| $A$ | $B$ | $A \oplus B$ | $\bar{A}$ | $\bar{B}$ | $\bar{A}B$ | $A\bar{B}$ | $\bar{A}B + A\bar{B}$ |
|-----|-----|--------------|-----------|-----------|------------|------------|-----------------------|
| 0   | 0   | 0            |           |           |            |            |                       |
| 0   | 1   | 1            |           |           |            |            |                       |
| 1   | 0   | 1            |           |           |            |            |                       |
| 1   | 1   | 0            |           |           |            |            |                       |

| $A$ | $B$ | $A \oplus B$ | $\bar{A}$ | $\bar{B}$ | $\bar{A}B$ | $A\bar{B}$ | $\bar{A}B + A\bar{B}$ |
|-----|-----|--------------|-----------|-----------|------------|------------|-----------------------|
| 0   | 0   | 0            | 1         |           |            |            |                       |
| 0   | 1   | 1            | 1         |           |            |            |                       |
| 1   | 0   | 1            | 0         |           |            |            |                       |
| 1   | 1   | 0            | 0         |           |            |            |                       |

| $A$ | $B$ | $A \oplus B$ | $\bar{A}$ | $\bar{B}$ | $\bar{A}B$ | $A\bar{B}$ | $\bar{A}B + A\bar{B}$ |
|-----|-----|--------------|-----------|-----------|------------|------------|-----------------------|
| 0   | 0   | 0            | 1         | 1         |            |            |                       |
| 0   | 1   | 1            | 1         | 0         |            |            |                       |
| 1   | 0   | 1            | 0         | 1         |            |            |                       |
| 1   | 1   | 0            | 0         | 0         |            |            |                       |

| $A$ | $B$ | $A \oplus B$ | $\bar{A}$ | $\bar{B}$ | $\bar{A}B$ | $A\bar{B}$ | $\bar{A}B + A\bar{B}$ |
|-----|-----|--------------|-----------|-----------|------------|------------|-----------------------|
| 0   | 0   | 0            | 1         | 1         | 0          |            |                       |
| 0   | 1   | 1            | 1         | 0         | 1          |            |                       |
| 1   | 0   | 1            | 0         | 1         | 0          |            |                       |
| 1   | 1   | 0            | 0         | 0         | 0          |            |                       |

| $A$ | $B$ | $A \oplus B$ | $\bar{A}$ | $\bar{B}$ | $\bar{A}B$ | $A\bar{B}$ | $\bar{A}B + A\bar{B}$ |
|-----|-----|--------------|-----------|-----------|------------|------------|-----------------------|
| 0   | 0   | 0            | 1         | 1         | 0          | 0          |                       |
| 0   | 1   | 1            | 1         | 0         | 1          | 0          |                       |
| 1   | 0   | 1            | 0         | 1         | 0          | 1          |                       |
| 1   | 1   | 0            | 0         | 0         | 0          | 0          |                       |

| $A$ | $B$ | $A \oplus B$ | $\bar{A}$ | $\bar{B}$ | $\bar{A}B$ | $A\bar{B}$ | $\bar{A}B + A\bar{B}$ |
|-----|-----|--------------|-----------|-----------|------------|------------|-----------------------|
| 0   | 0   | 0            | 1         | 1         | 0          | 0          | 0                     |
| 0   | 1   | 1            | 1         | 0         | 1          | 0          | 1                     |
| 1   | 0   | 1            | 0         | 1         | 0          | 1          | 1                     |
| 1   | 1   | 0            | 0         | 0         | 0          | 0          | 0                     |

| $A$ | $B$ | $A \oplus B$ | $\bar{A}$ | $\bar{B}$ | $\bar{A}B$ | $A\bar{B}$ | $\bar{A}B + A\bar{B}$ |
|-----|-----|--------------|-----------|-----------|------------|------------|-----------------------|
| 0   | 0   | 0            | 1         | 1         | 0          | 0          | 0                     |
| 0   | 1   | 1            | 1         | 0         | 1          | 0          | 1                     |
| 1   | 0   | 1            | 0         | 1         | 0          | 1          | 1                     |
| 1   | 1   | 0            | 0         | 0         | 0          | 0          | 0                     |

$$Z = A \oplus B = \bar{A}B + A\bar{B}$$



## 2. Hadamard Algorithm



$$z_i = a_i \cdot b_i$$

When the  **$\gcd(M, N) = 1$** , the period length of the final sequence is  **$(2^M - 1)(2^N - 1)$** , which is the **maximum period**.



~~$$z_i = a_i b_i$$~~

$$z_i = a_i + b_i + a_i b_i$$

Prove that

When the  **$\gcd(M,N)=1$** , the period length of the final sequence is  **$(2^M-1)(2^N-1)$** , which is the **maximum period**.

## Example

We have two linear feedback shift registers with **2** and **3** stages respectively, and the corresponding connection polynomials are

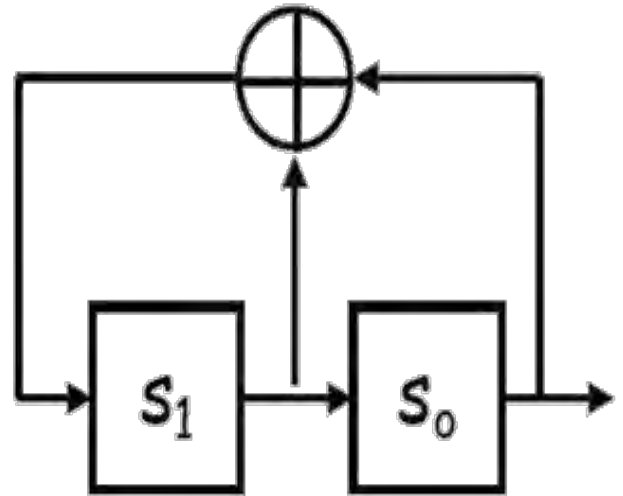
$$C_1(D)=1+D+D^2 \text{ and } C_2(D)=1+D^2+D^3,$$

With initial states **[1,1]** and **[1,1,1]** respectively.

Apply the **Hadamard** algorithm to find the resulting sequence.

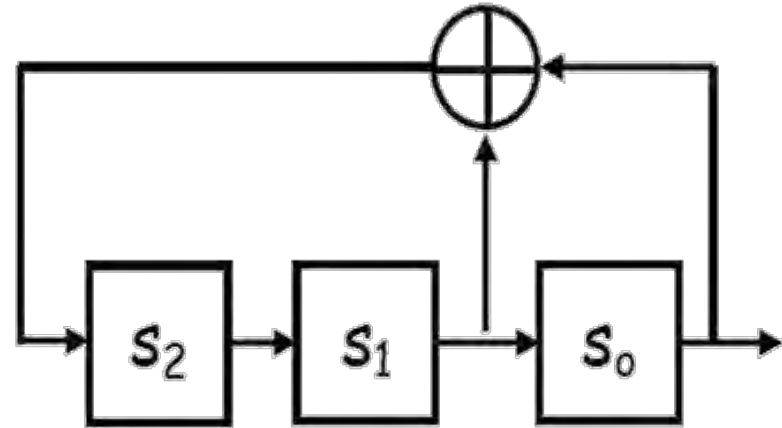
## Example

$$C_1(D) = 1 + D + D^2 \Rightarrow s_0 + s_1.$$



# Example

$$C_2(D) = 1 + D^2 + D^3 \Rightarrow s_0 + s_1.$$



|          | LFSR 1 $S_0+S_1$ |       |       |
|----------|------------------|-------|-------|
| T        | $S_1$            | $S_0$ | $a_i$ |
| 0        | 1                | 1     |       |
| 1        | 0                | 1     | 1     |
| 2        | 1                | 0     | 1     |
| 3        | 1                | 1     | 0     |
| 4        |                  |       |       |
| 5        |                  |       |       |
| 6        |                  |       |       |
| 7        |                  |       |       |
| Max per. | $2^2-1=3$        |       |       |
| Output   | 110110110110...  |       |       |

|          | LFSR 1 $S_0+S_1$ |       |       |
|----------|------------------|-------|-------|
| T        | $S_1$            | $S_0$ | $a_i$ |
| 0        | 1                | 1     |       |
| 1        | 0                | 1     | 1     |
| 2        | 1                | 0     | 1     |
| 3        | 1                | 1     | 0     |
| 4        |                  |       |       |
| 5        |                  |       |       |
| 6        |                  |       |       |
| 7        |                  |       |       |
| Max per. | $2^2-1=3$        |       |       |
| Output   | 110110110110...  |       |       |

| LFSR 2 $S_0+S_1$  |       |       |       |
|-------------------|-------|-------|-------|
| $S_2$             | $S_1$ | $S_0$ | $b_i$ |
| 1                 | 1     | 1     |       |
| 0                 | 1     | 1     | 1     |
| 0                 | 0     | 1     | 1     |
| 1                 | 0     | 0     | 1     |
| 0                 | 1     | 0     | 0     |
| 1                 | 0     | 1     | 0     |
| 1                 | 1     | 0     | 1     |
| 1                 | 1     | 1     | 0     |
| $2^3-1=7$         |       |       |       |
| 11100101110010... |       |       |       |

|          | LFSR 1 $S_0+S_1$ |       |       |
|----------|------------------|-------|-------|
| T        | $S_1$            | $S_0$ | $a_i$ |
| 0        | 1                | 1     |       |
| 1        | 0                | 1     | 1     |
| 2        | 1                | 0     | 1     |
| 3        | 1                | 1     | 0     |
| 4        |                  |       |       |
| 5        |                  |       |       |
| 6        |                  |       |       |
| 7        |                  |       |       |
| Max per. | $2^2-1=3$        |       |       |
| Output   | 110110110110...  |       |       |

| LFSR 2            |       |       | $s_0+s_1$ |
|-------------------|-------|-------|-----------|
| $s_2$             | $s_1$ | $s_0$ | $b_i$     |
| 1                 | 1     | 1     |           |
| 0                 | 1     | 1     | 1         |
| 0                 | 0     | 1     | 1         |
| 1                 | 0     | 0     | 1         |
| 0                 | 1     | 0     | 0         |
| 1                 | 0     | 1     | 0         |
| 1                 | 1     | 0     | 1         |
| 1                 | 1     | 1     | 0         |
| $2^3-1=7$         |       |       |           |
| 11100101110010... |       |       |           |

Since  $\gcd(3,7)=1$ , hence the period of the resulting sequence  $=3 \times 7=21$ .

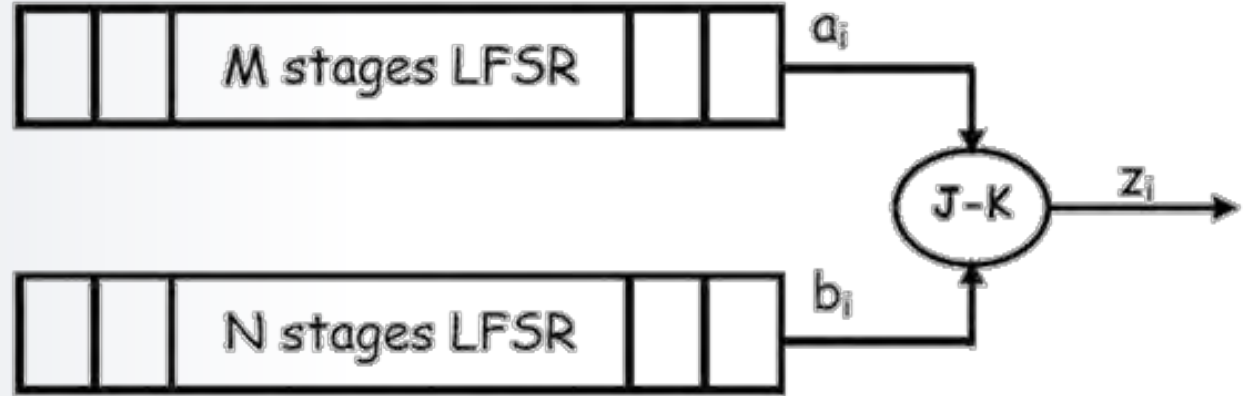
|    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|----|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| A= | 1 | 1 | 0 | 1 | 1 | 0 | 1 | 1 | 0 | 1 | 1 | 0 | 1 | 1 | 0 | 1 | 1 | 0 |
| B= | 1 | 1 | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 0 | 1 | 1 | 1 | 0 |
| Z= | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 1 | 1 | 0 |

## NOTE:

Approximately, **three to four** from the results are **zeros**, because of the **AND** operation.

So, the result of the algorithm **does not** satisfy the first randomness postulate.

### **3. J-K flip-flop Algorithm**



$$z_i = (a_i + b_i + 1) z_{i-1} + a_i$$

When the  **$\gcd(M,N)=1$** , the period length of the final sequence is  **$(2^M-1)(2^N-1)$** , which is the **maximum period**.

**Prove that** ↓

The truth table for J-K flip flop ( $z_i = (a_i + b_i + 1) z_{i-1} + a_i$ ) is:

| J | K | $z_{i+1}$   |
|---|---|-------------|
| 0 | 0 | $z_i$       |
| 0 | 1 | 0           |
| 1 | 0 | 1           |
| 1 | 1 | $\bar{z}_i$ |

## HW:

You have **two** linear feedback shift registers with **3** and **5** stages respectively, and the corresponding connection polynomials are  $C_1(D)=1+D+D^3$  and  $C_2(D)=1+D^3+D^5$ , with initial states **[1,0,1]** and **[1,0,0,1,1]** respectively. Apply the **J-K flip-flop** algorithm to find the first 35 digits of the resulting sequence.

# THANK YOU

**Any questions?**

**You can find me at:**

**[saad.m@sc.uobaghdad.edu.iq](mailto:saad.m@sc.uobaghdad.edu.iq)**

**Saad Al-Momen**

# Stream Ciphers

**CIPHER SYSTEMS**

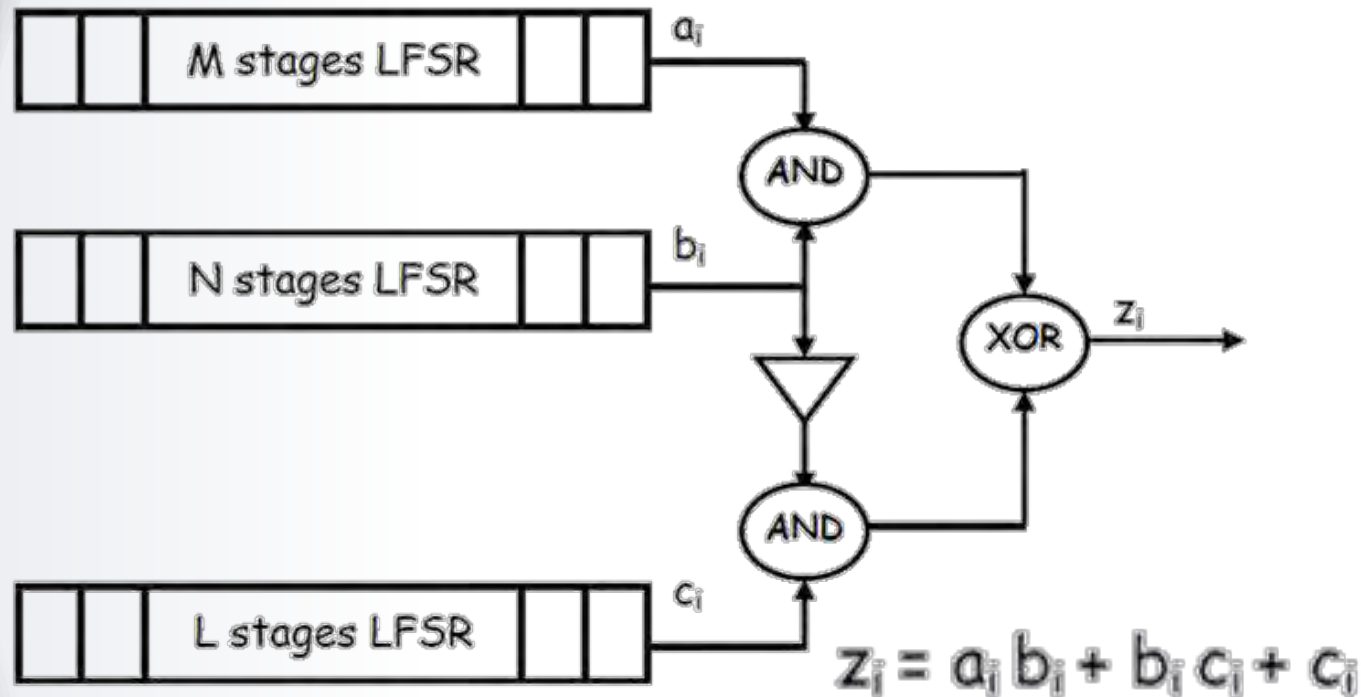
**Fourth Class  
Department of Mathematics  
College of Science - University of Baghdad**

**12.**

# Stream Cipher Algorithms



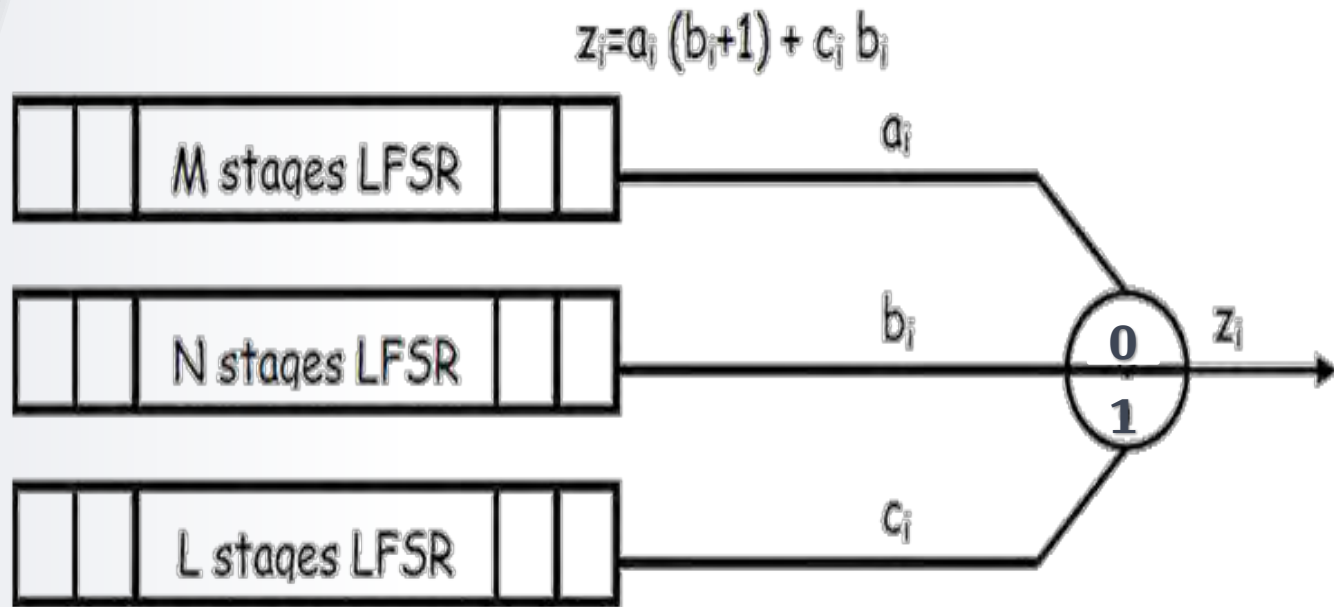
## 4. Geffe's Algorithm



When the  **$\gcd(M, N, L) = 1$** , the period length of the final sequence is  **$(2^M - 1)(2^N - 1)(2^L - 1)$** , which is the **maximum period**.



## 5. Police Algorithm



If  $b_i=0$  then  $z_i=a_i$ , and if  $b_i=1$  then  $z_i=c_i$

When the  $\text{gcd}(M,N,L)=1$ , the period length of the final sequence is  $(2^M-1)(2^N-1)(2^L-1)$ , which is the **maximum period**.



$$z_i = a_i (b_i + 1) + c_i b_i$$

If  $b_i = 0$  then  $z_i = a_i$

Let  $b_i = 0$

$$\begin{aligned} z_i &= a_i(0+1) + c_i(0) \\ &= a_i(1) = a_i \end{aligned}$$



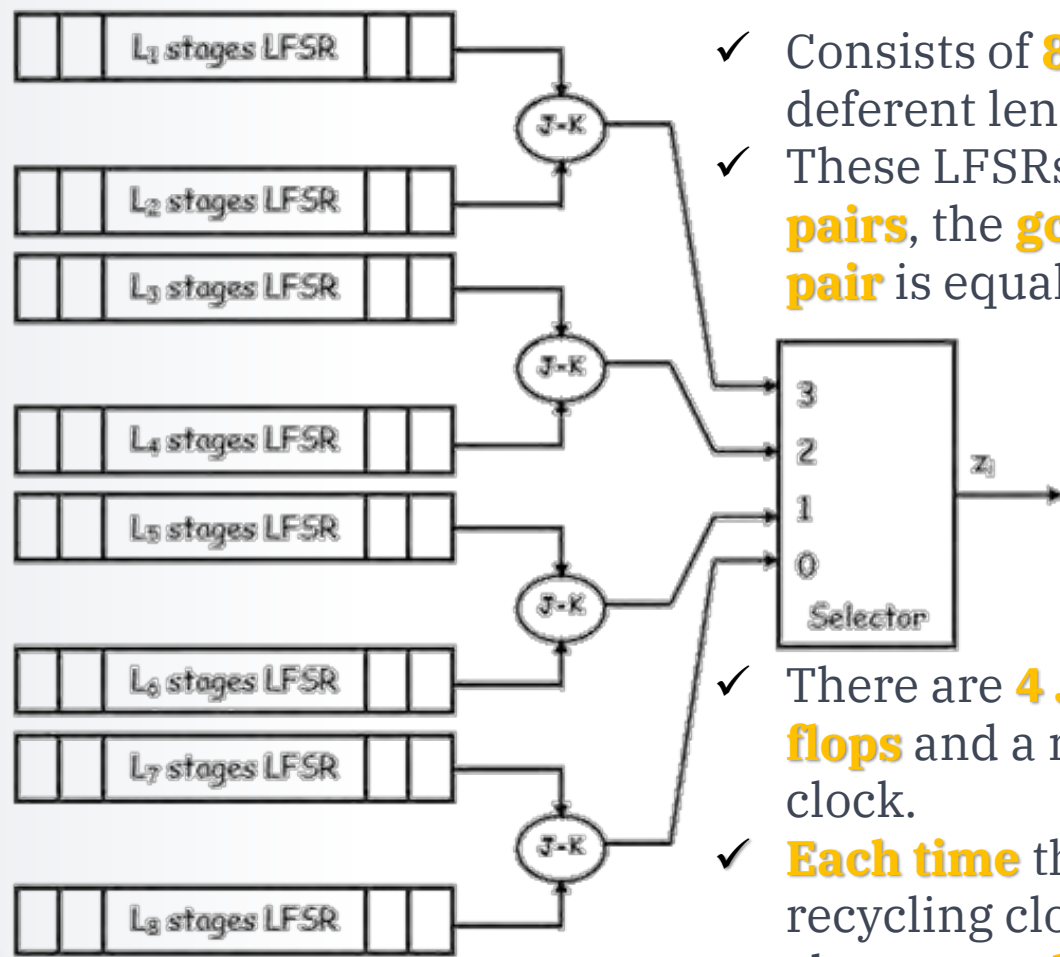
If  $b_i = 1$  then  $z_i = c_i$

Let  $b_i = 1$

$$\begin{aligned} z_i &= a_i(1+1) + c_i(1) \\ &= a_i(0) + c_i = c_i \end{aligned}$$



## 6. Pless's Algorithm



- ✓ Consists of **8 LFSRs** of different lengths.
- ✓ These LFSRs put in **4 pairs**, the **gcd of each pair** is equal to **one**.
- ✓ There are **4 J-K flip-flops** and a recycling clock.
- ✓ **Each time** the recycling clock will choose **one bit** from the four arrival bits

# Example

In Pless's algorithm, there are 4 shift registers pairs with the following output:

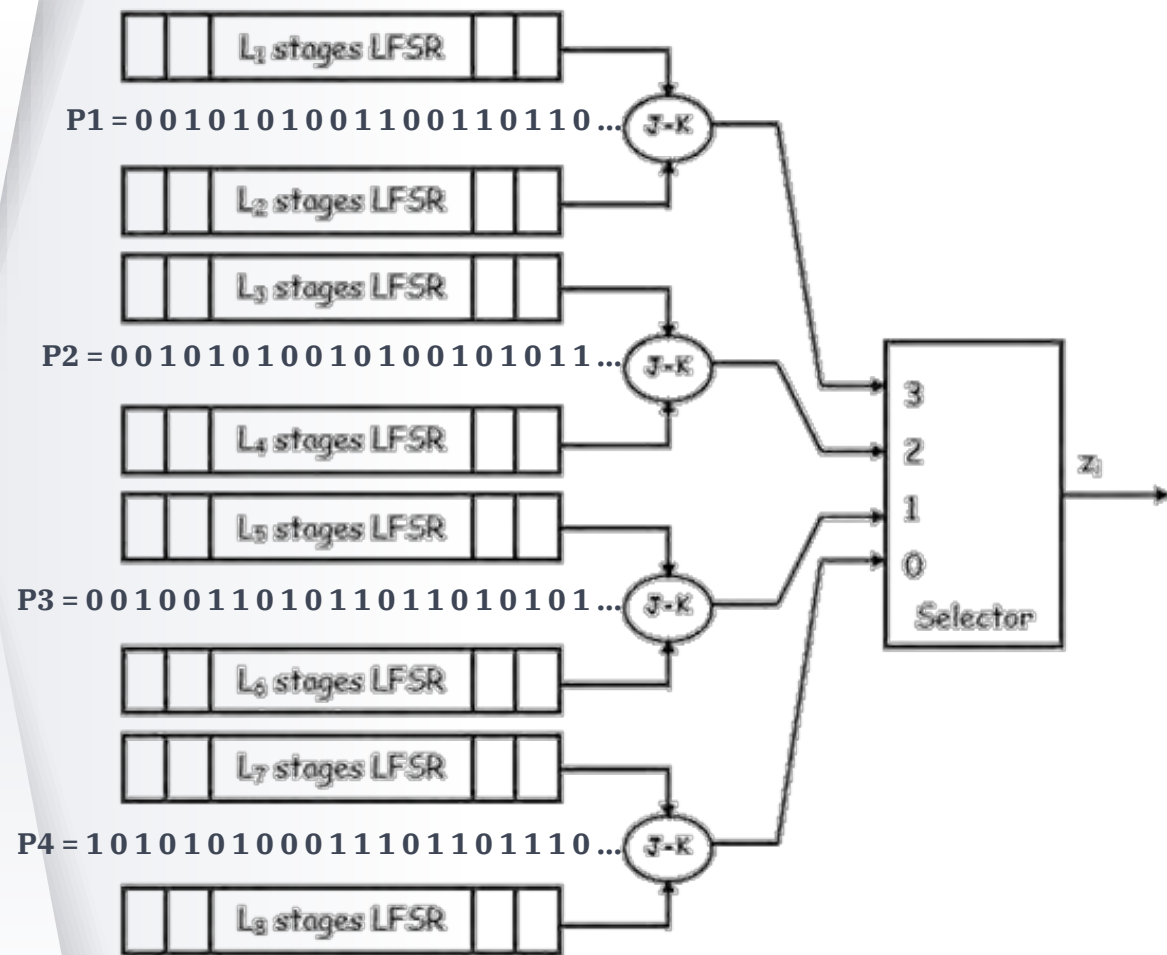
P1 = 0010101001100110110...

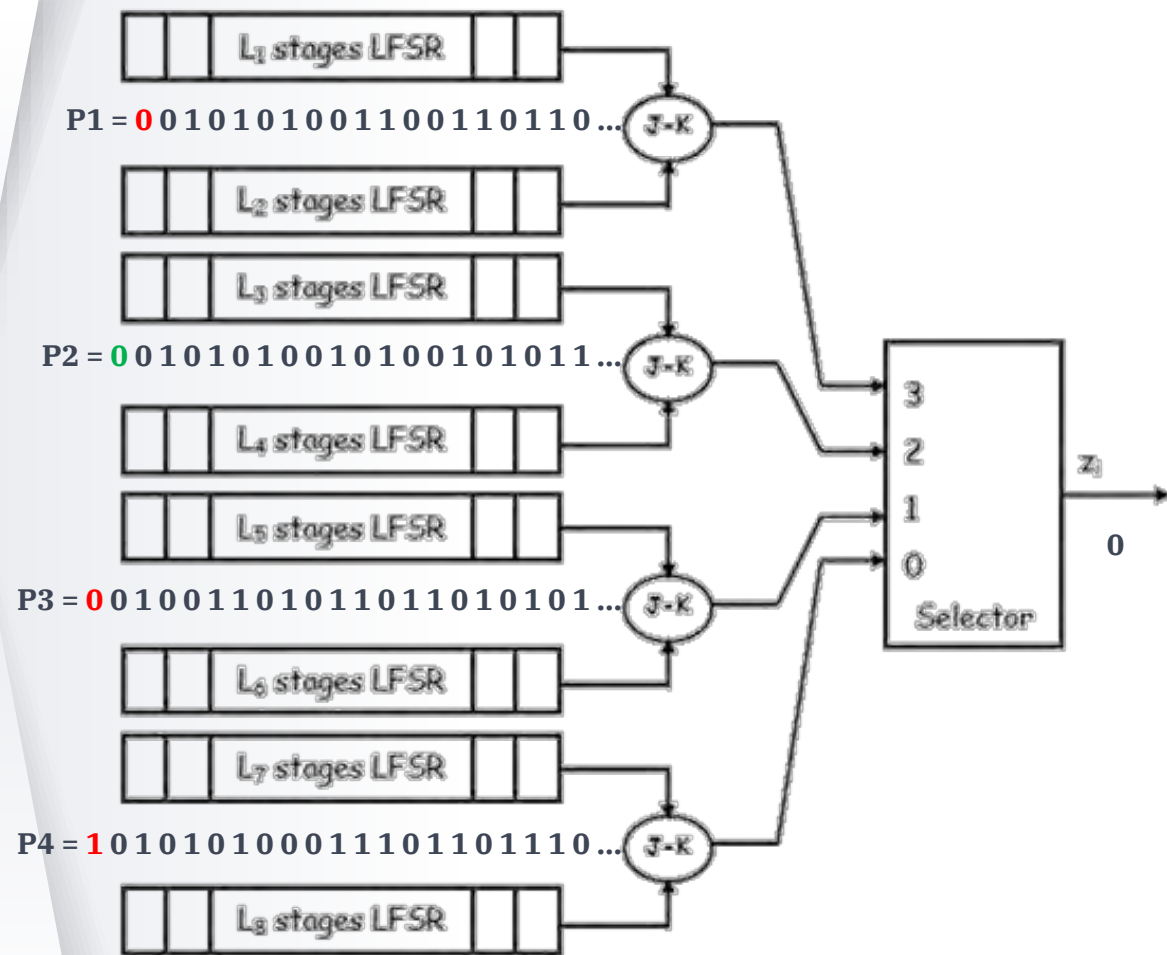
P2 = 00101010010100101011...

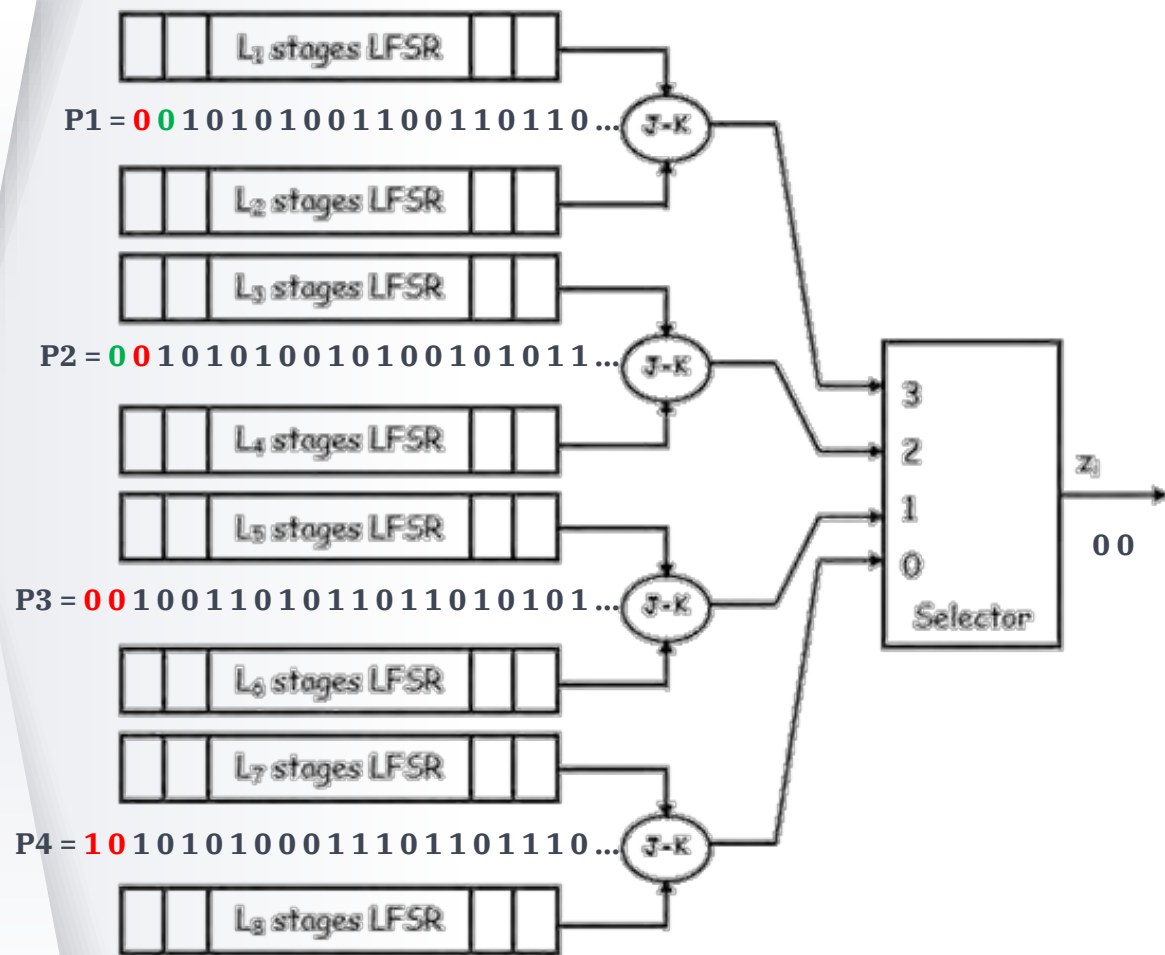
P3 = 001001101011011010101...

P4 = 101010100011101101110...

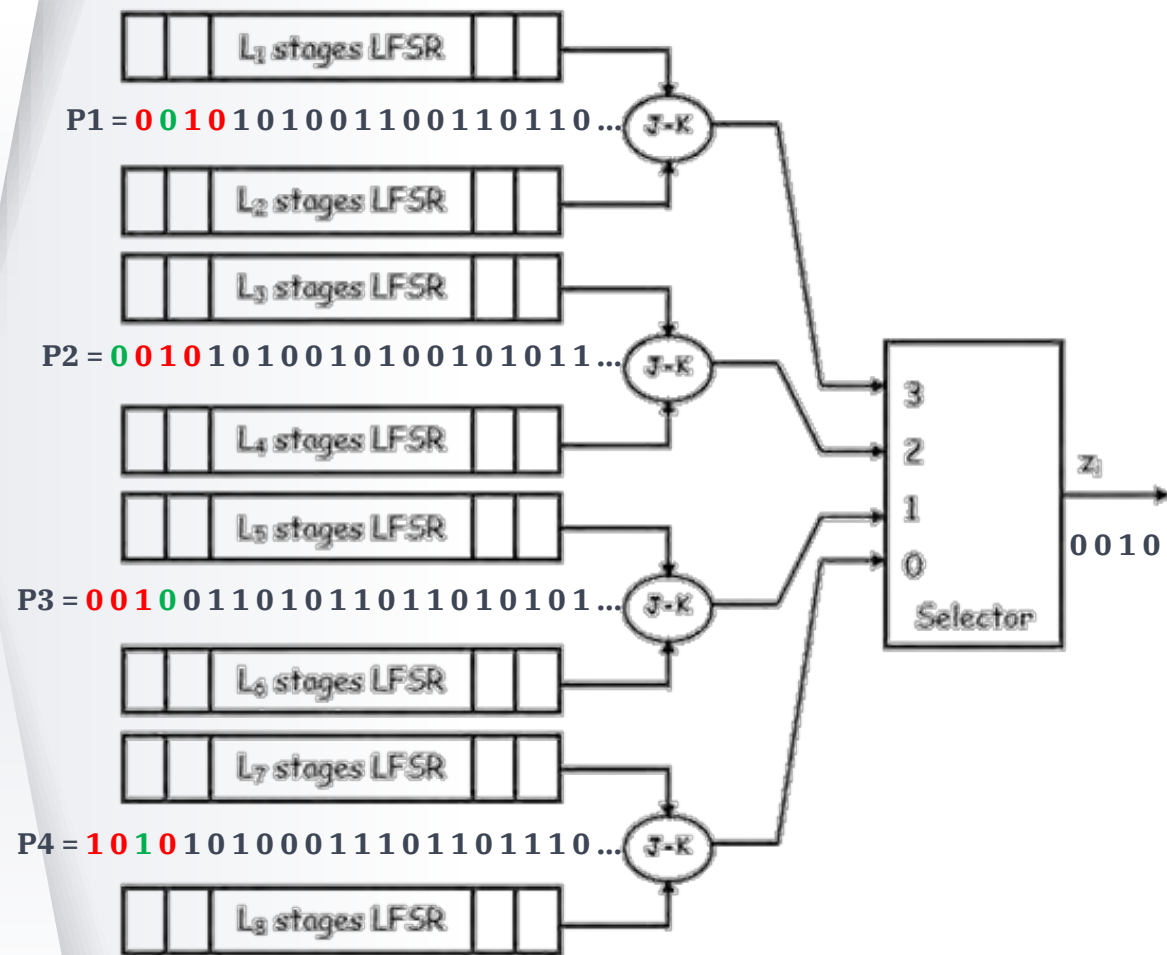
If the initial of the recycling clock is 2, what are the first 10 bits of the resulting sequence?

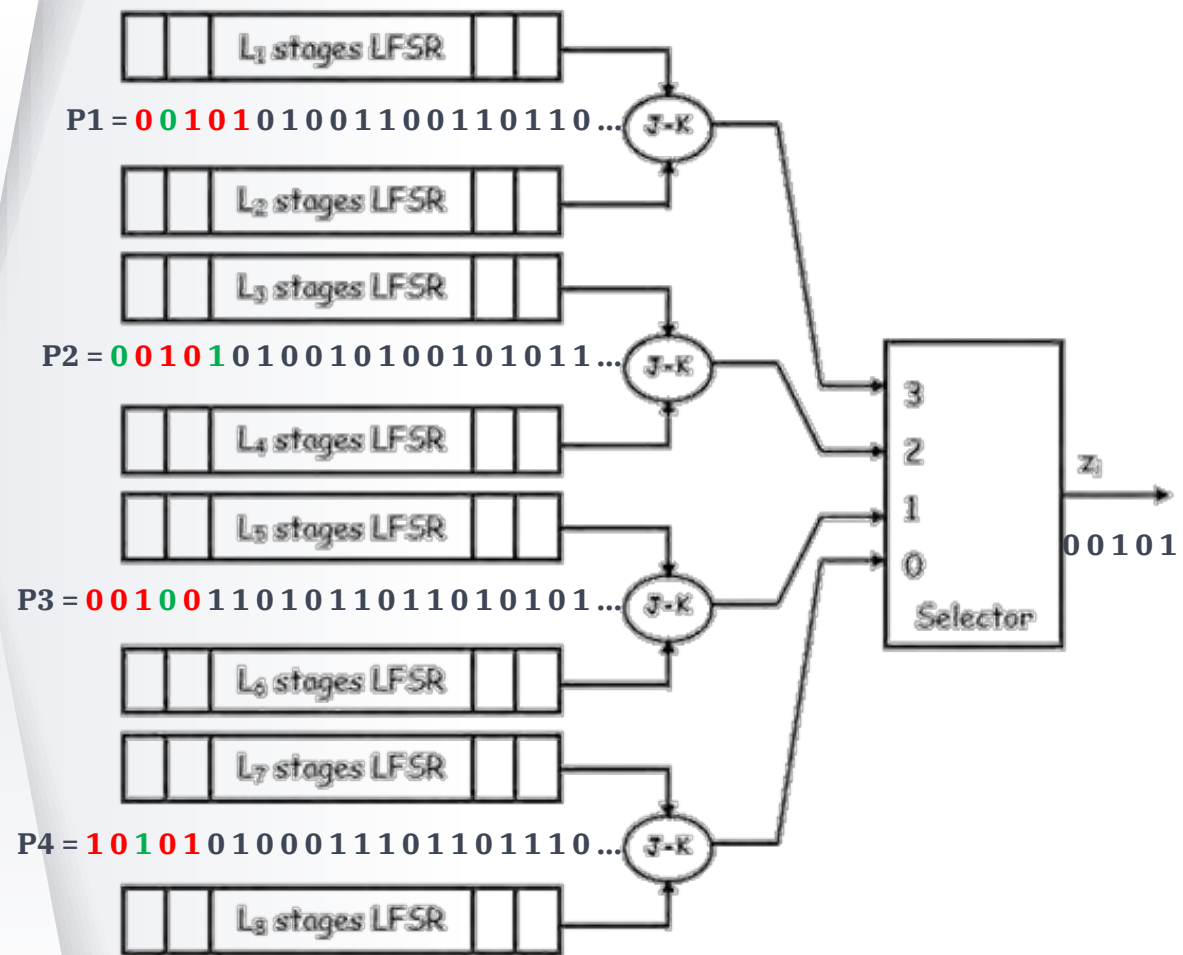












# THANK YOU

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**[saad.m@sc.uobaghdad.edu.iq](mailto:saad.m@sc.uobaghdad.edu.iq)**